



Textures – essential for high quality rendering

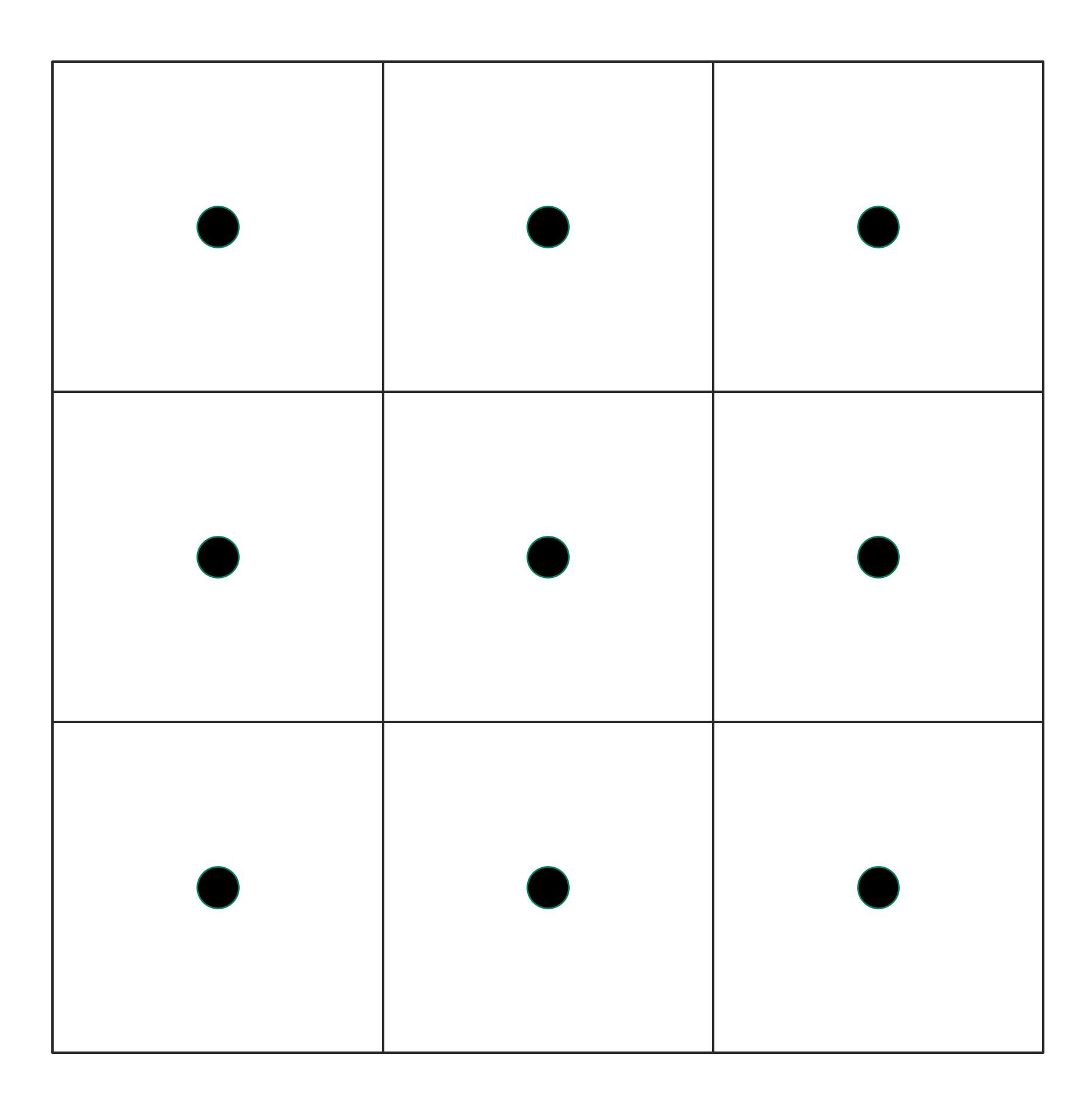


"Physically Based Rendering: From Theory To Implementation", 2004-2021 M. Pharr, W. Jakob, and G. Humphreys



Texture mapping – why we need filtering?

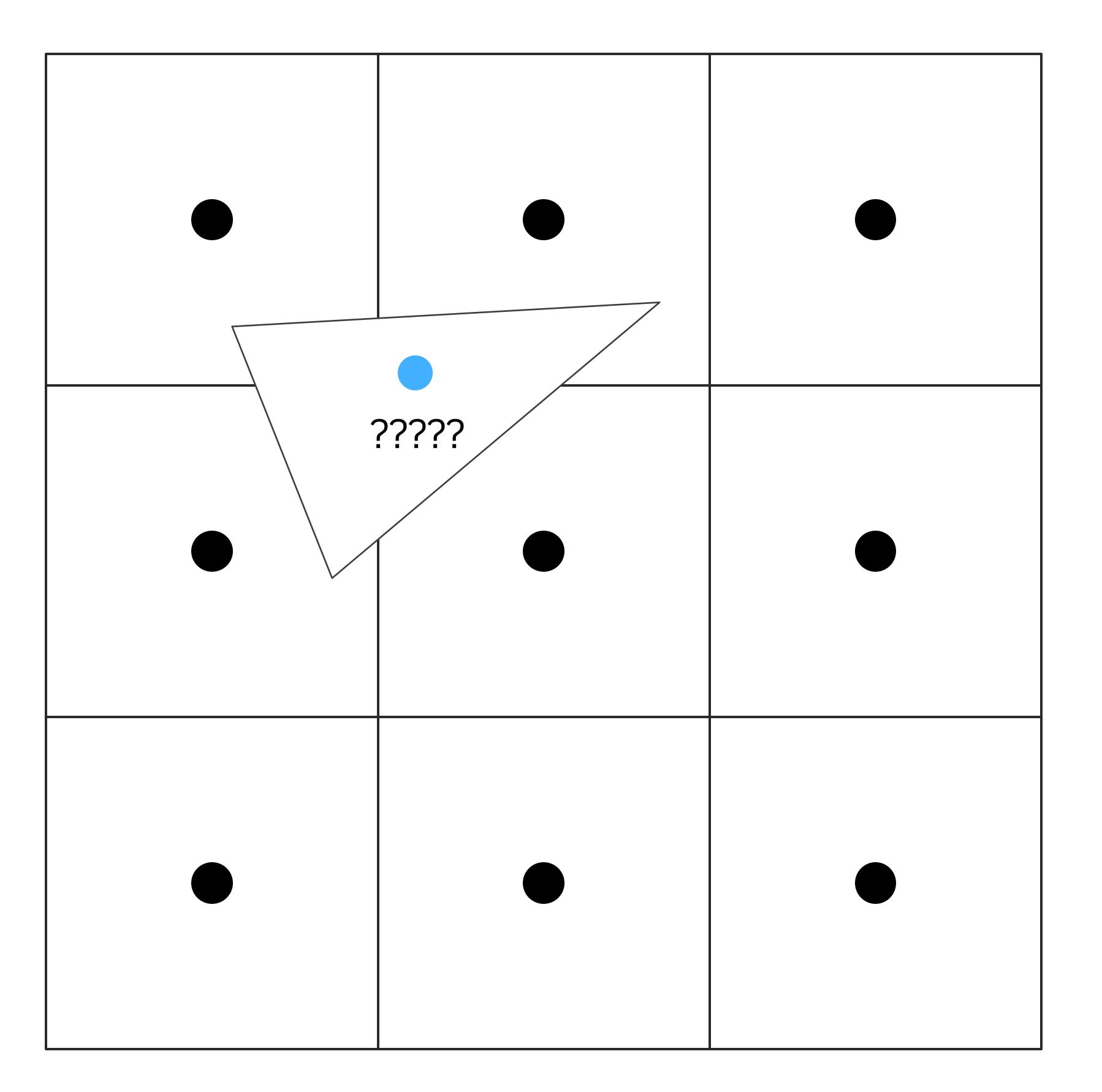
- Texture a 1D/2D/3D/4D grid of discrete values
- Values defined only at texel centers
- "Pixel/texel is not a little square!"
- Infinitely small point Dirac delta





Texture mapping – why we need filtering?

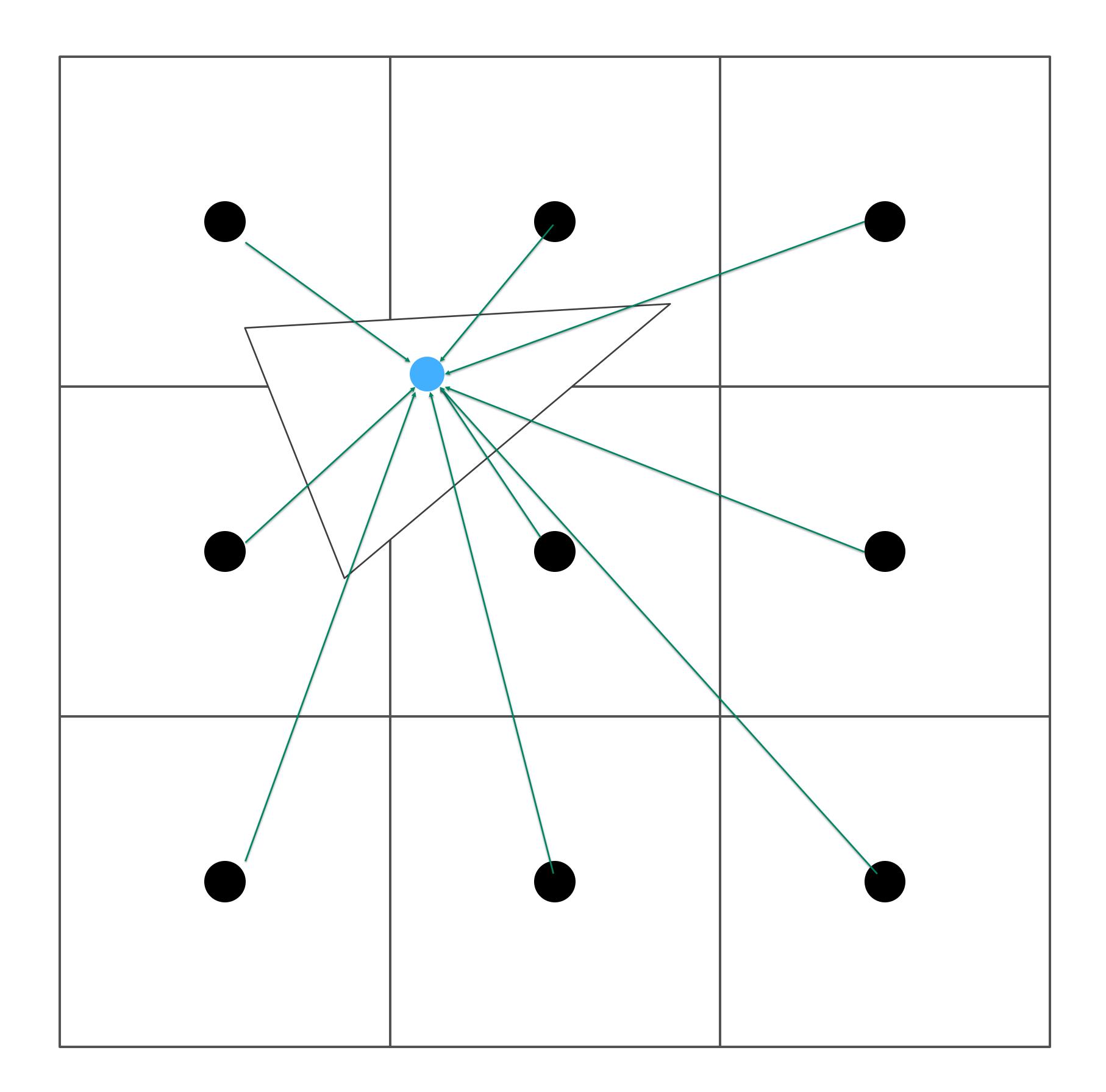
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- What happens between?





Texture mapping – why we need filtering?

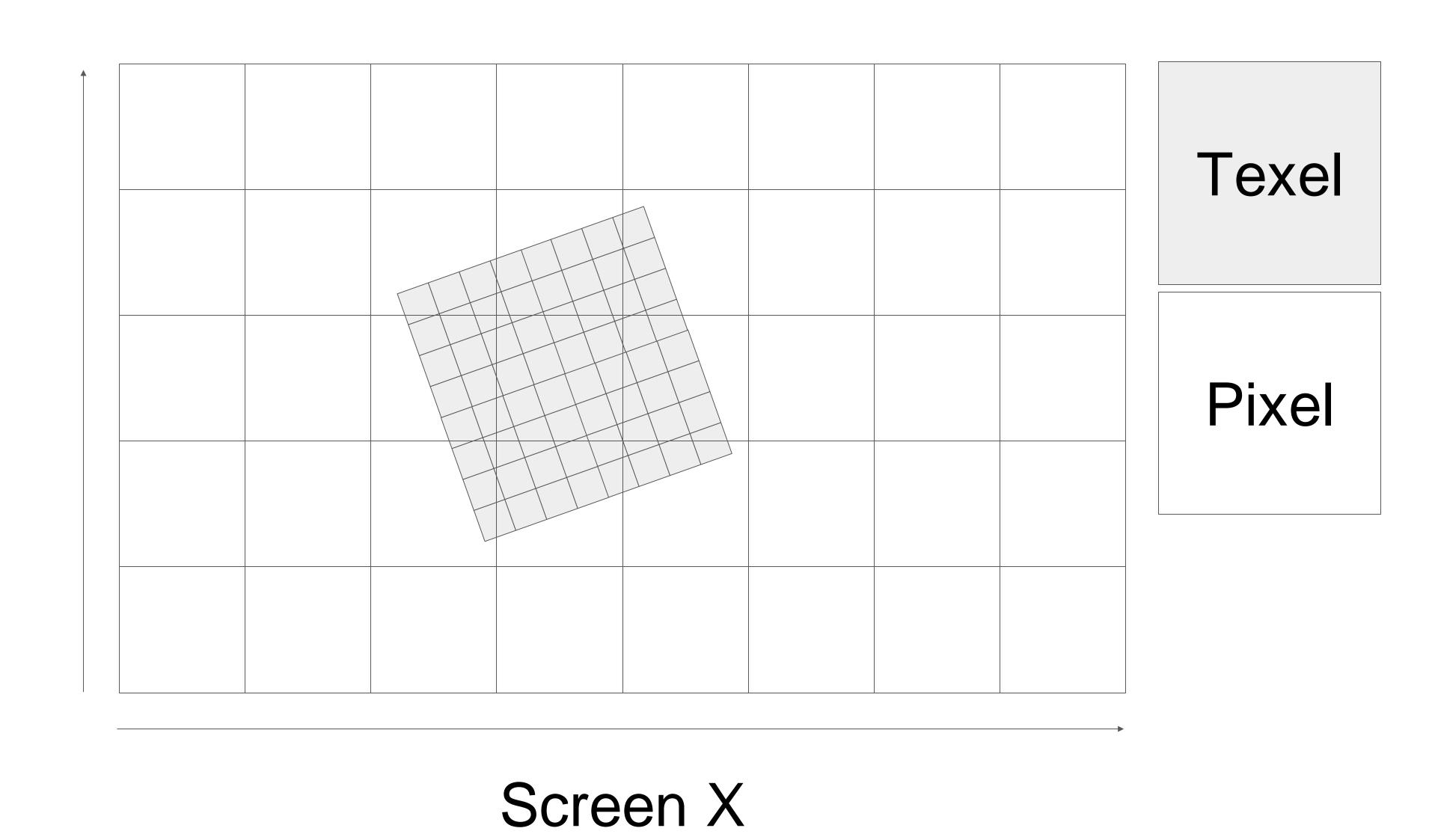
- Texture a 1D/2D/3D/4D grid of discrete values
- Values defined only at texel centers
- "Pixel/texel is not a little square!"
- Infinitely small point Dirac delta
- What happens between?
- Filtering and interpolation
- Weighted averaging of multiple texture samples





Texture filtering – minification

- Multiple texels might cover a single pixel area
- Potentially thousands (millions?) texels



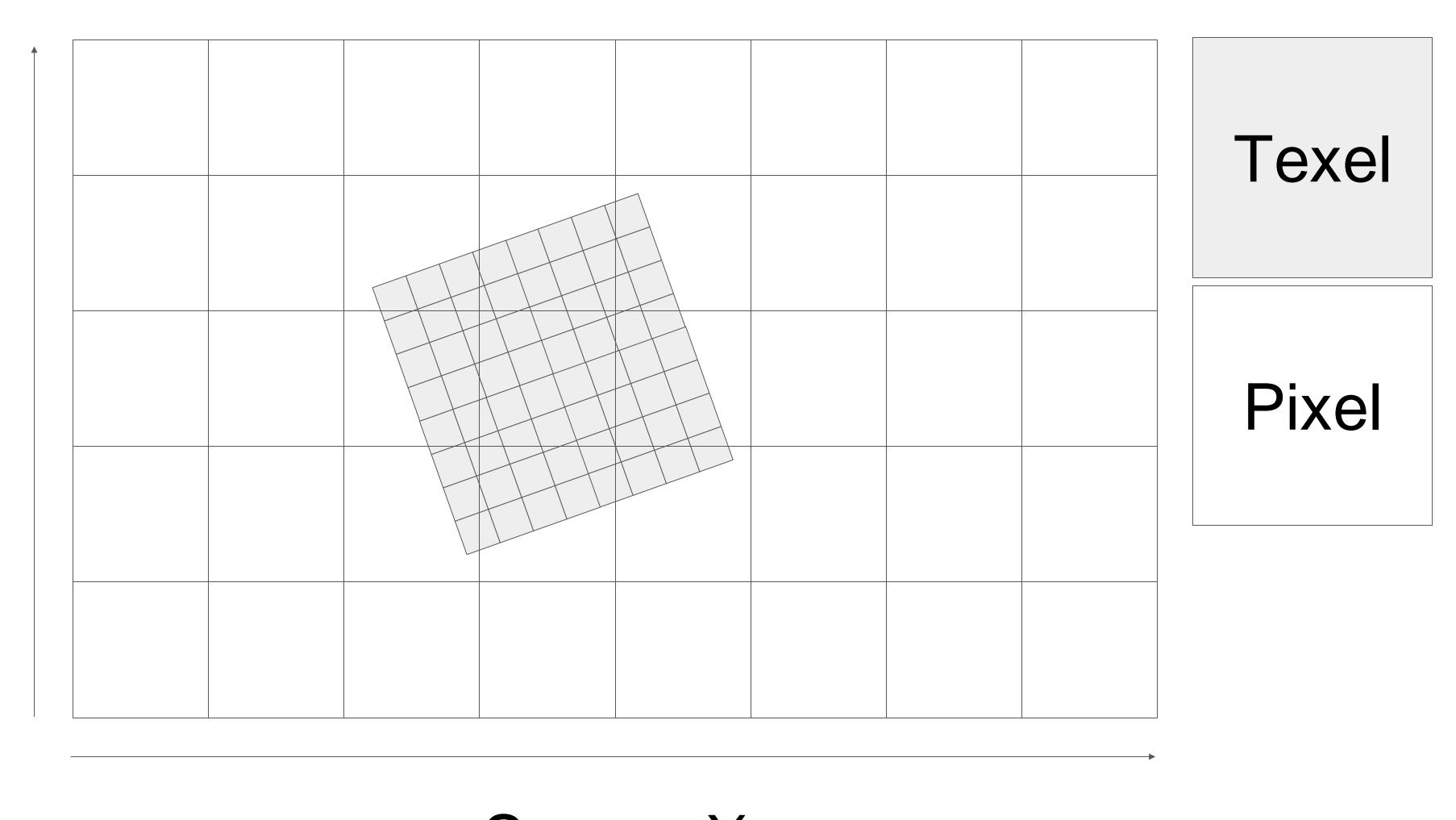


Texture filtering – minification

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Solution – full filter – EWA, anisotropic filtering:

- Possibly very slow
- Hundreds+ of texture samples
- Higher quality







Texture filtering – minification

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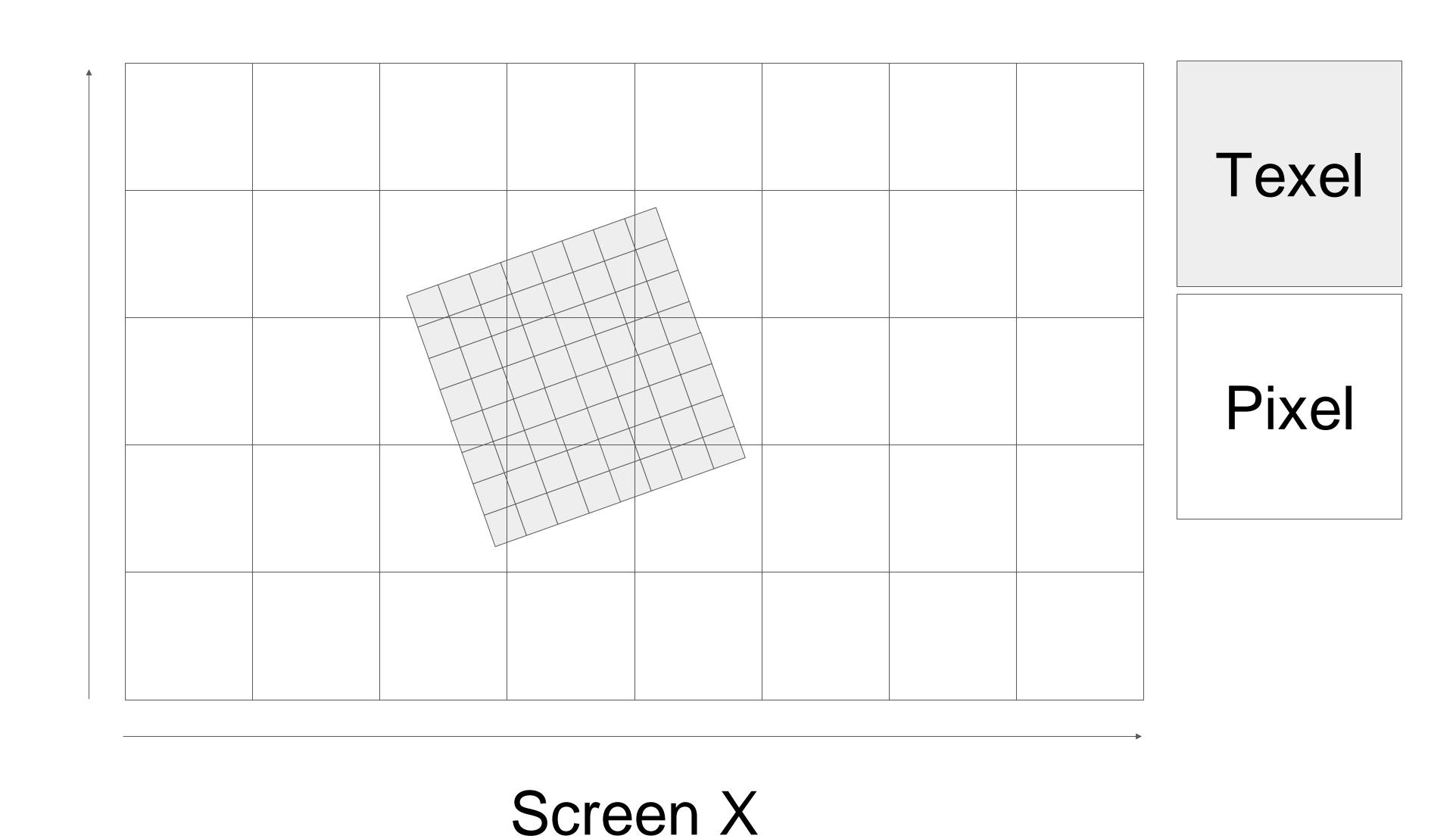
Solution – full filter – EWA, anisotropic filtering:

- Possibly very slow
- Hundreds+ of texture samples
- Higher quality

Solution – prefilter – precomputed mipmap pyramid:

- Very fast
- Low quality (blurry!)

(Often – hybrid, mipmapping + anisotropic/mip bias)





"Common knowledge"

Almost "axiomatic"

All modern graphics APIs standardize filtering

• Standard filters – (low-quality) bi/trilinear, anisotropic



"Common knowledge"

Almost "axiomatic"

All modern graphics APIs standardize filtering

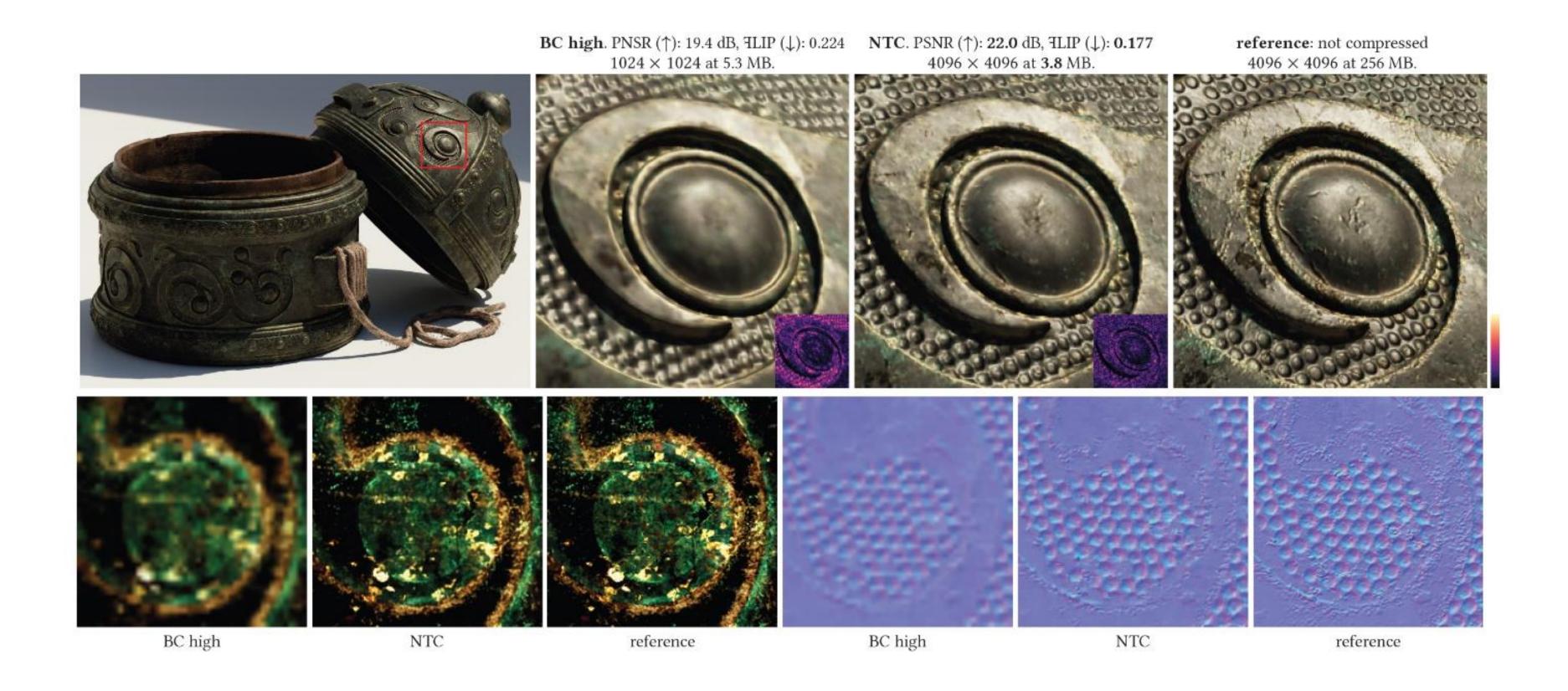
- Standard filters (low-quality) bi/trilinear, anisotropic
- All modern GPUs have dedicated filtering hardware
- Very easy and attractive to use without questioning

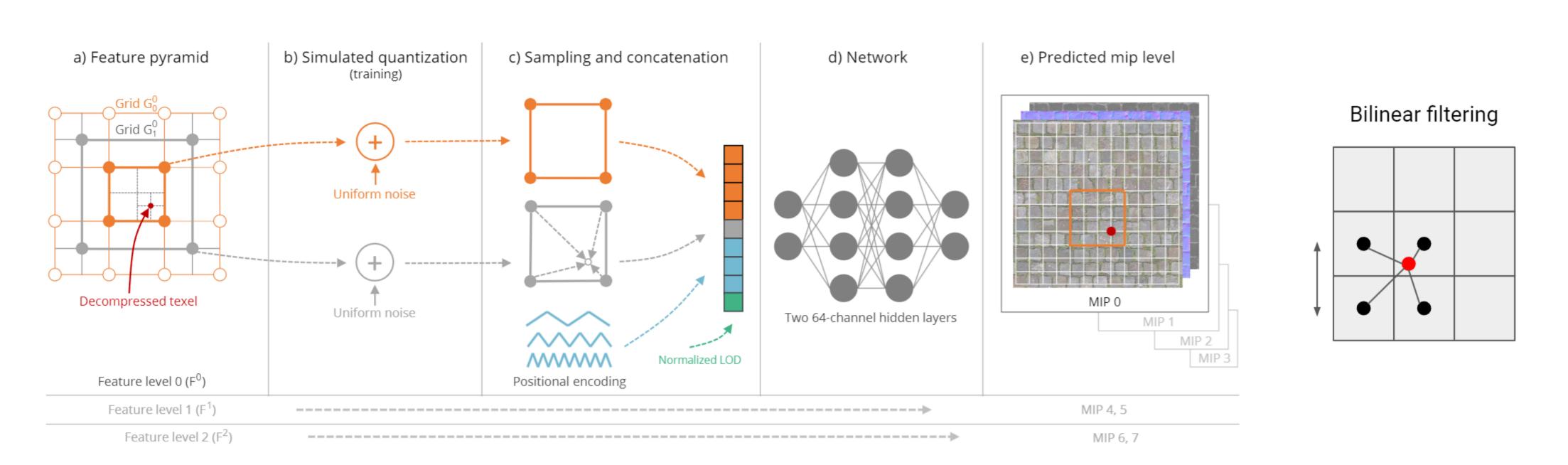
Feedback loop!





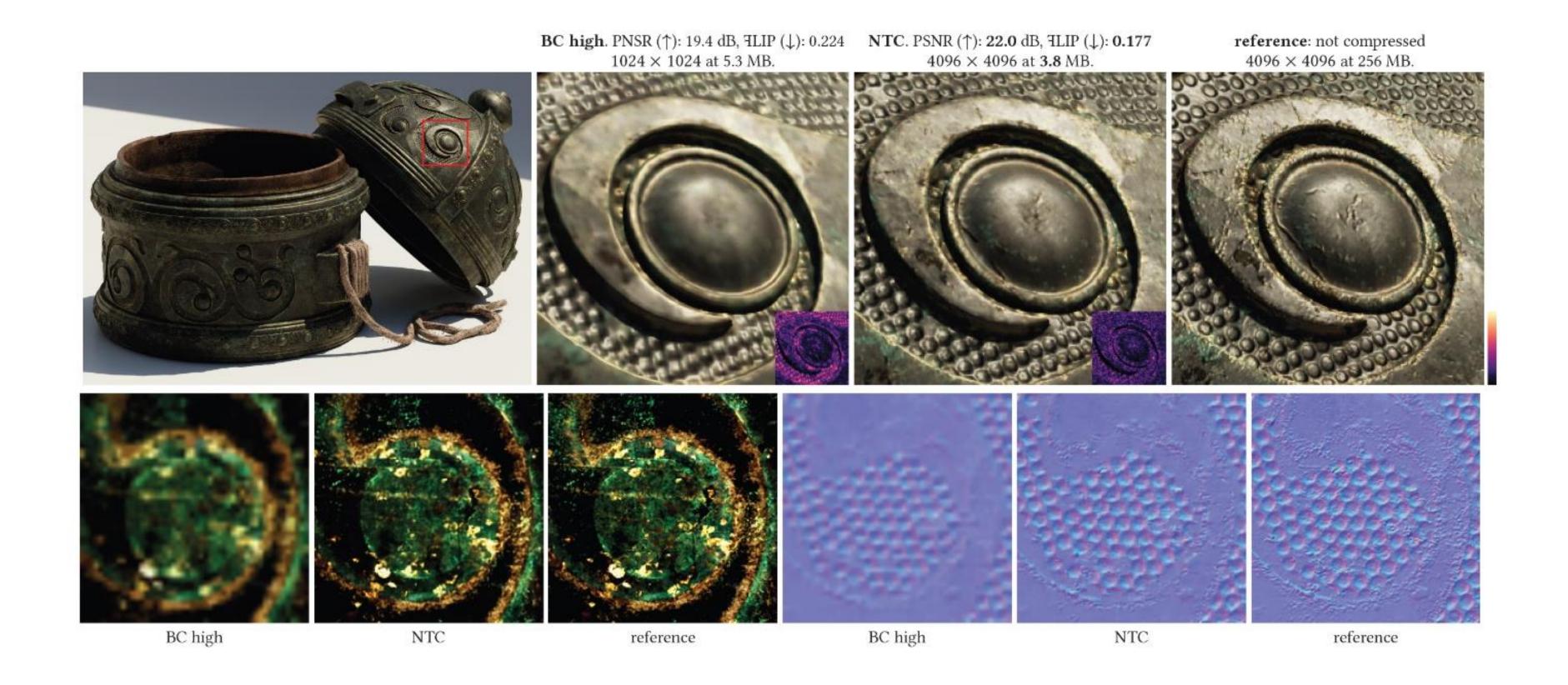
Project beginning: Stochastic neural texture filtering (performance)

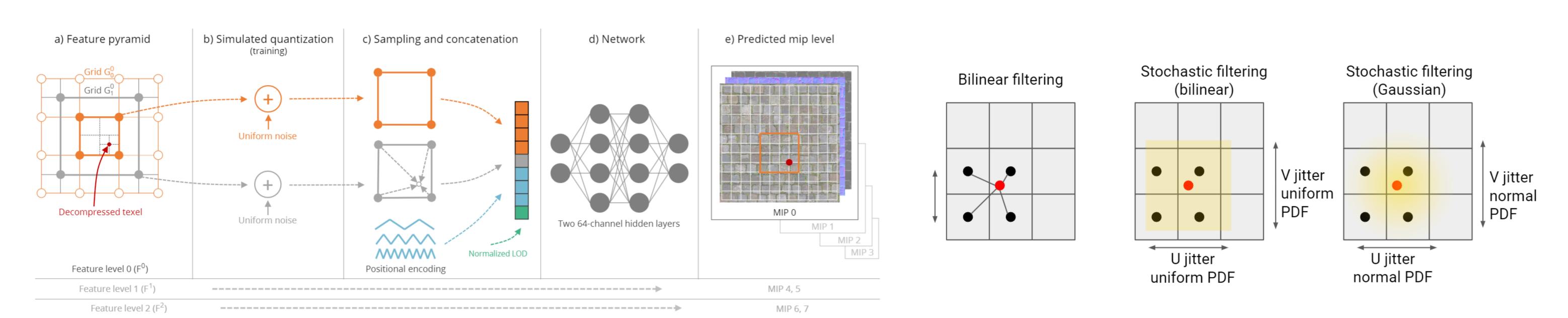




Random-Access Neural Compression of Material Textures, Vaidyanathan et al., Siggraph 2023

Project beginning: Stochastic neural texture filtering (performance)





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Related Work – Long History of Stochastic Filtering

- Percentage closer filtering
- Original UE software rasterizer: texture-space dithered nearest lookups
- Star Trek, 25th Anniversary: dithered bilinear filtering
- Negative LOD biasing (UE + everyone using TAA/DLSS...)
- OpenImageIO: stochastic LOD selection (via Max Liani)
- Dreamworks MoonRay: nearest sampling for minification, bilerp for magnification
- Interactive Path Tracing and Reconstruction of Sparse Volumes, Hofmann, Hasselgren, Clarberg, and Munkberg, i3d 2021: stochastic trilinear
- Random-Access Neural Compression of Material Textures, Vaidyanathan, Salvi, Wronski, Akenine-Möller, Ebelin, Lefohn, SIGGRAPH 2023: stochastic trilinear

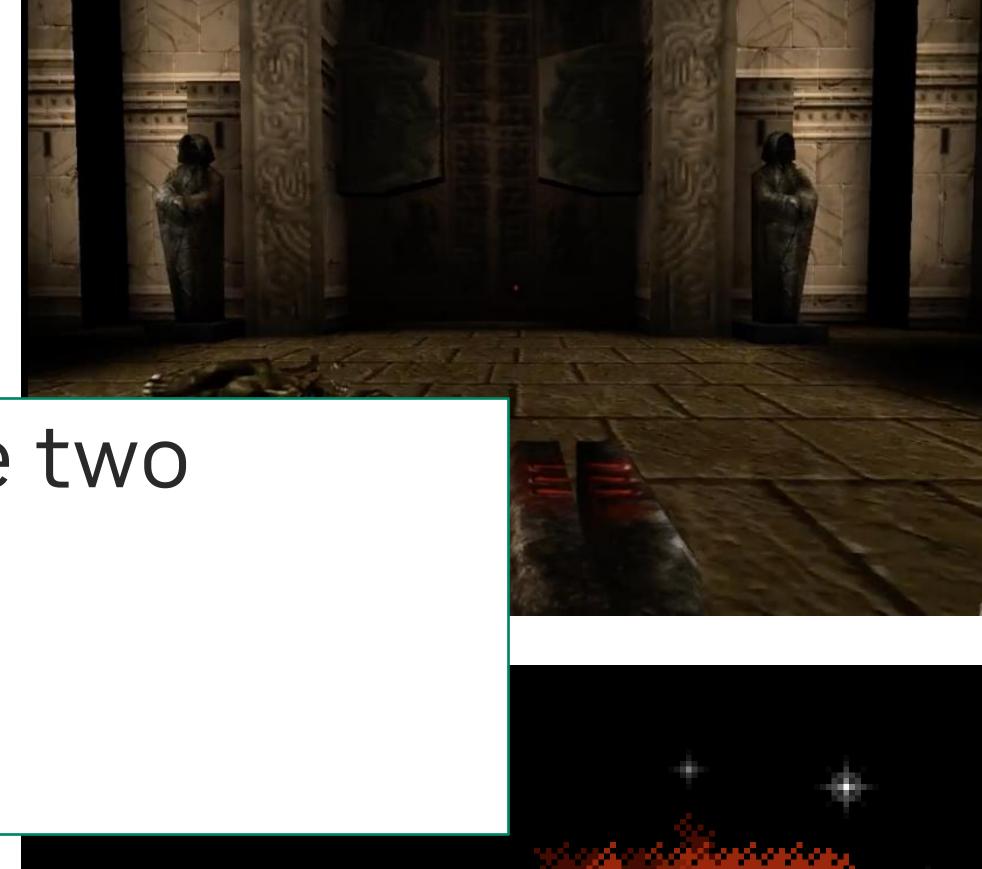




Related Work – Long History of Stochastic Filtering

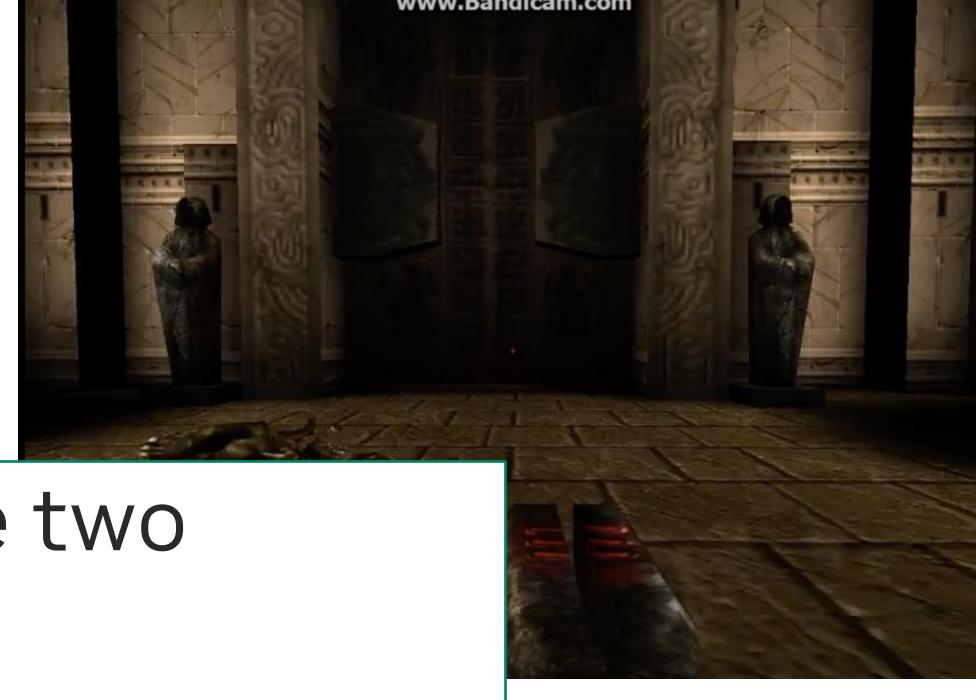
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 We will generalize those, formalize, and propose two
 Dreamw magnific
 families of techniques beyond simple filters
- Interacti Hofman trilinear

 Random-Access Neural Compression of Material Textures, Vaidyanathan, Salvi, Wronski, Akenine-Möller, Ebelin, Lefohn, SIGGRAPH 2023: stochastic trilinear



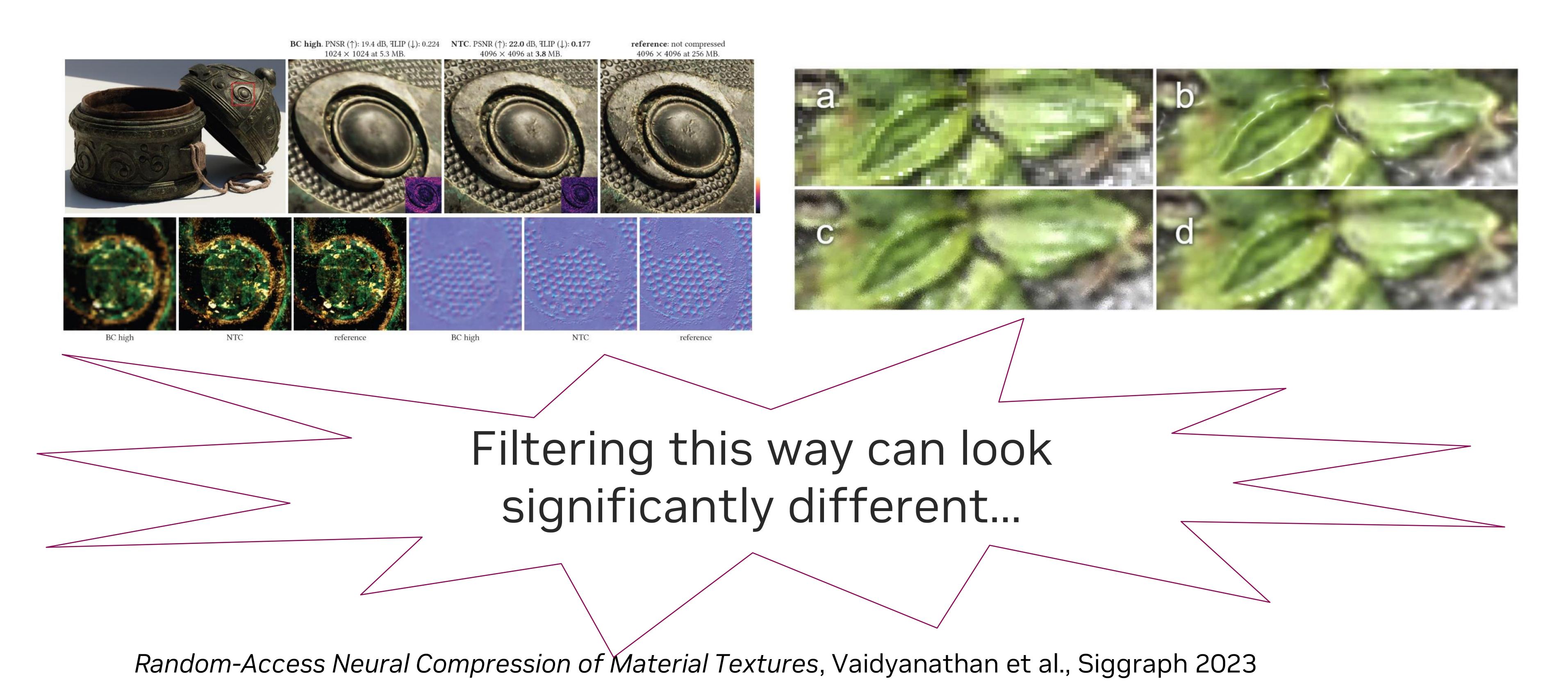
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- Random-Access Neural Compression of Material Textures, Vaidyanathan, Salvi, Wronski, Akenine-Möller, Ebelin, Lefohn, SIGGRAPH 2023: stochastic trilinear





Stochastic texture filtering: do we have a problem?







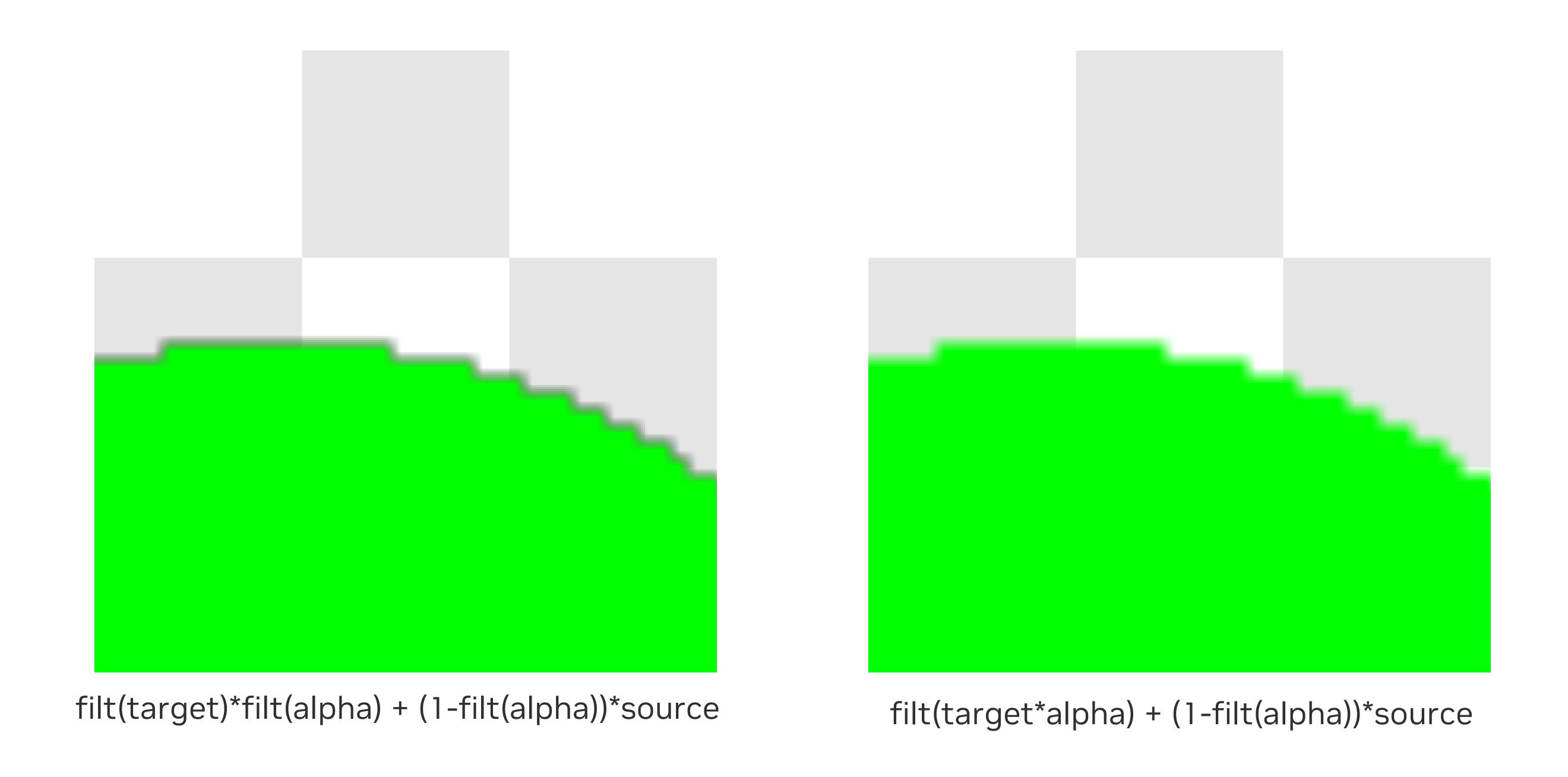
Precedent: Pre-multiplied alpha



filt(target)*filt(alpha) + (1-filt(alpha))*source

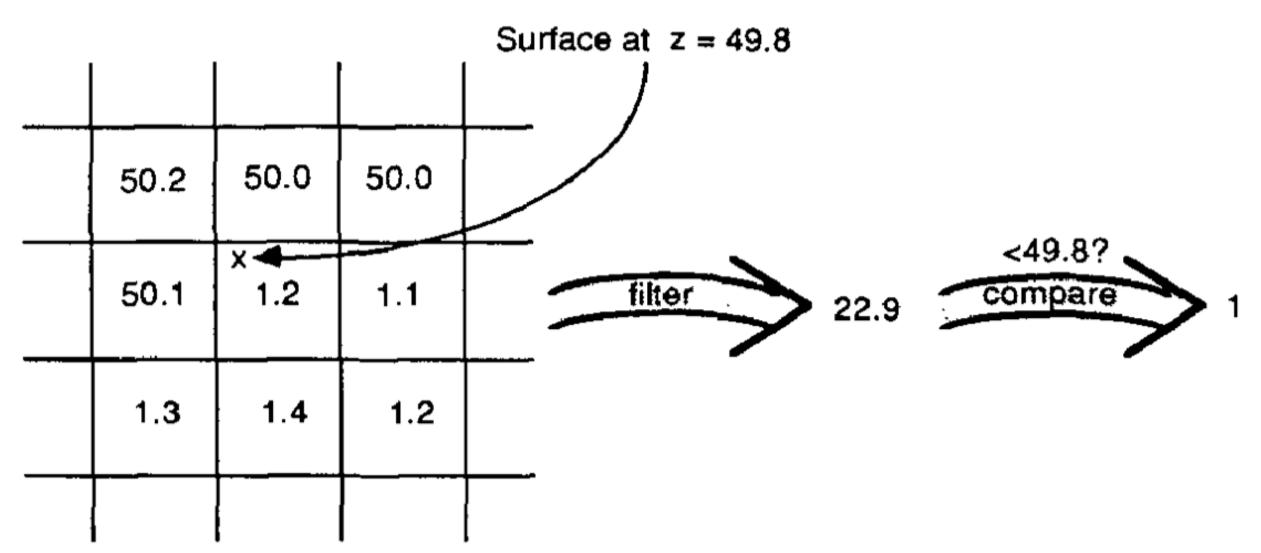
"Compositing digital images", Thomas Porter and Tom Duff., SIGGRAPH 1984. Figure credit: "premultiplied alpha – 2022", Inigo Quilez

Precedent: Pre-multiplied alpha



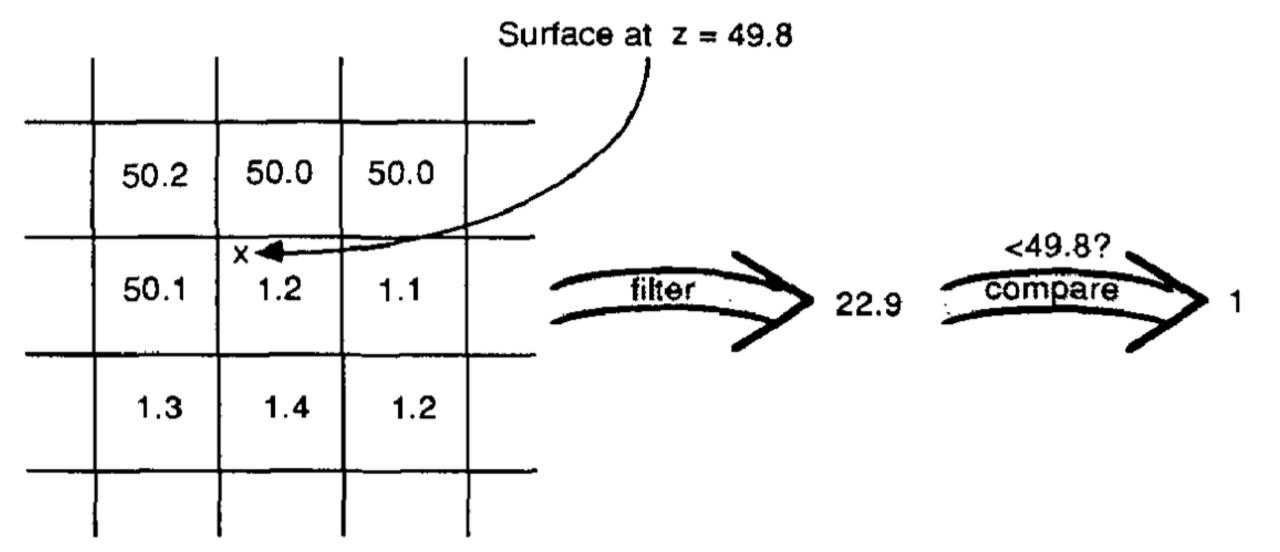
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Precedent: Percentage Closer Shadow Filtering



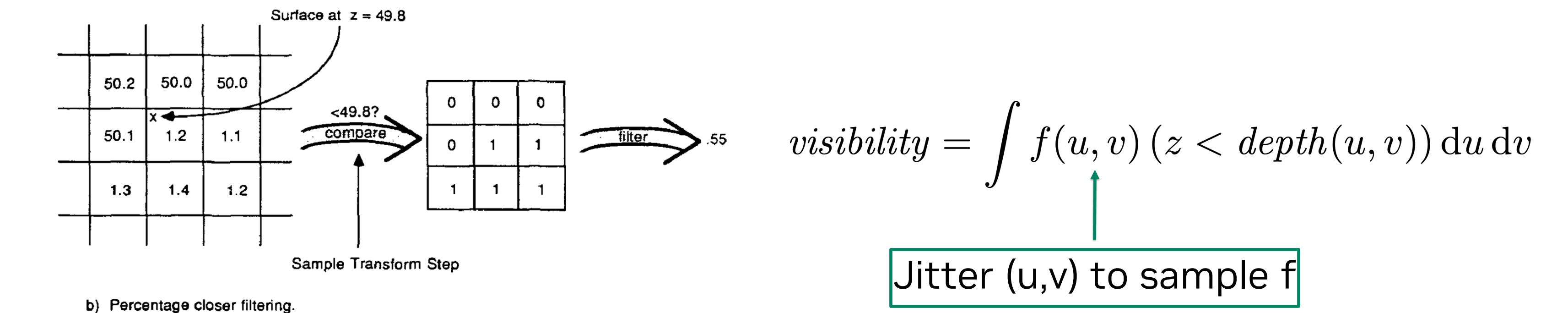
$$visibility = z < \int depth(u, v) du dv$$

Precedent: Percentage Closer Shadow Filtering



 $visibility = z < \int depth(u, v) du dv$

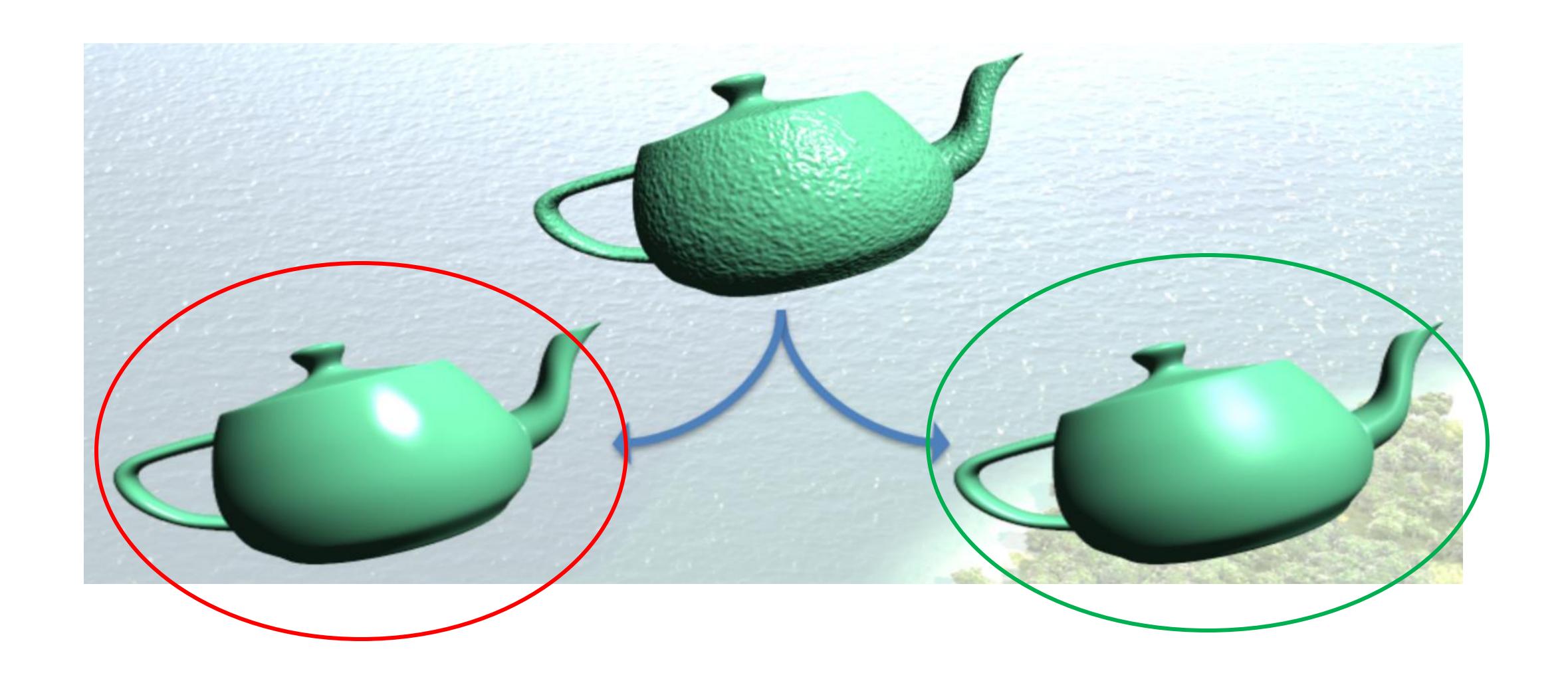
a) Ordinary texture map filtering. Does not work for depth maps.



Precedent: Percentage Closer Shadow Filtering

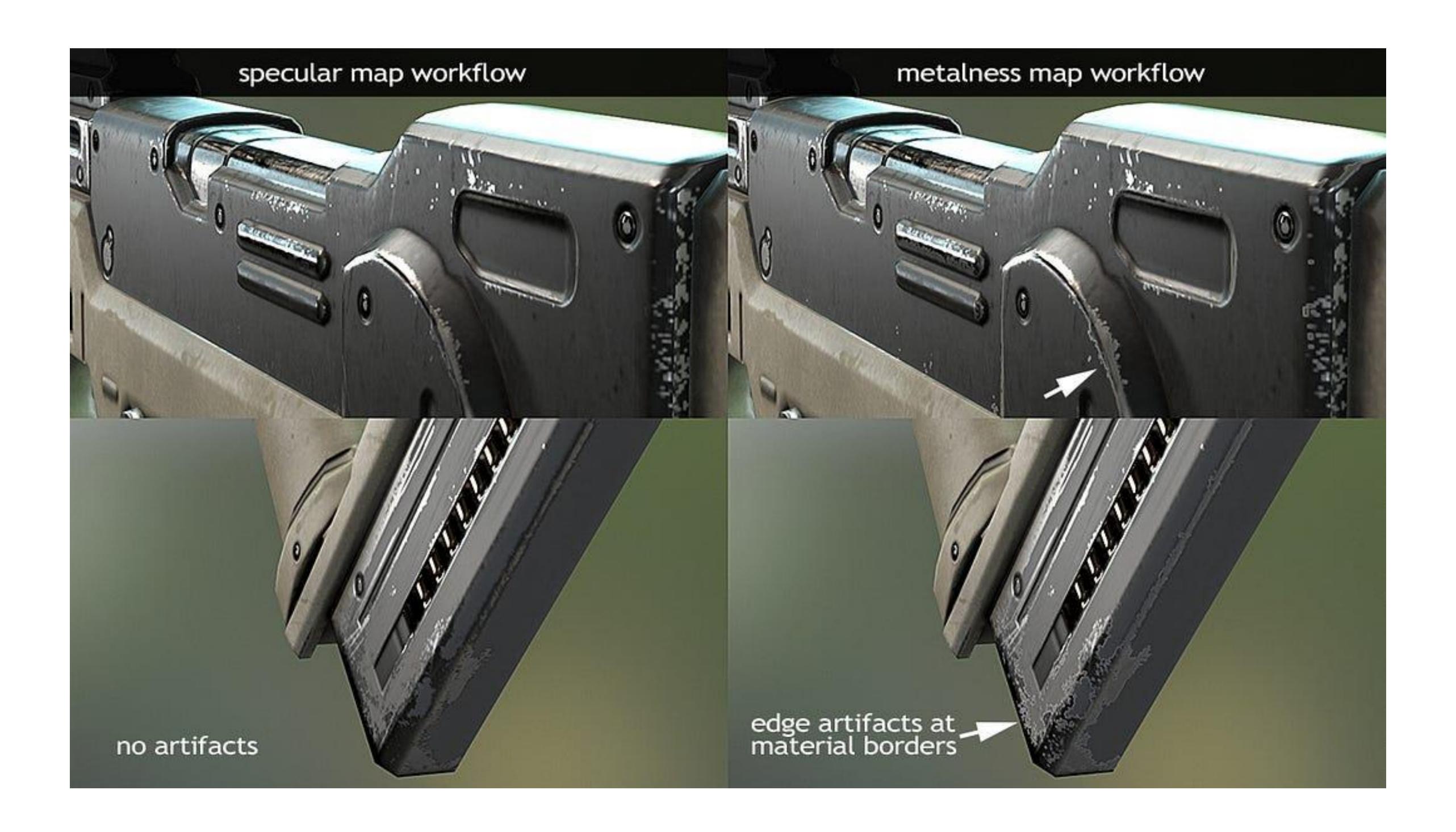
Finally, we hope to be able to generalize and formalize the sample transformation step in percentage closer filtering. We believe that this technique may have important implications to the use of texture maps for other purposes. For example, in bump mapping [Bli78], specular reflections could be computed before filtering, and the results could be filtered and sampled as ordinary textures. In this way, specular highlights from the microfacets of a bumpy surface would be maintained even as the surface were translated back into the far distance.

Precedent: Specular anti-aliasing (minification)



Mipmapping Normal Maps, Michael Toksvig, 2006 LEAN Mapping, Marc Olano and Dan Baker, I3D 2011 Figure credit: Spectacular Specular: LEAN and CLEAN Specular Highlights, Dan Baker, GDC 2011

Still a problem: Metalness vs specular PBR workflow



Specular reflectance = lerp(0.04, filt(color), filt(metalness))
Diffuse reflectance = lerp(filt(color), 0.0, 1-filt(metalness))

Figure credit: Metallic magic, Daniel Rose

- Texture filtering theory and practice were developed for interpolating just "color"
- ...in early work, not even gamma-corrected!

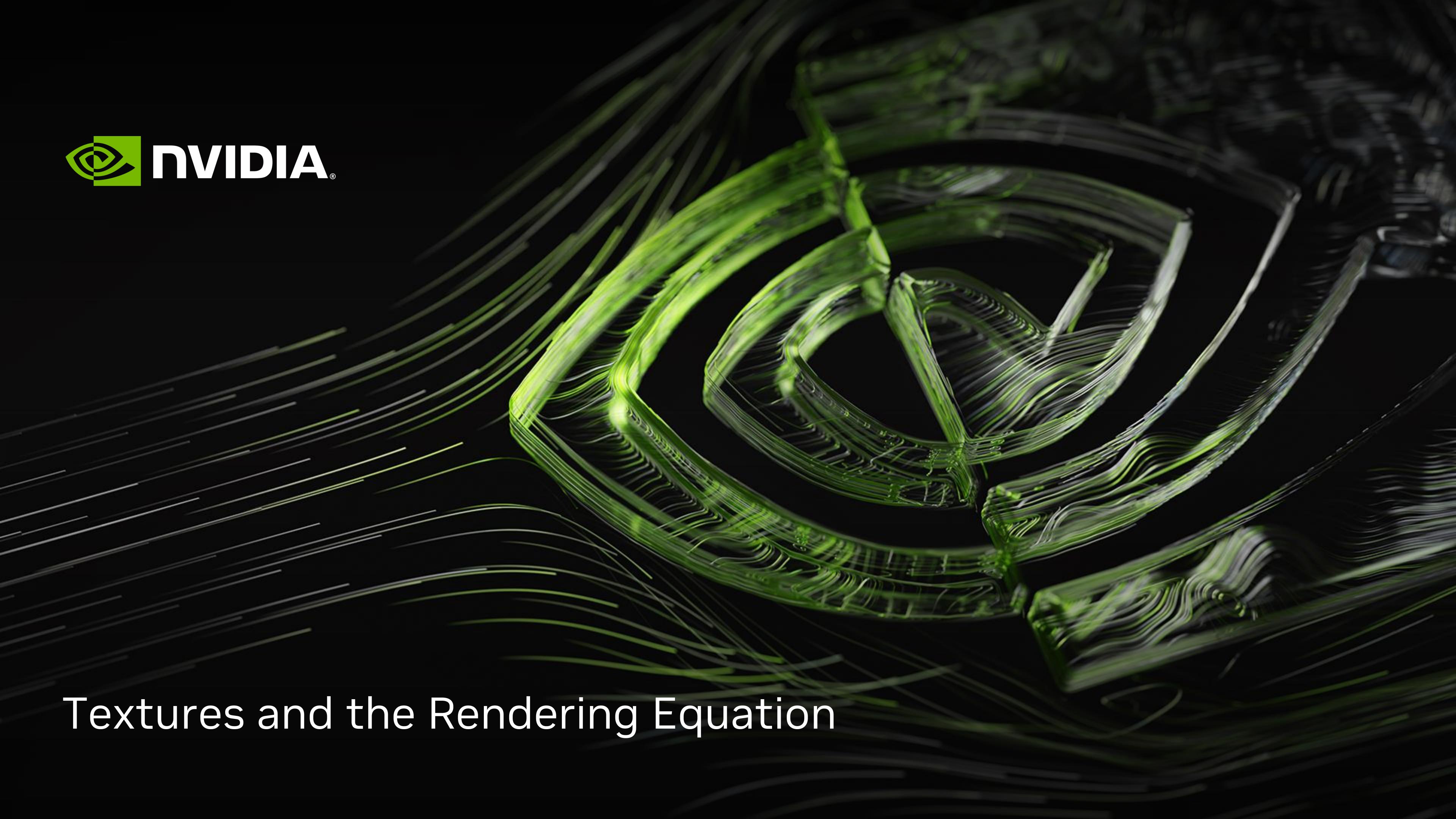
- Texture filtering theory and practice were developed for interpolating just "color"
- ...in early work, not even gamma-corrected!
- Filtering and affine functions commute perfectly this approach didn't introduce errors
- Non-linearity and filtering do not commute and swapping the order results in error

Assumption: textures are authored by artists with ~1-1 pixel-texel ratio

- Assumption: textures are authored by artists with ~1-1 pixel-texel ratio
- Minifying or magnifying textures before (non-linear) shading introduces error/bias
- Different techniques proposed to address specific types of errors

- Can we do better in general?
- Let's try to answer this question from 37y ago!

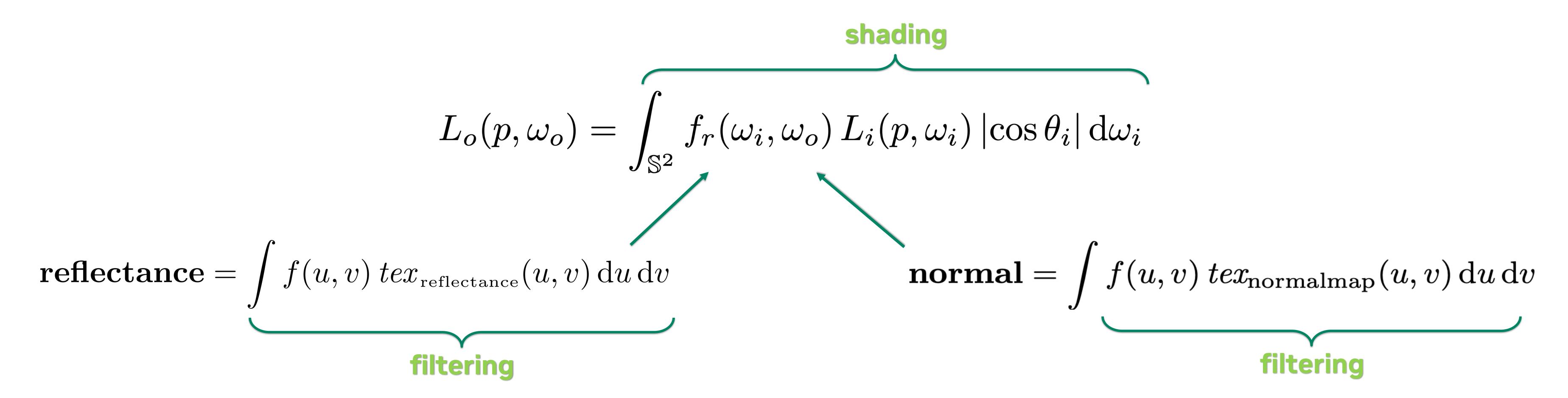
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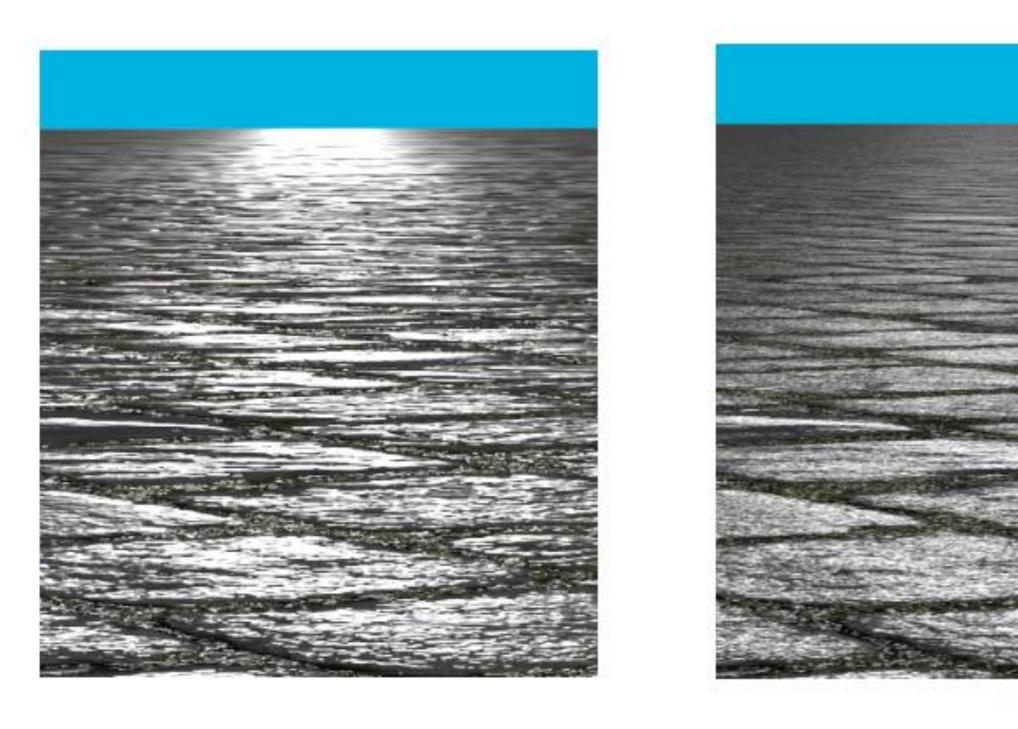


Filtering Before Shading (Standard Practice Today)

shading
$$L_o(p,\omega_o) = \int_{\mathbb{S}^2} f_r(\omega_i,\omega_o) \, L_i(p,\omega_i) \, |\!\cos heta_i| \, \mathrm{d}\omega_i$$

Filtering Before Shading (Standard Practice Today)





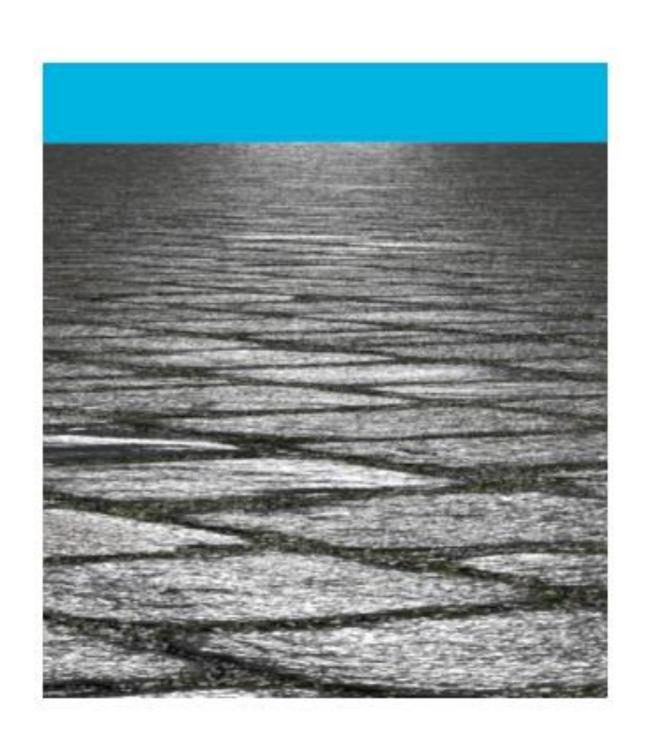
HW 16x Aniso

Reference

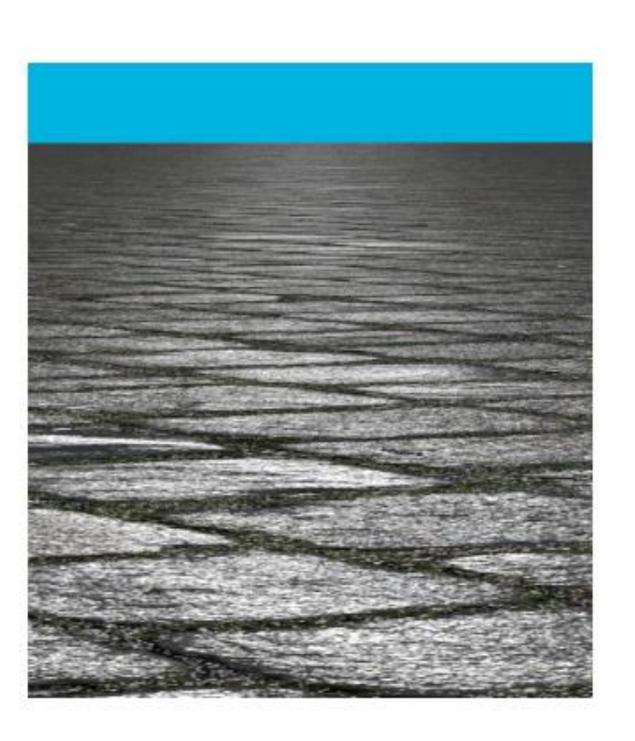


Filtering After Shading

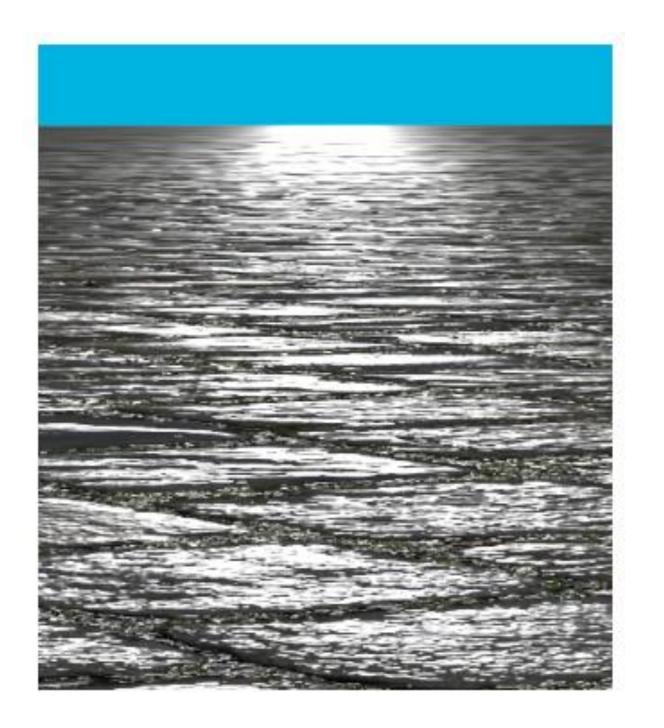
filtering shading
$$L_o(p,\omega_o) = \int f(u,v) \left(\int_{\mathbb{S}^2} f_r(\omega_i,\omega_o) \, L_i(p,\omega_i) \, |\!\cos\theta_i| \, \mathrm{d}\omega_i \right) \mathrm{d}u \, \mathrm{d}v$$



Filter after shading (real-time implementation)

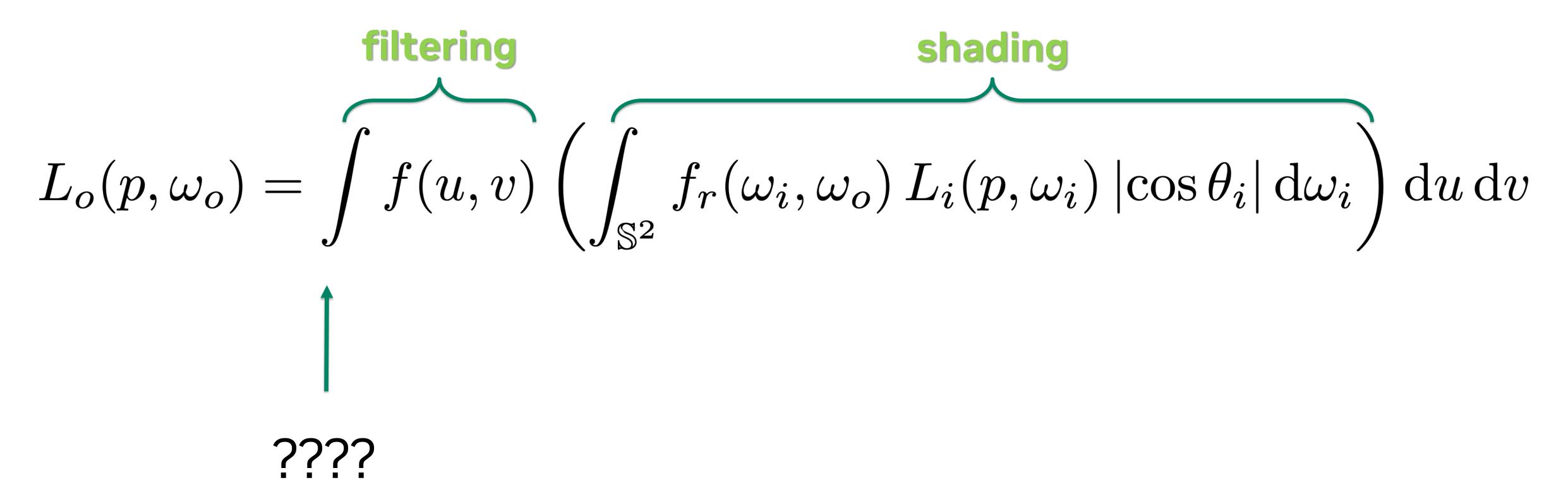


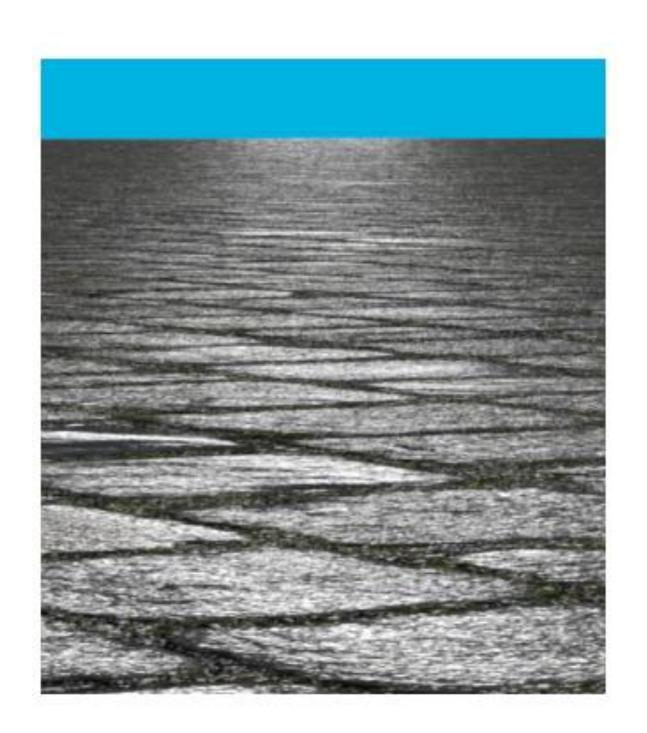
Reference



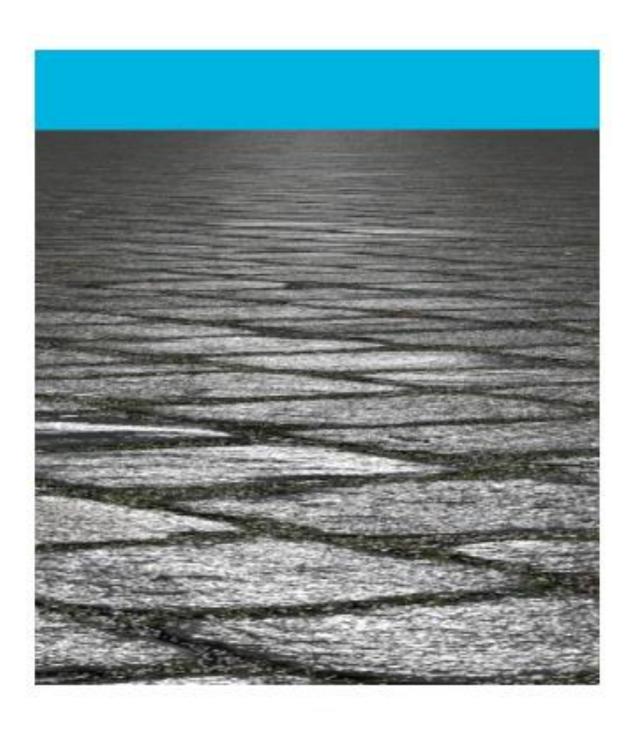
Filter before shading

Filtering After Shading

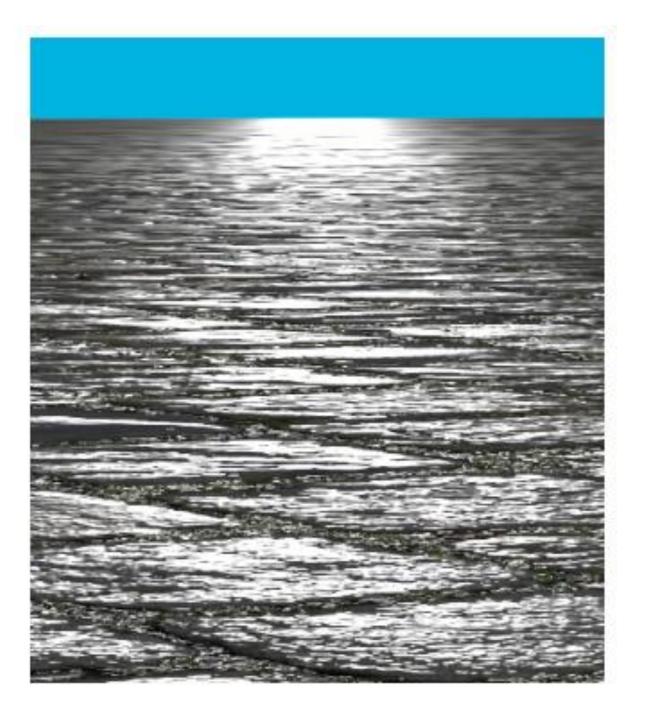




Filter after shading (real-time implementation)



Reference



Filter before shading

Filtering After Shading

filtering shading
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- Use Monte Carlo!
- Sample $(u',v') \sim f(u,v)$

Filtering After Shading

filtering shading
$$L_o(p,\omega_o) = \int f(u,v) \left(\int_{\mathbb{S}^2} f_r(\omega_i,\omega_o) \, L_i(p,\omega_i) \, |\!\cos\theta_i| \, \mathrm{d}\omega_i \right) \mathrm{d}u \, \mathrm{d}v$$

- Use Monte Carlo!
- Sample $(u', v') \sim f(u, v)$

• Estimator:
$$L_o(p,\omega_o) \approx \frac{f(u,v)}{p(u,v)} \left(\int_{\mathbb{S}^2} f_r(\omega_i,\omega_o) \, L_i(p,\omega_i) \, |\cos \theta_i| \, \mathrm{d}\omega_i \right) \mathrm{d}u \, \mathrm{d}v$$

$$= \int_{\mathbb{S}^2} f_r(\omega_i,\omega_o) \, L_i(p,\omega_i) \, |\cos \theta_i| \, \mathrm{d}\omega_i$$

$$\mathbf{reflectance} = tex_{\text{reflectance}}(u',v') \qquad \mathbf{normal} = tex_{\mathbf{normalmap}}(u',v')$$

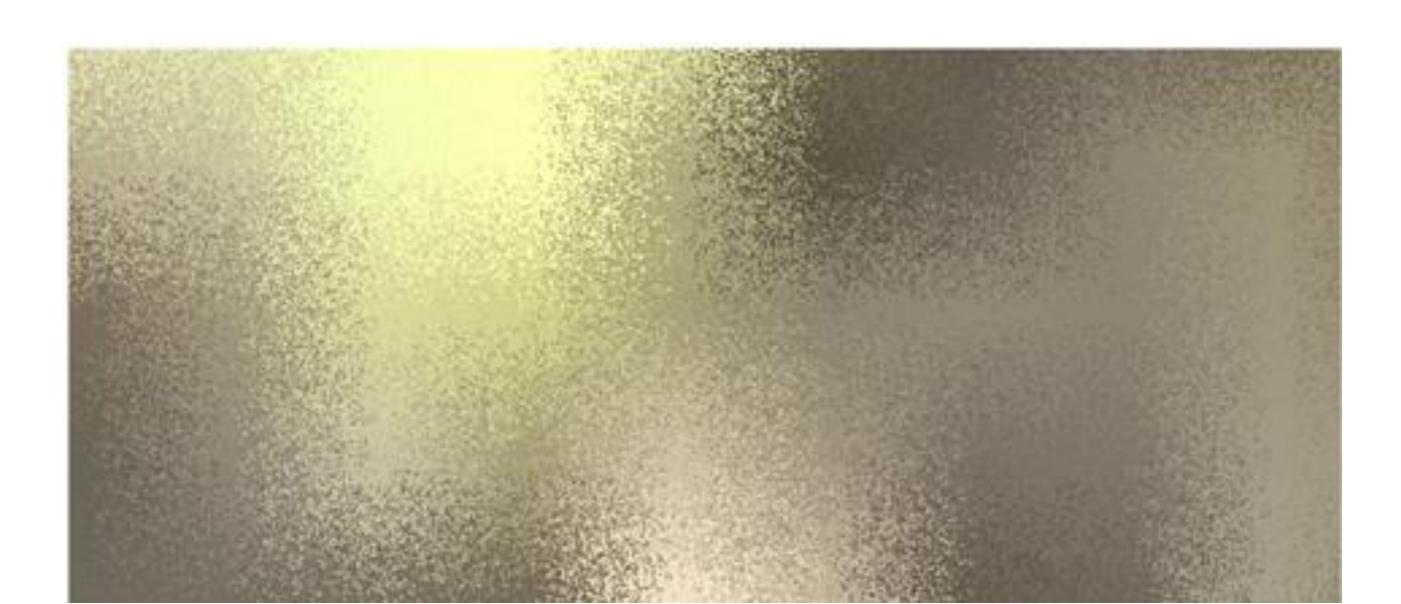
Unfiltered single texel lookups!



Even Single Sample! Real Time Rendering – Noise

White noise







Even Single Sample! Real Time Rendering – Noise

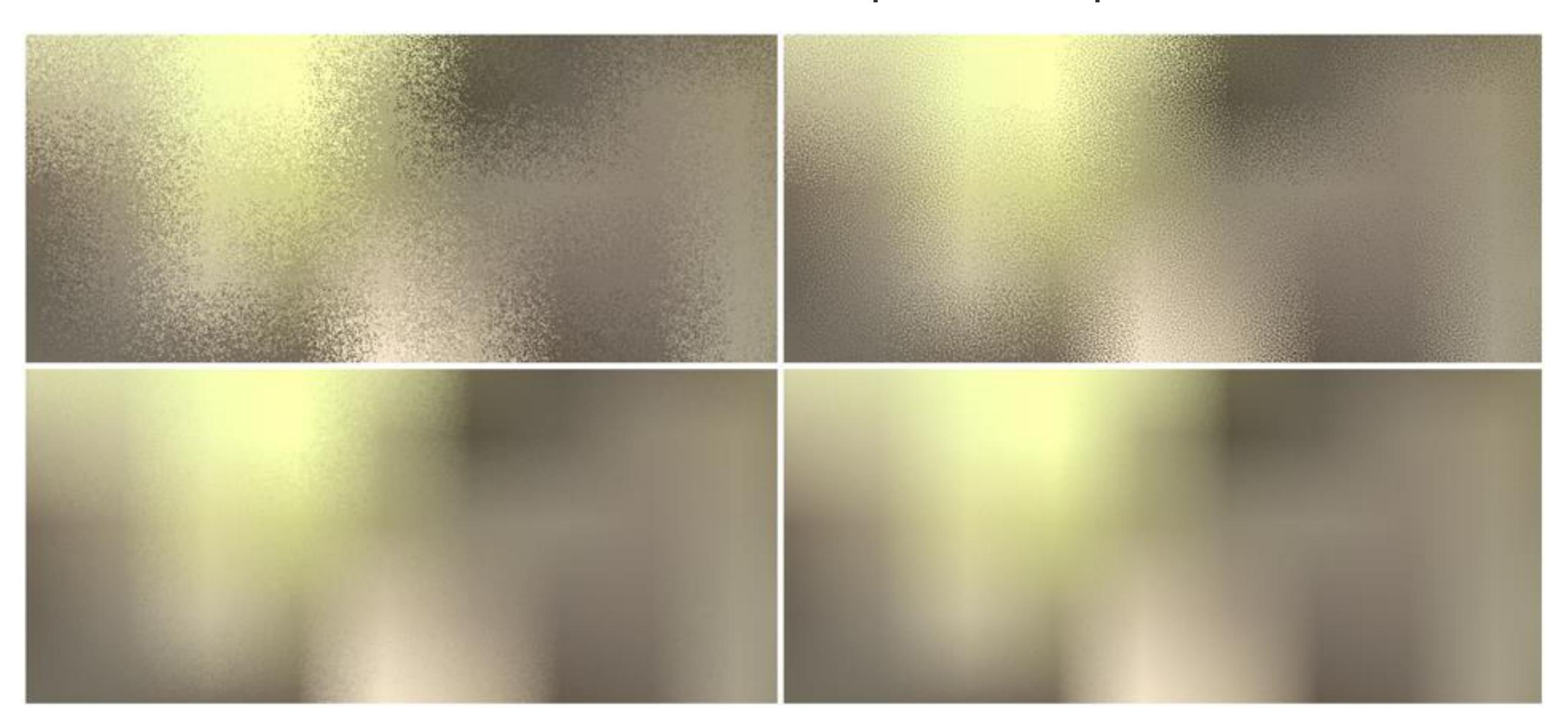
- DLSS as the robust temporal integrator
- Spatiotemporal Blue Noise reduces the noise appearance
- Makes DLSS job easier, together -> no visible noise in most cases

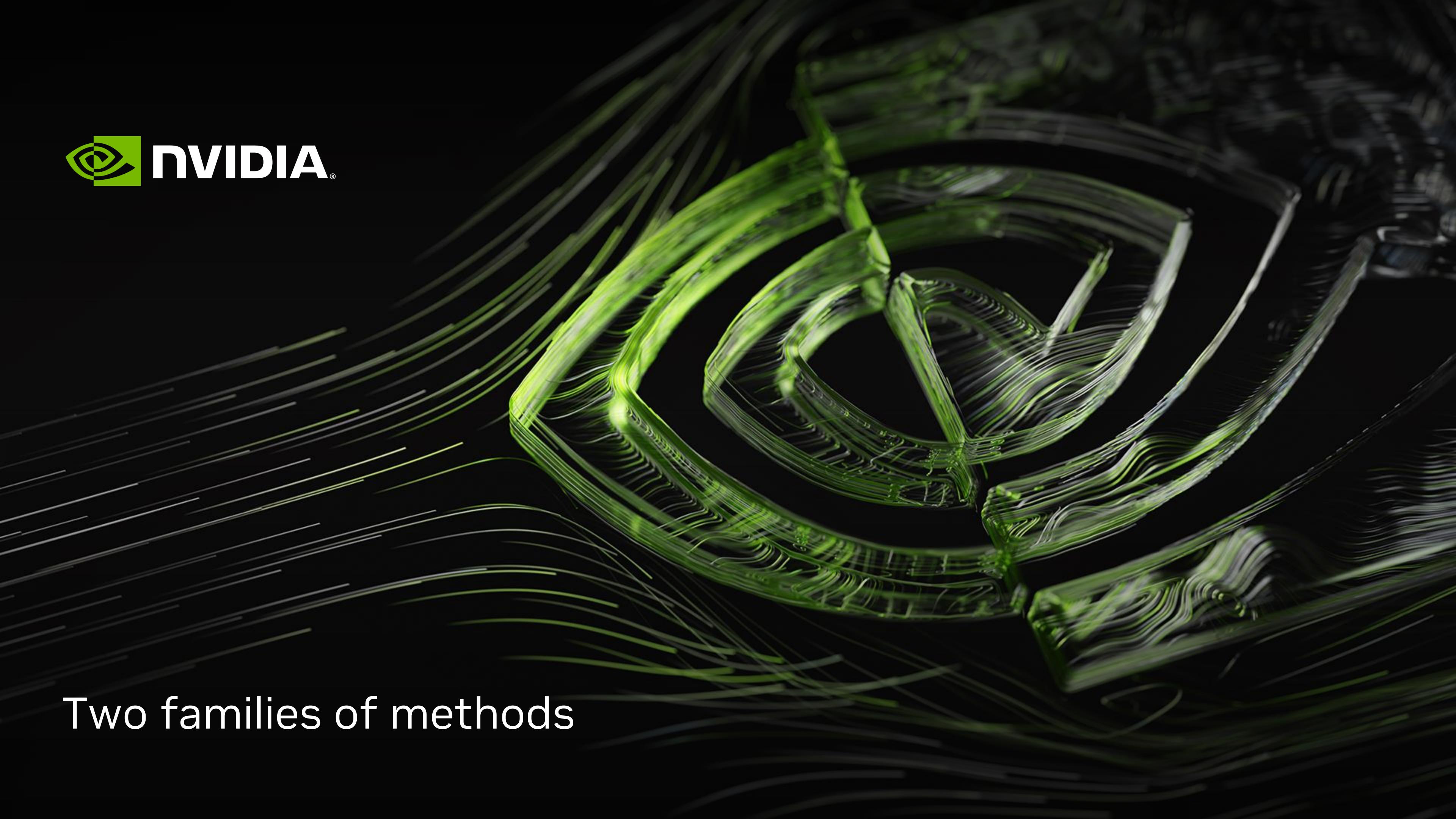
White noise

(Spatiotemporal) Blue Noise

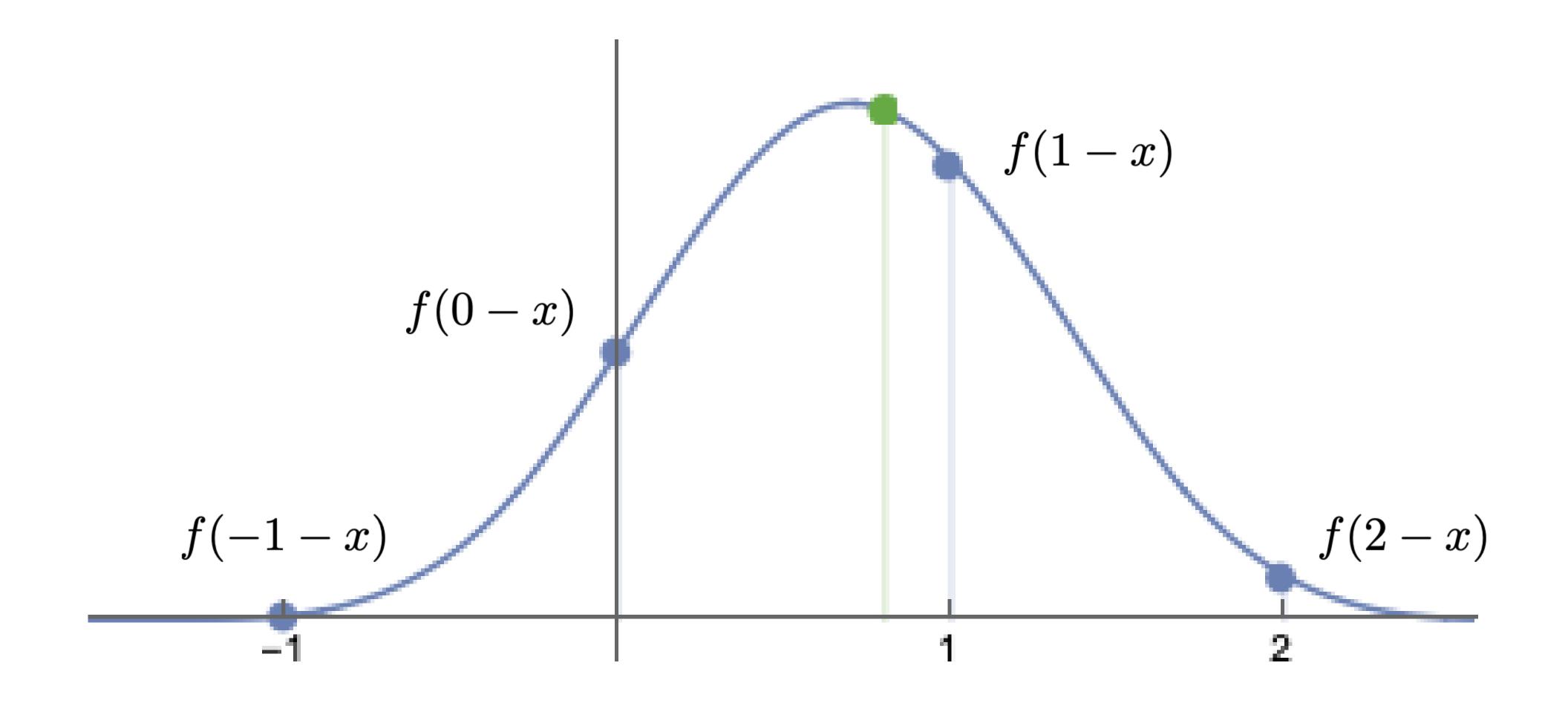
Single frame

DLSS





Sampling Texture Filters - Discrete, 1D



$$lookup(x) = \int f(u-x) t(u) du = \sum_{u=-1}^{2} \underbrace{f(u-x)}_{u=-1} t(u)$$

Chose a sample with probability ~f

Filter Reservoir Sampling

- Importance sampling: Sample a texel with probability p~f
- Sample an array of weights or online through weighted reservoir sampling
- Details in the paper

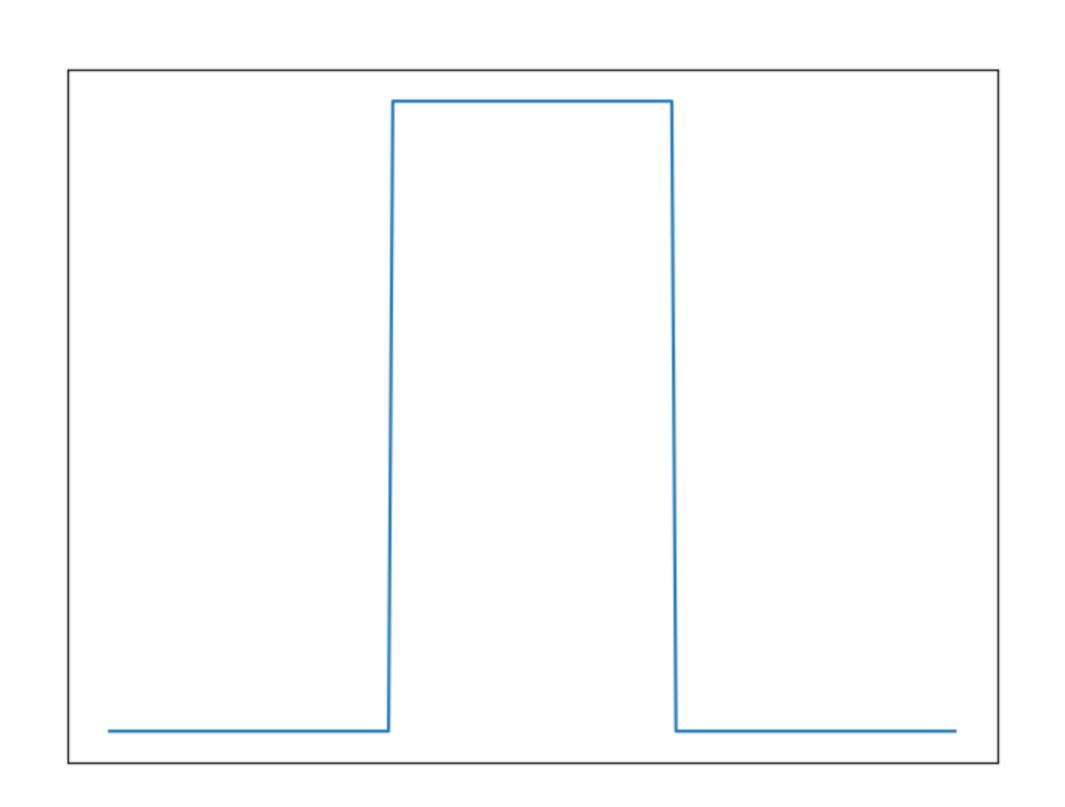
Sampling Texture Filters Disadvantages of Filter Reservoir Sampling

- Discrete filter sampling with large filters, can be costly
- Evaluate filter function K^M or K*M times
- Does not support infinite filters (Gaussian, sinc)

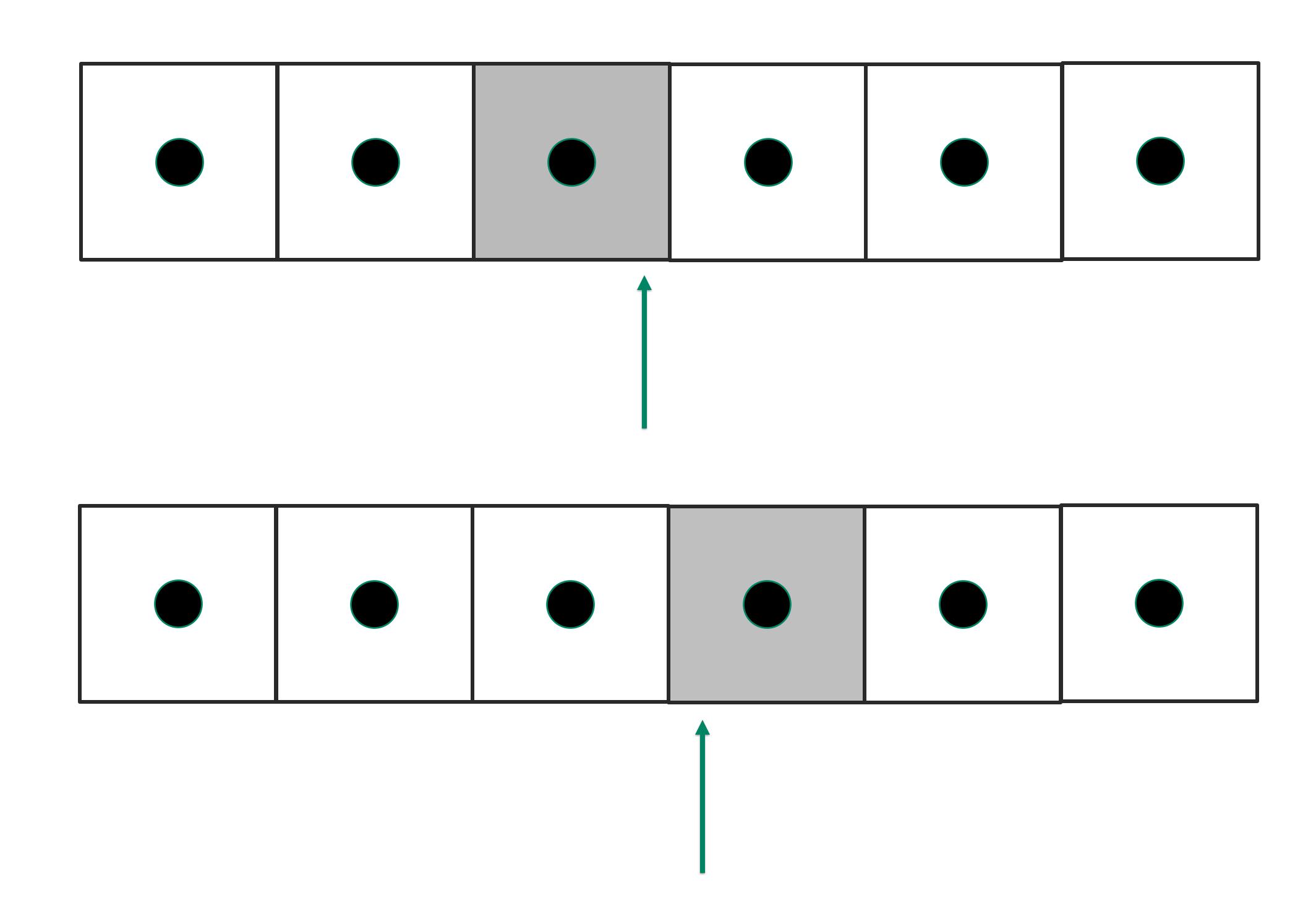
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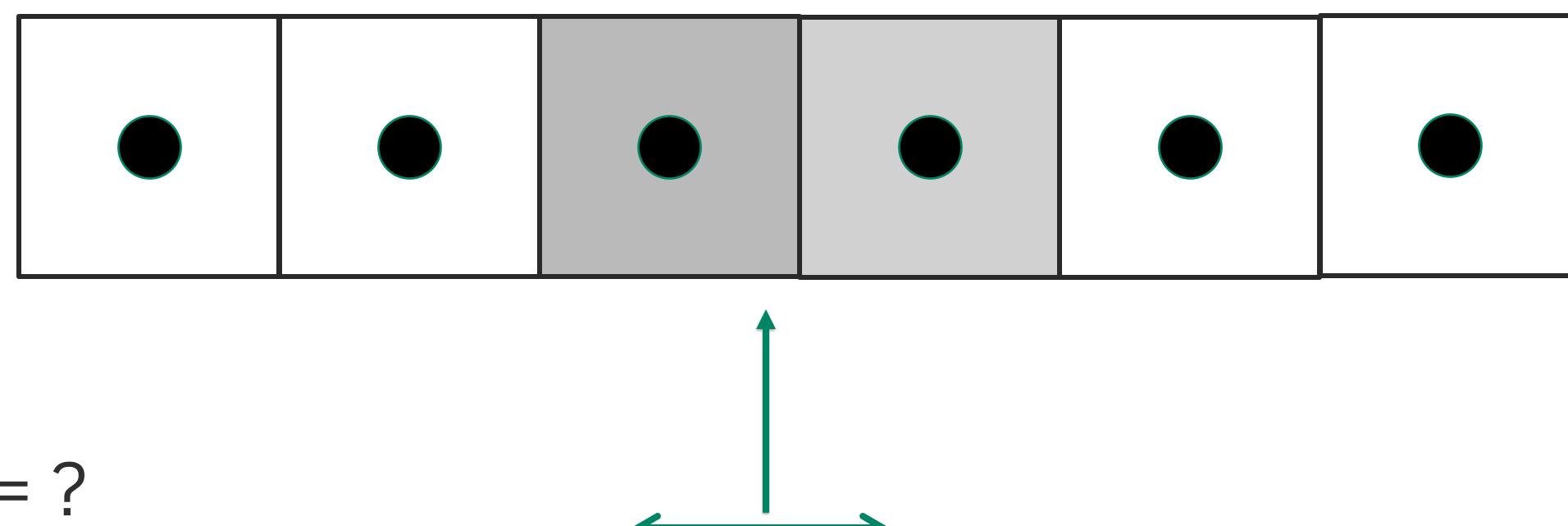
- Discrete filter sampling with large filters, can be costly
- Evaluate filter function K^M or K*M times
- Does not support infinite filters (Gaussian, sinc)
- There's a different way!
- Let's analyze and understand the "UV jitter + nearest neighbor" prior work.

Magnification What happens when you take a nearest-neighbor sample?

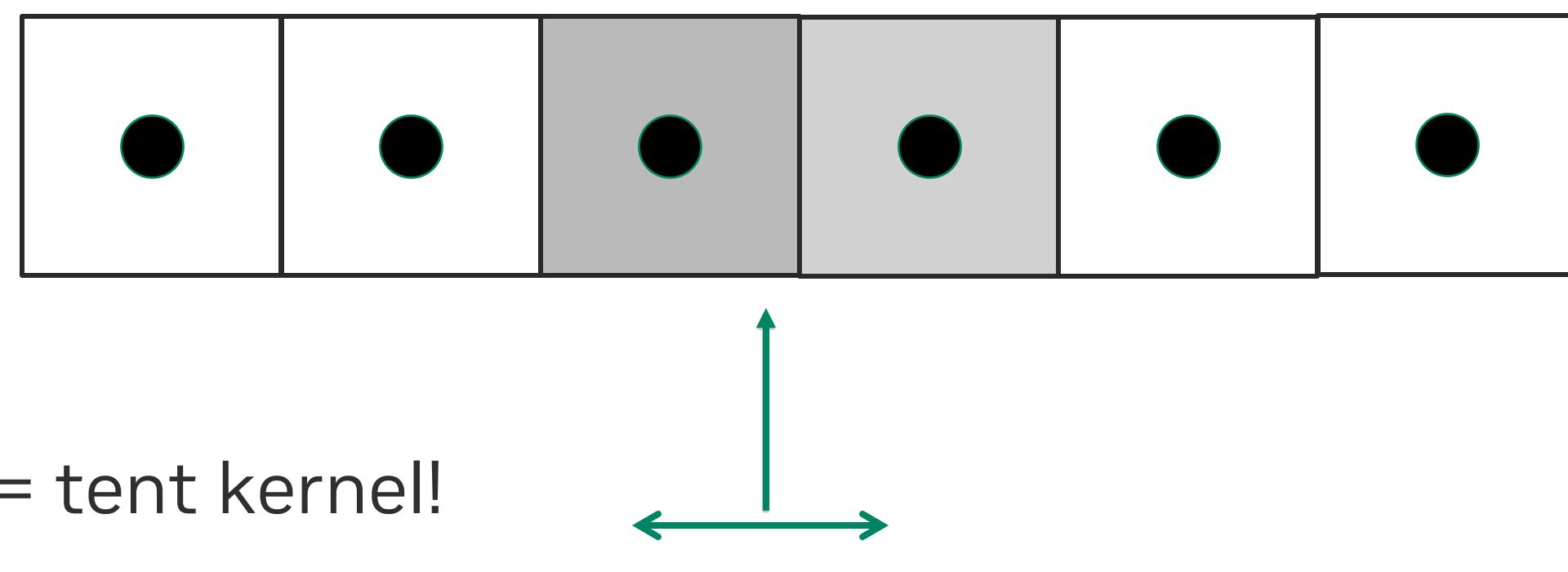


Nearest neighbor = box filter

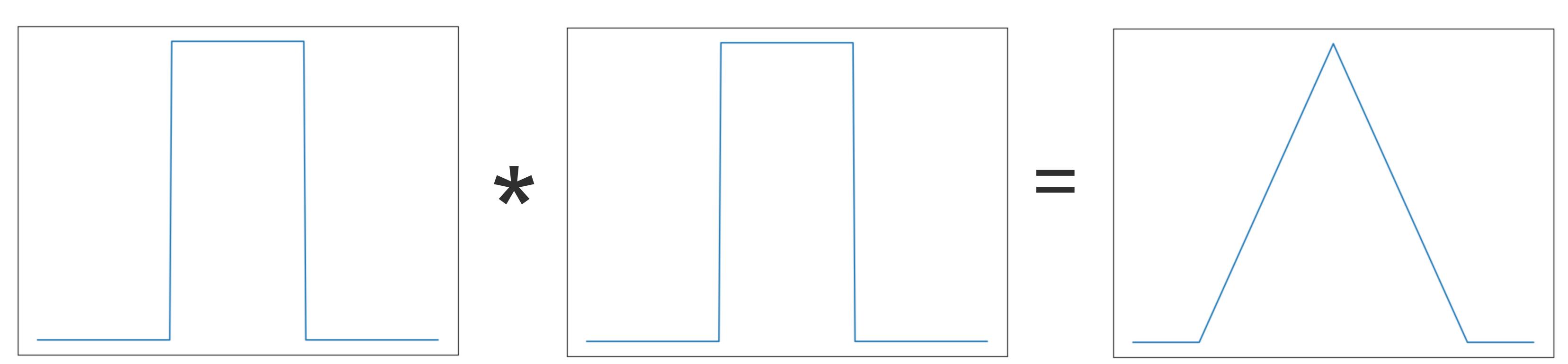




Uniform UV jitter + nearest neighbor = ?

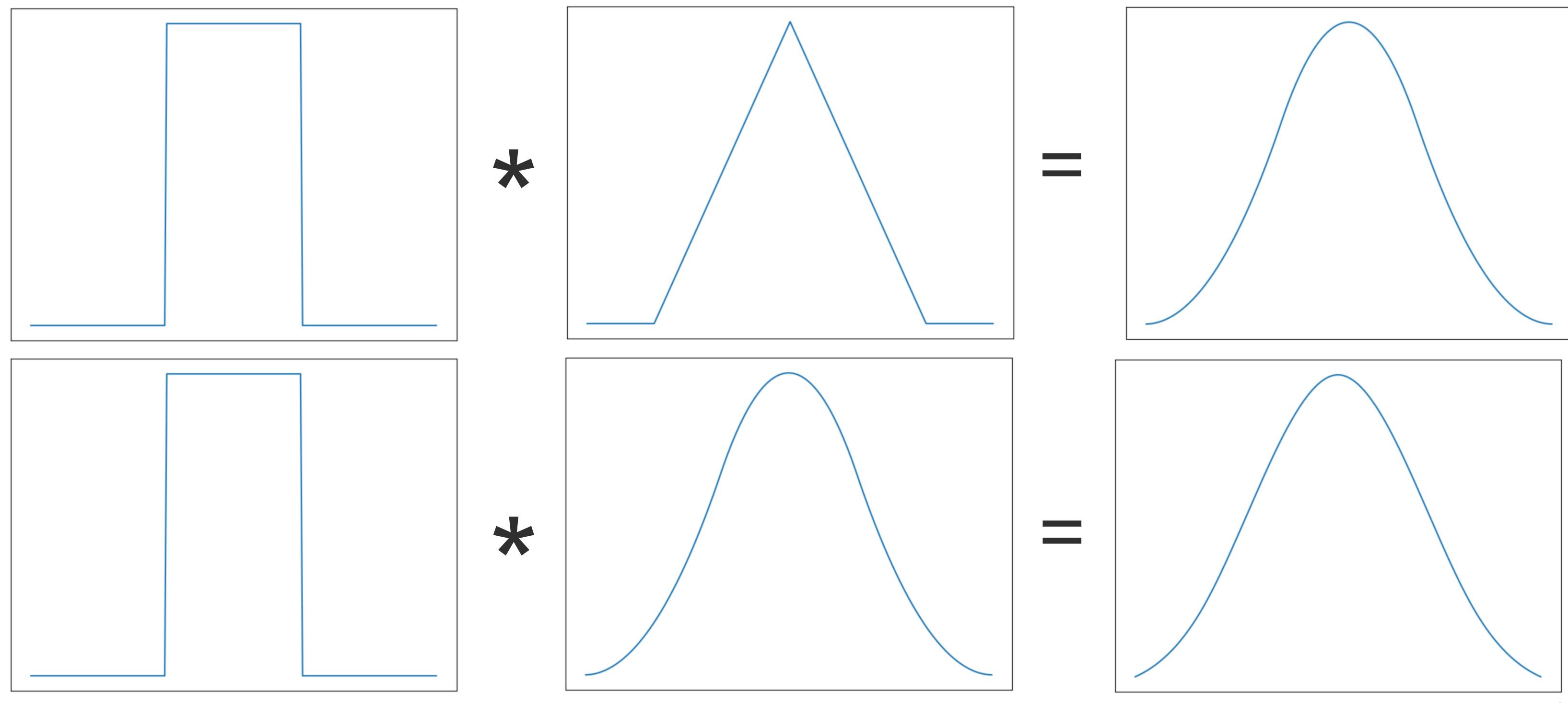


Uniform UV jitter + nearest neighbor = tent kernel! The same as **linear interpolation**



Jitter PDF * Box Kernel Convolution

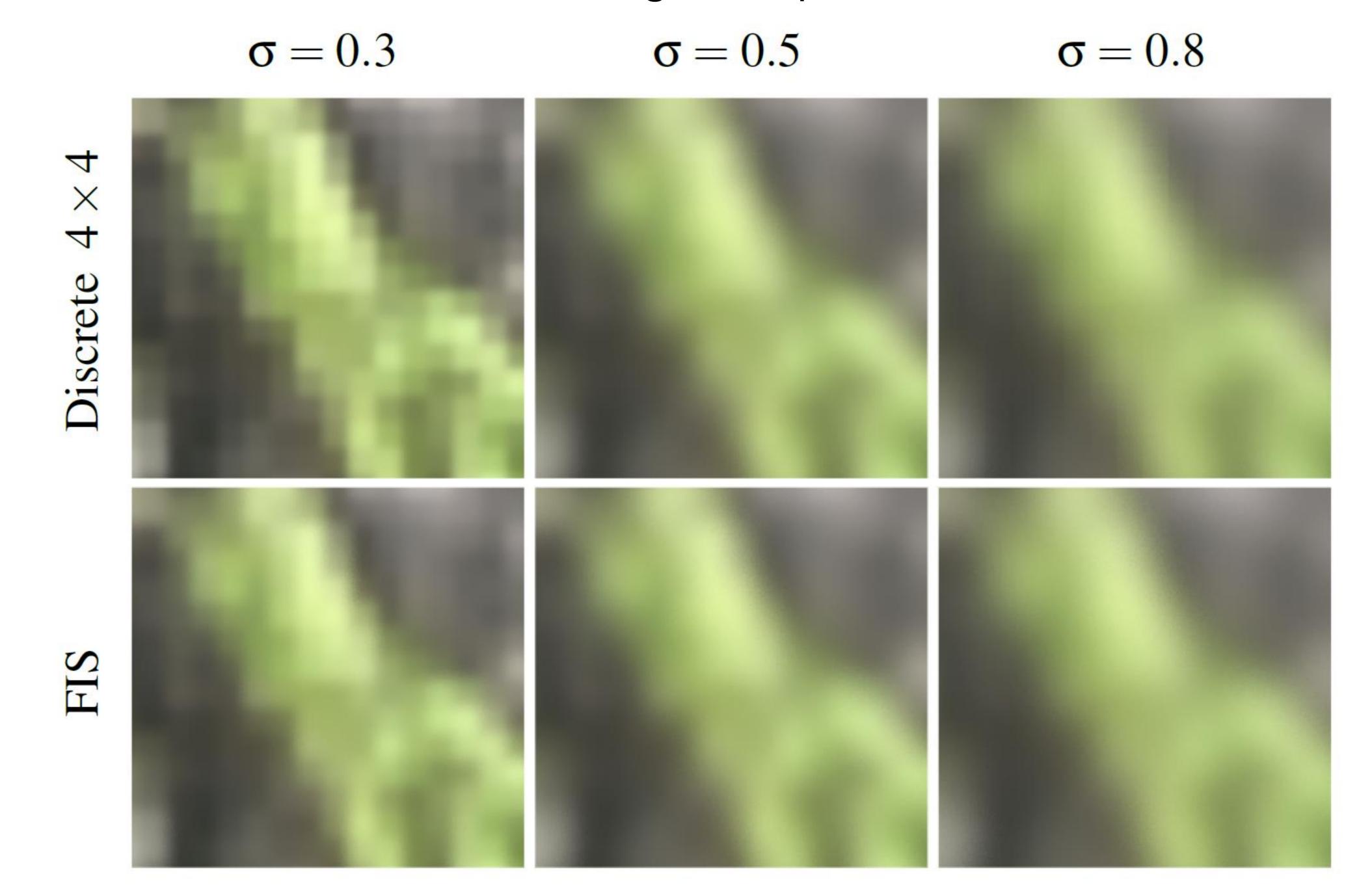
Linear/tent UV jitter + nearest neighbor box = quadratic B-Spline Quadratic UV jitter + nearest neighbor box = cubic B-Spline



- For B-Spline filters, this additional box is desirable!
- Can sample other, including infinite spatial support filters
- Jitter UVs according to PDF deconvolved with a box



- For B-Spline filters, this additional box is desirable!
- Can sample other, including infinite spatial support filters
- Jitter UVs according to PDF deconvolved with a box
- For many other filters -> can still be advantageous (prevent Gaussian under-sampling)



Stochastic Filtering families compared

- Main difference: discrete vs continuous domain
- In some cases, FRS is the only option (arbitrary discrete kernels, positivization)
- Otherwise, we recommend FIS simpler implementation, see provided source code

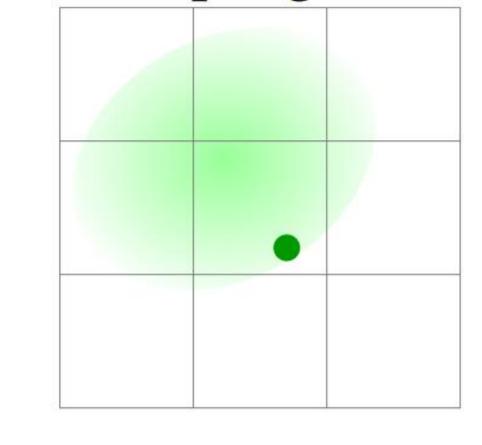
Filter Reservoir Sampling

0.0	0.1	0.1
0.1	0.2	0.2
0.0	0.1	0.1

10% 10% 20% 10% 10%

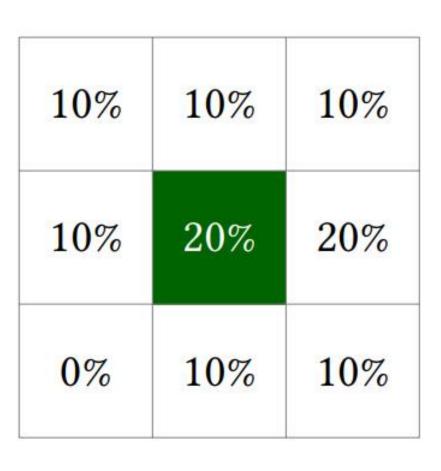


PDF.



Filter Importance Sampling

(a) Find texture texels weights.



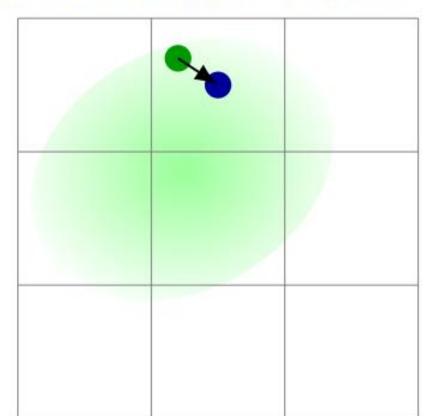
(b) Convert weights to probabilities.



(c) Align UV offset with texel center and sample the texel.

(a) Select continuous filter

(b) Sample the continuous distribution to find UV offset.

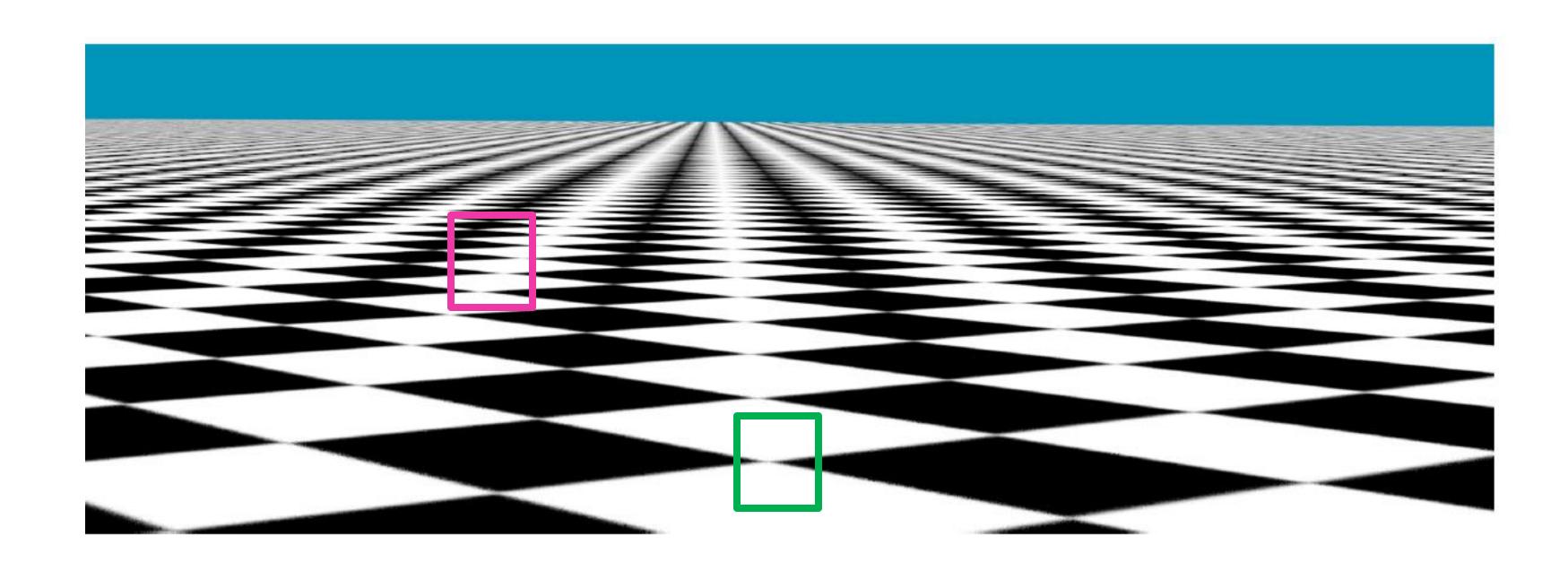


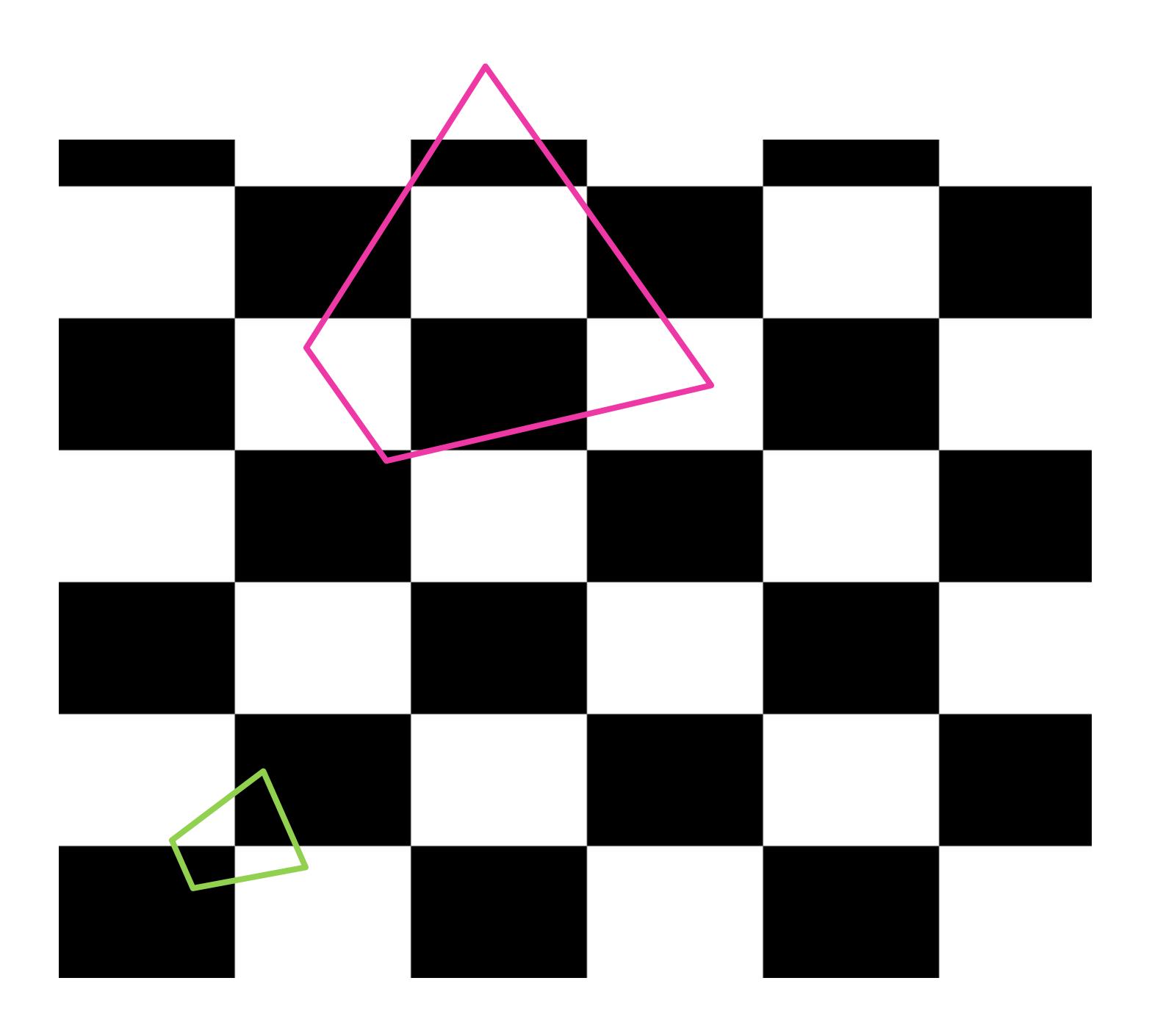
(c) Randomly select one texel.

(d) Repeat in the next frame, selecting a different texel.

(d) Repeat steps b and c in the next frame.

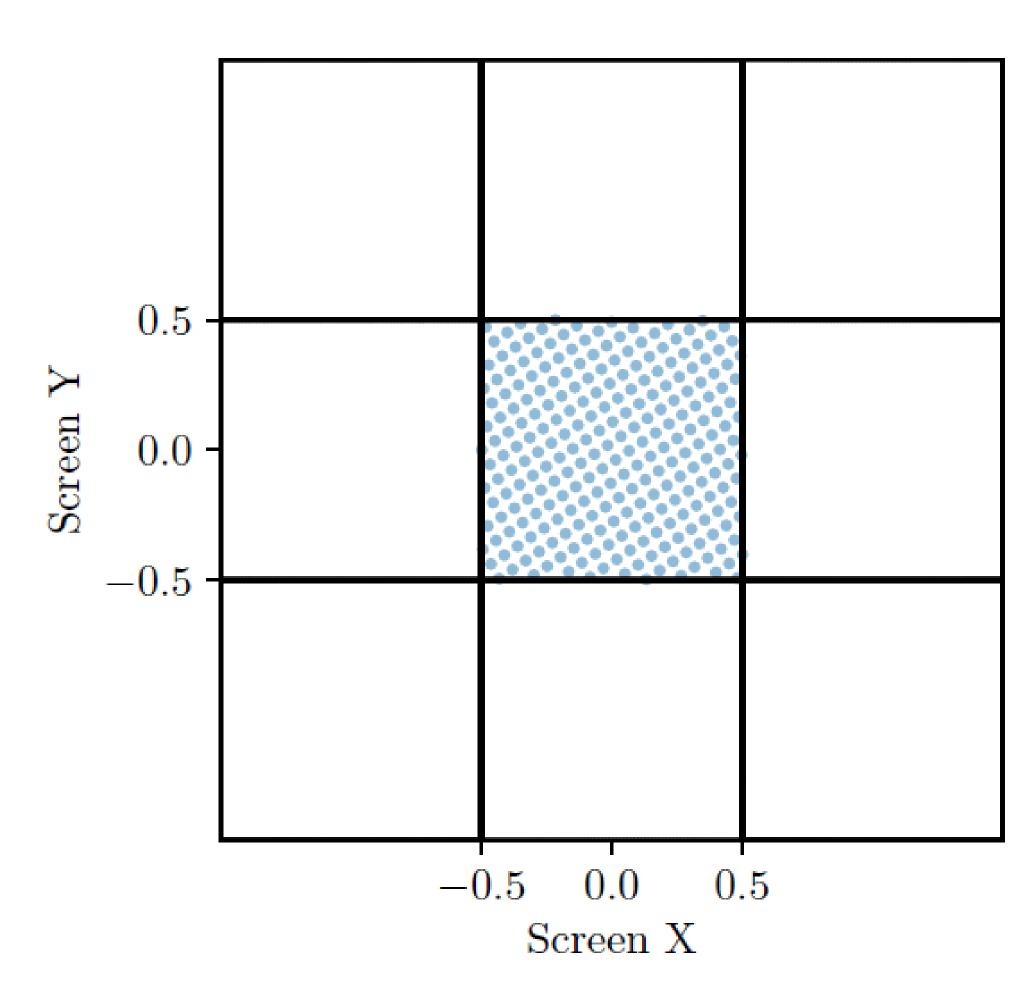
- Anisotropic filtering or elliptically weighted average
- Many pixels, non-uniform mapping for jittering
- There's a simpler, already-used method!





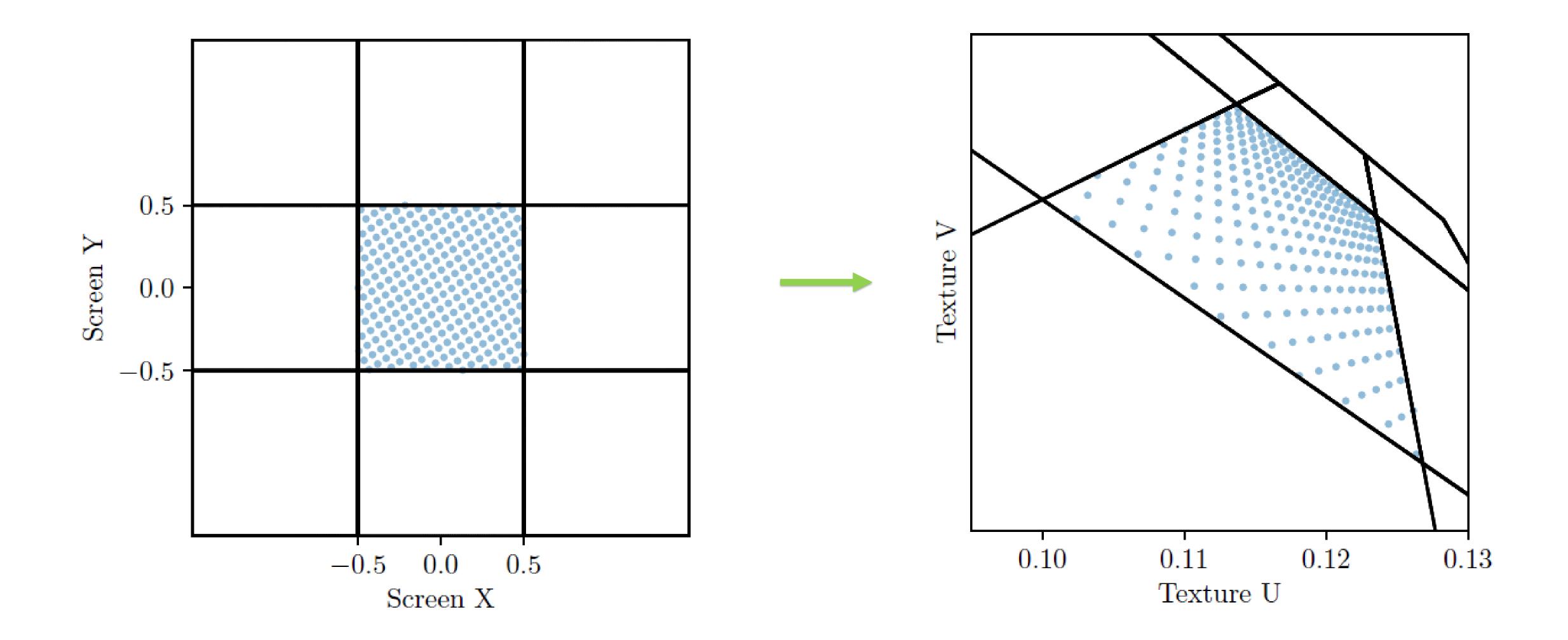


- Common practice jitter the projection matrix for anti-aliasing reconstruction filter
- Used offline (e.g., MoonRay) and real-time (TAA, DLSS)



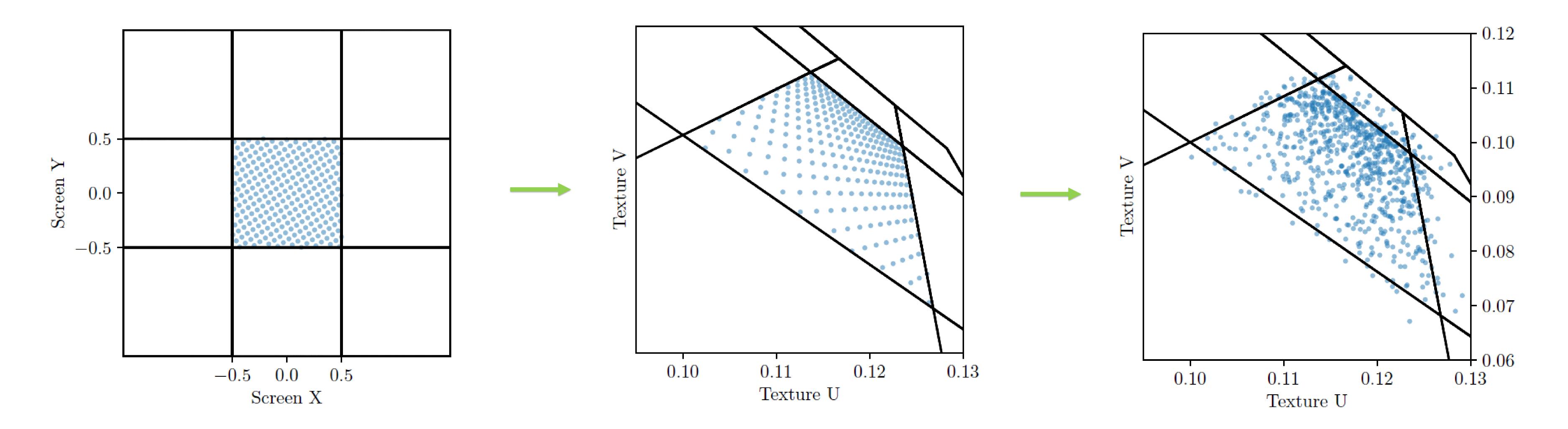


- Common practice jitter the projection matrix for anti-aliasing reconstruction filter
- Used offline (e.g., MoonRay) and real-time (TAA, DLSS)
- Projects to trapezoid, minification supersampling -> filtering after shading!





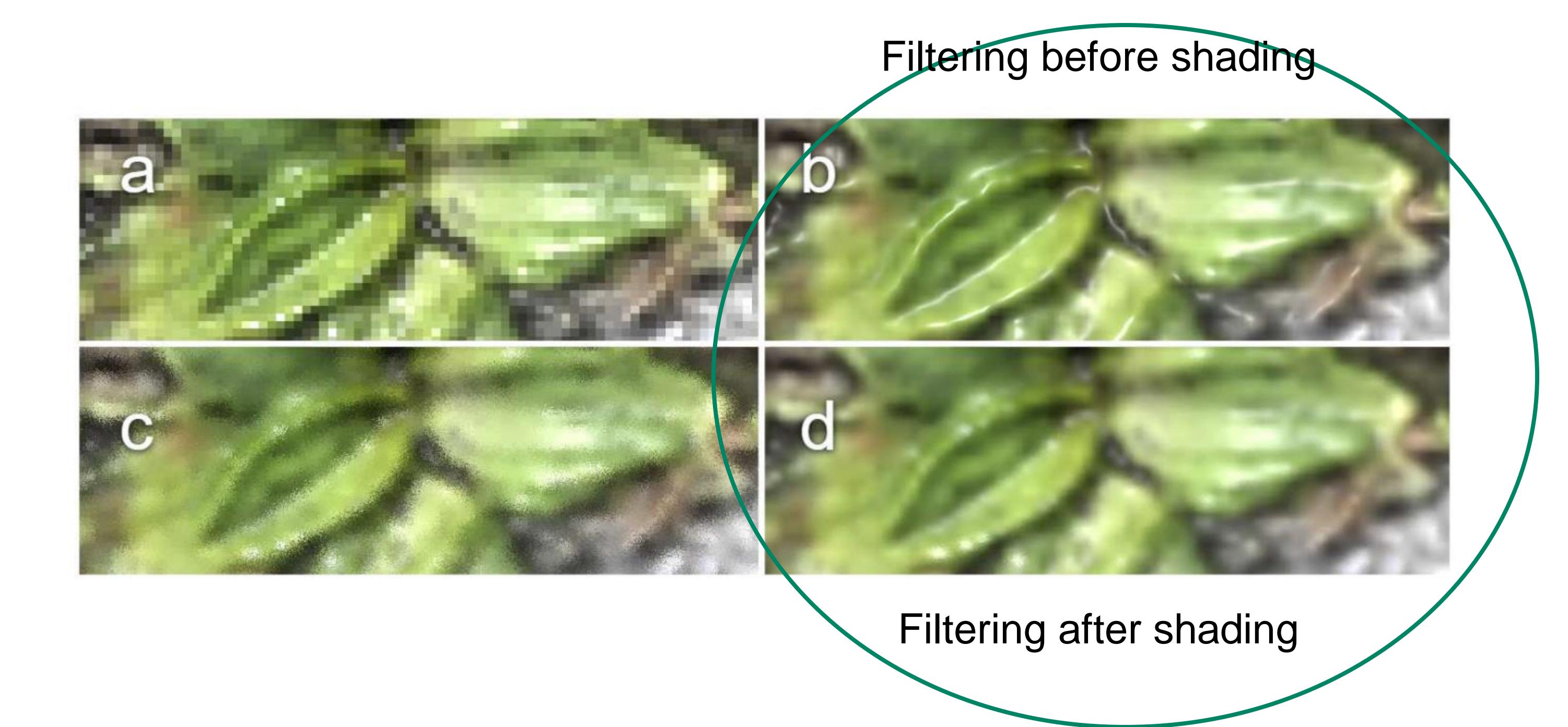
- Common practice jitter the projection matrix for anti-aliasing reconstruction filter
- Used offline (e.g., MoonRay) and real-time (TAA, DLSS)
- Projects to trapezoid, minification supersampling -> filtering after shading!
- Add magnification/translation UV jitter -> unified minification and magnification



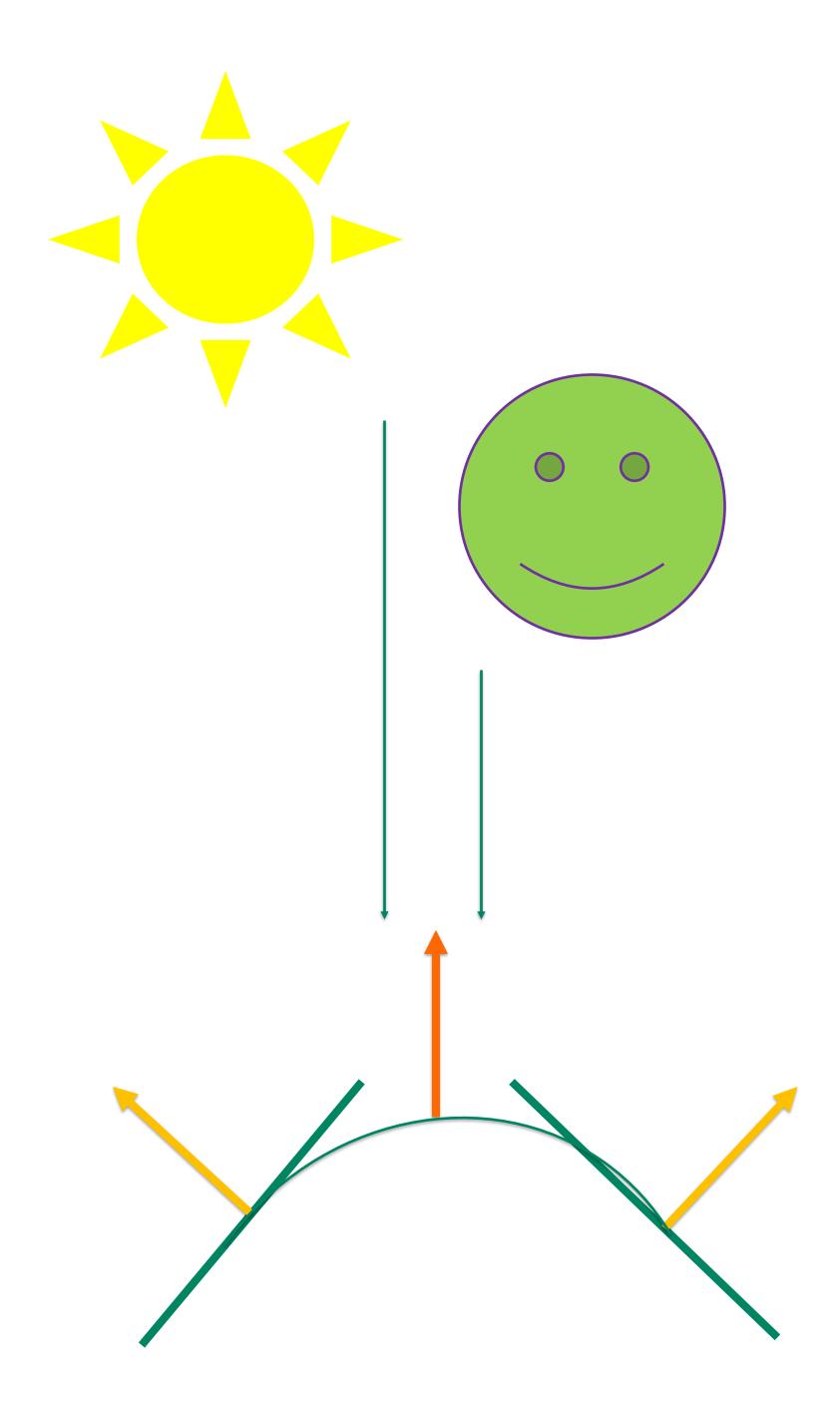




Magnification specular appearance change



Appearance change explained

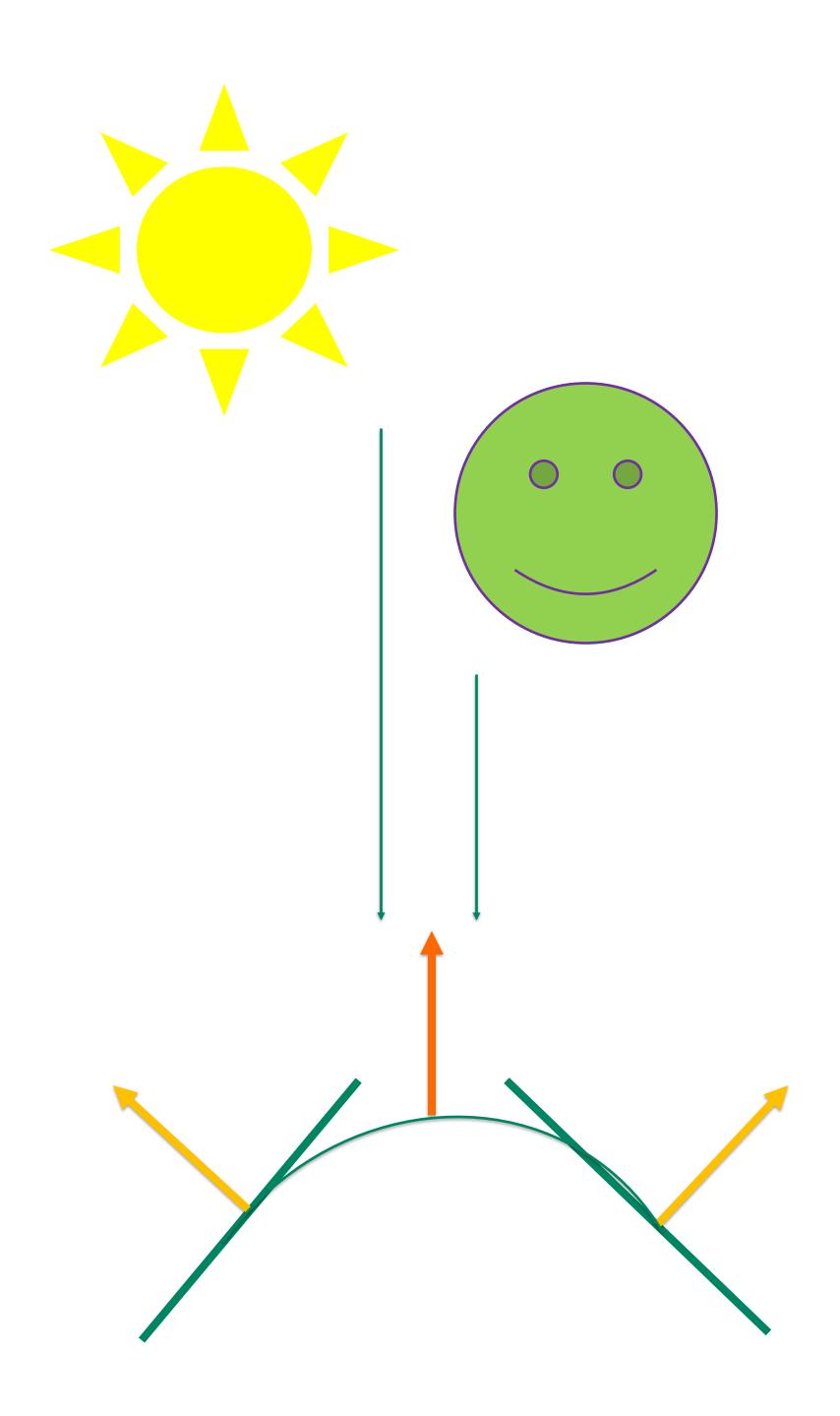


Filtering before shading:

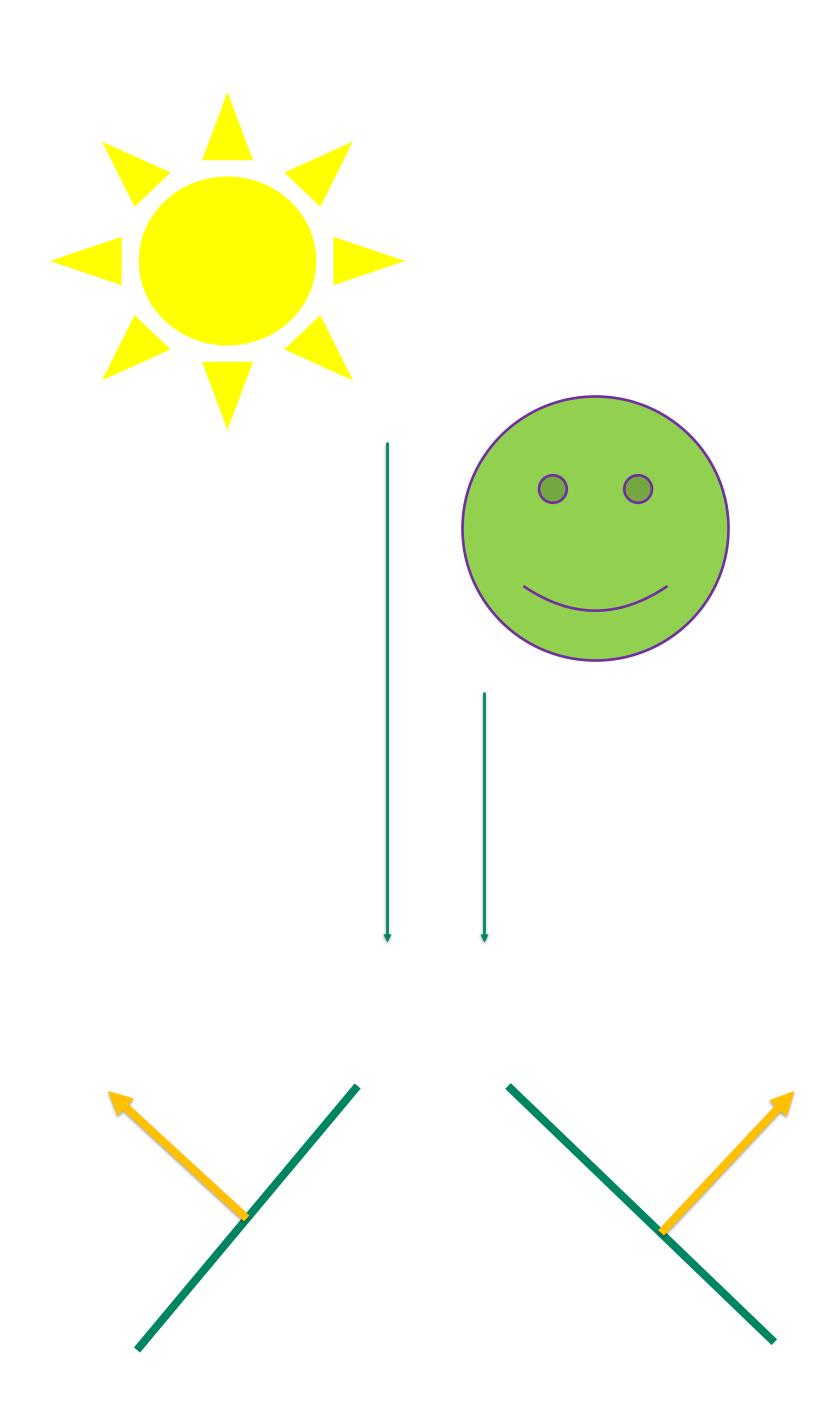
Interpolated surface and normals



Appearance change explained

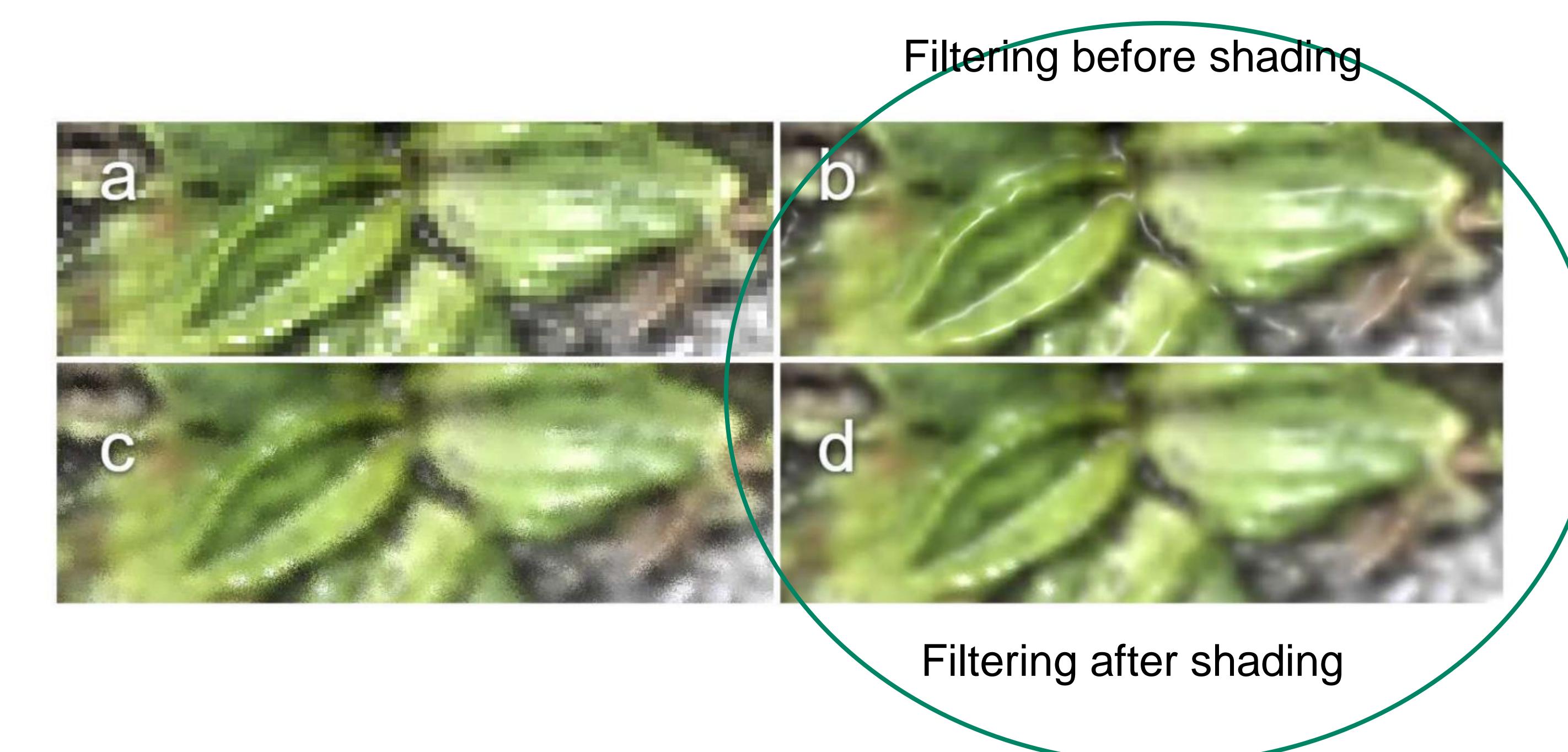


Filtering before shading: Interpolated surface and normals



Filtering after shading:
Two adjacent geometric facets and normals

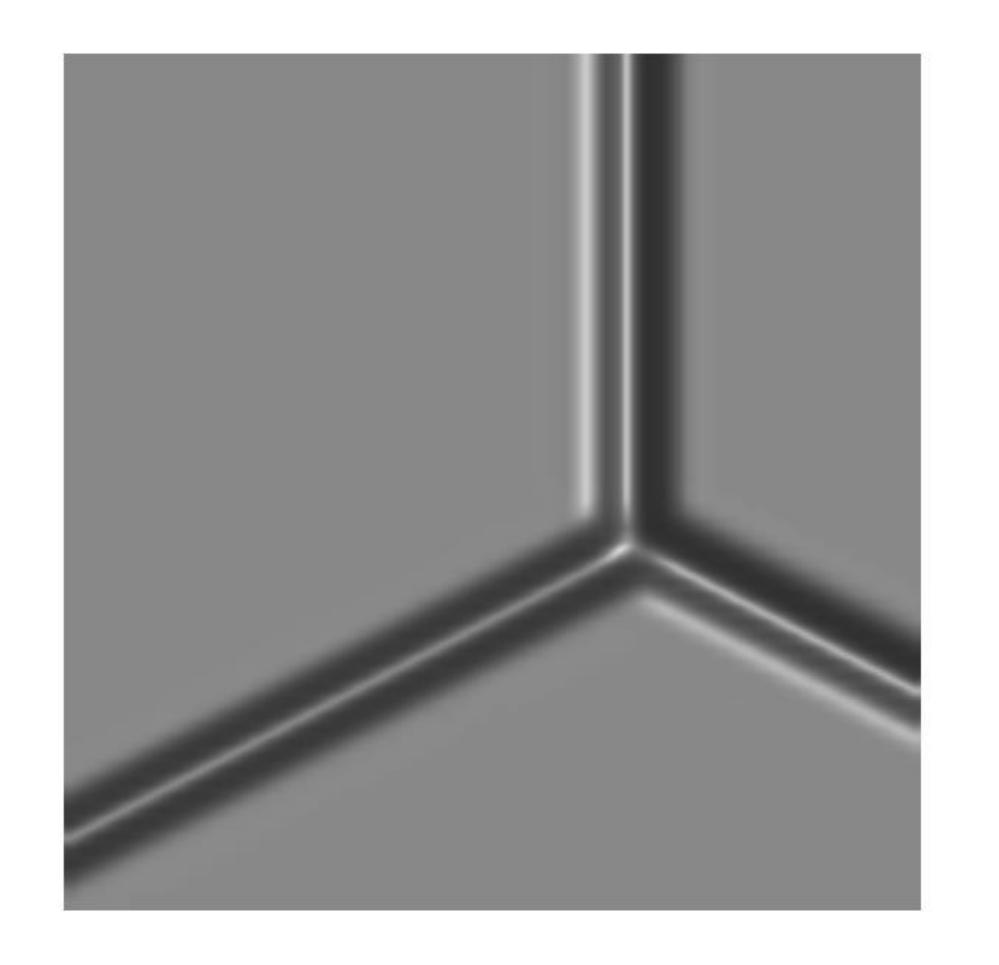
Filtering lighting does not produce surface curvature



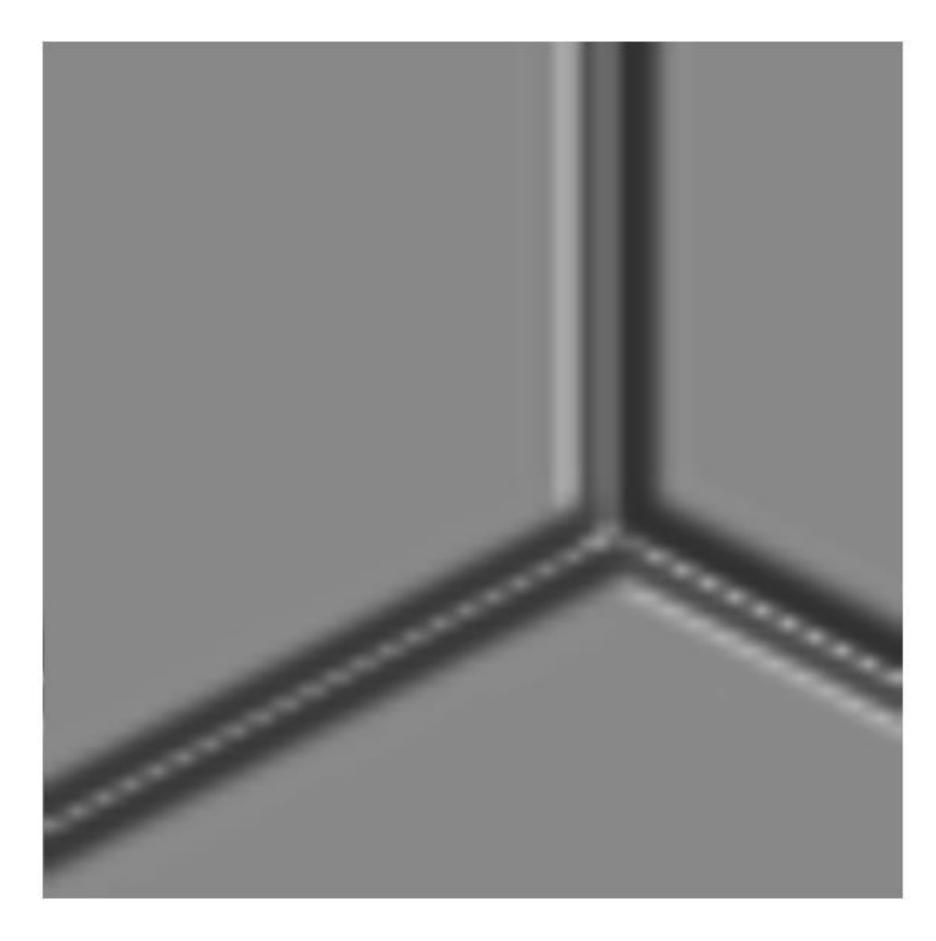
Note: it's neither "good" or "bad", depends on the intent / assumption But it changes the appearance – artists need to be aware!



Worse example – magnification aliasing



Filtering before shading

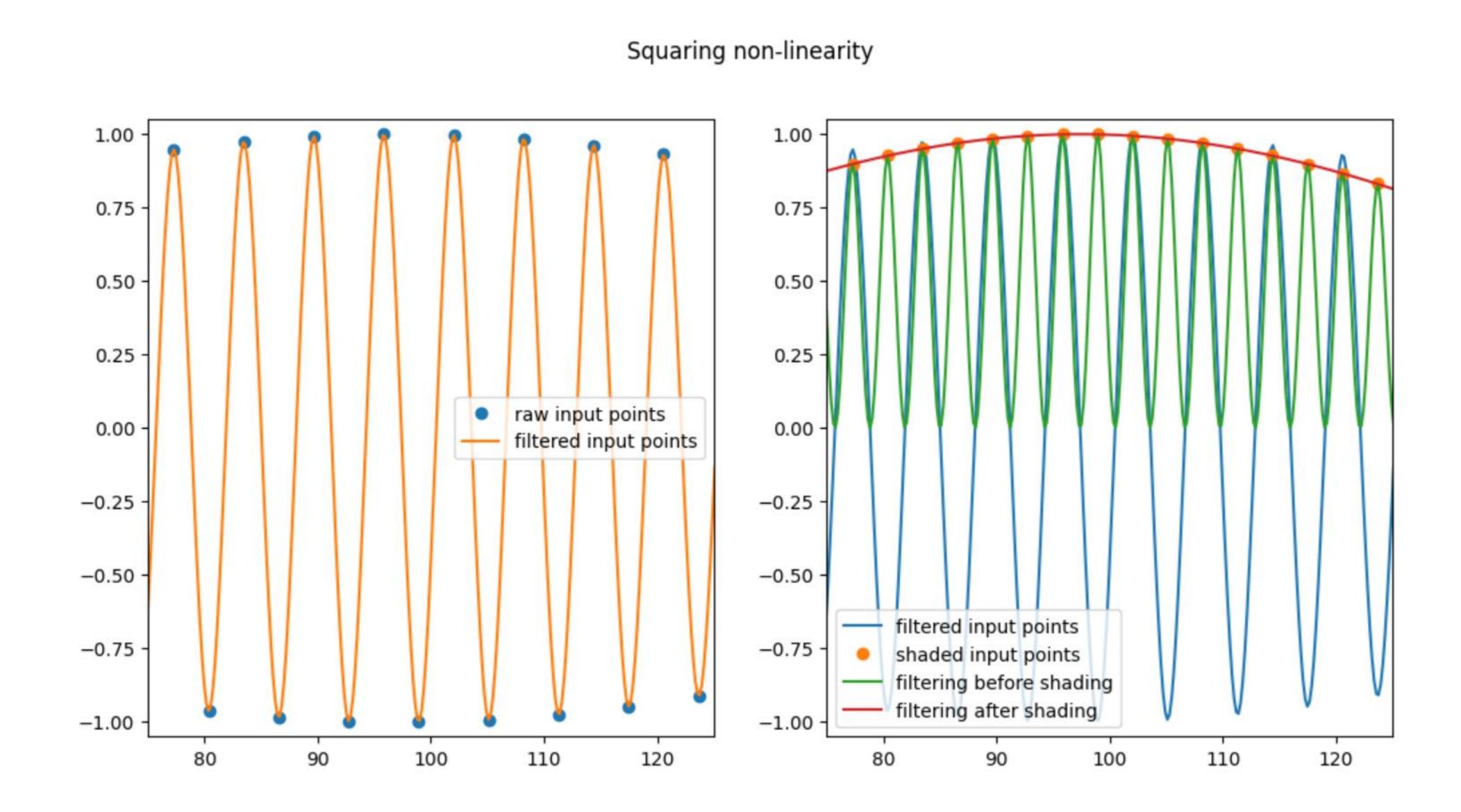


Filtering after shading



Non-linearity introduced aliasing

- Any non-linearity always introduces new, higher signal frequencies ("harmonics")
- When applied to discrete signals... those frequencies alias immediately

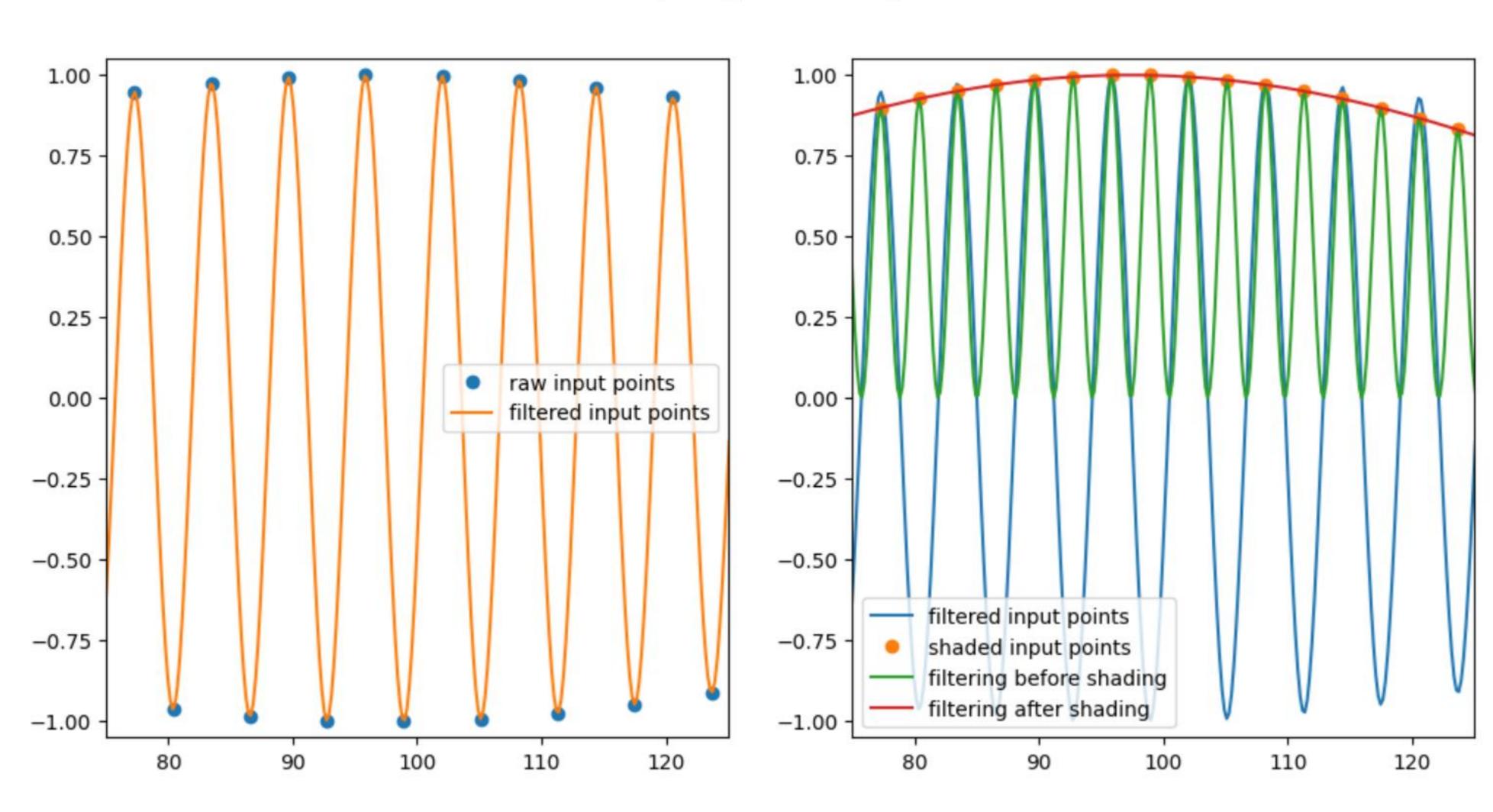




Non-linearity introduced aliasing

- Any non-linearity always introduces new, higher signal frequencies ("harmonics")
- When applied to discrete signals... those frequencies alias immediately
- Magnification: screen Nyquist higher than texture Nyquist
- For formal analysis, see the paper supplement

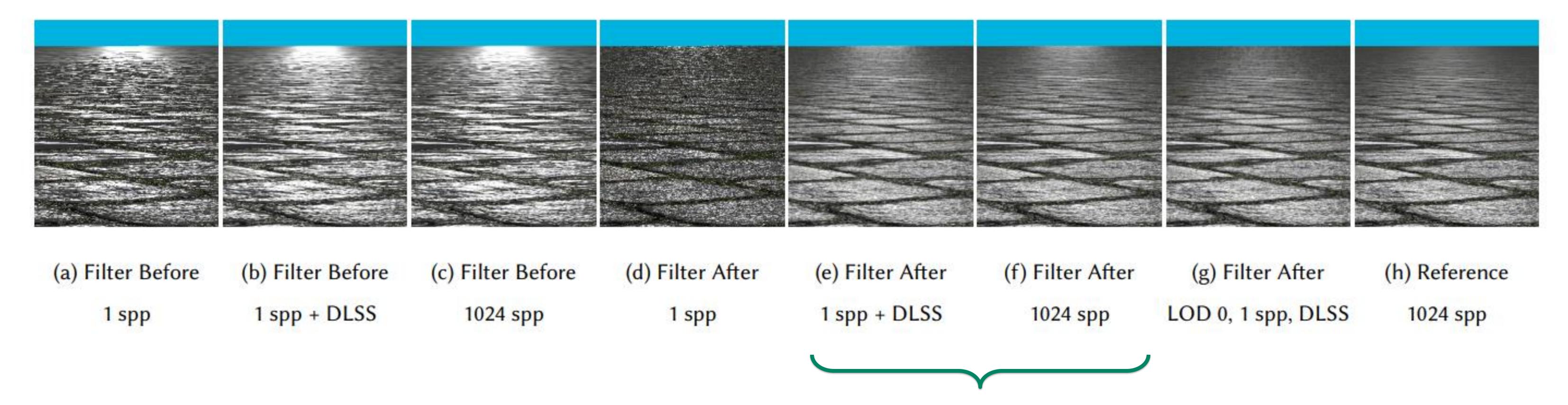








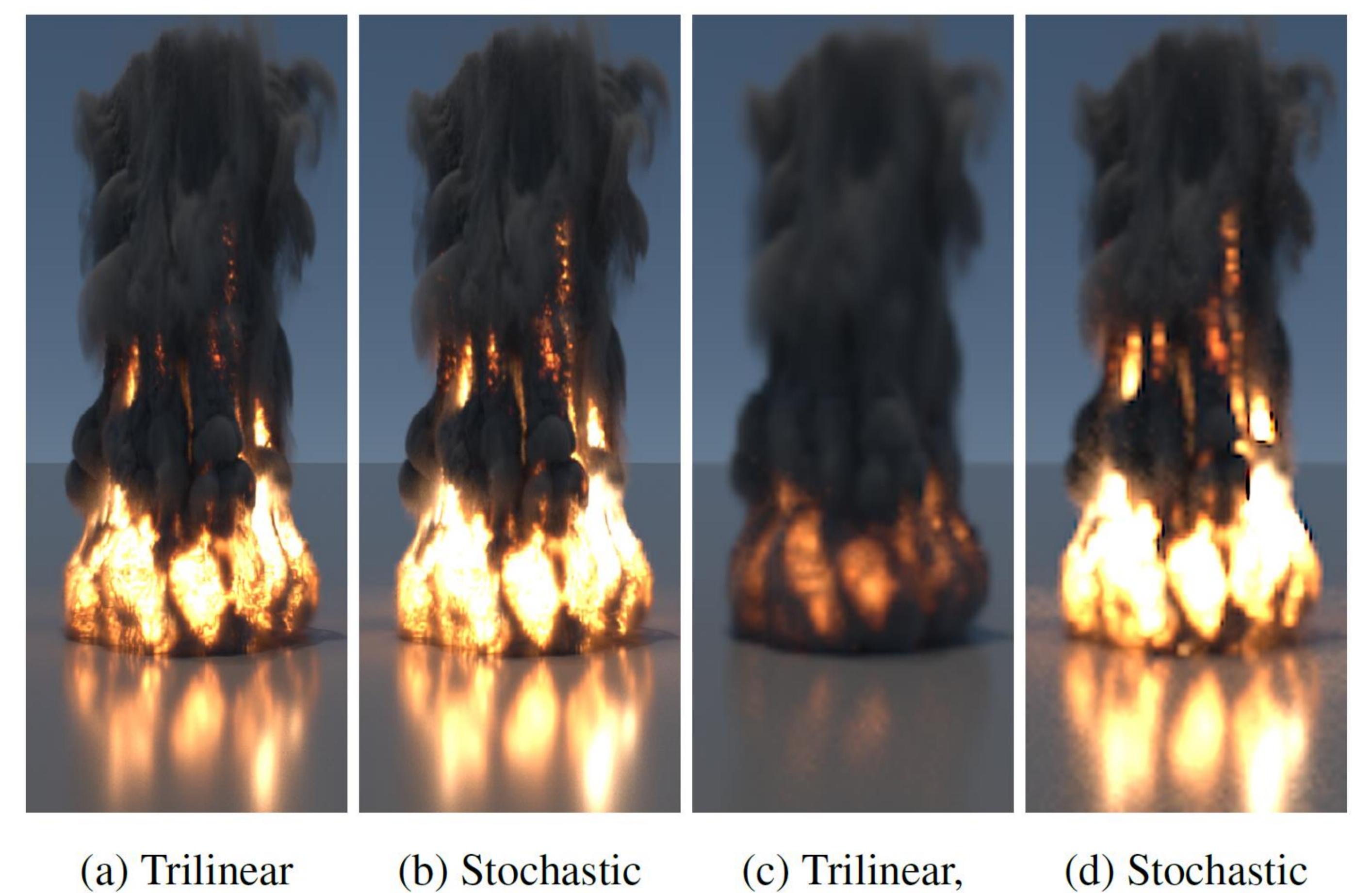
Appearance preservation – real time



Hybrid: Use a mipmap, but higher resolution (reduce cache trashing, make it easier for DLSS)



Appearance Preservation – offline, volumetric textures



trilinear

MIP mapped

minification



Offline - Improved Image Quality & Performance No additional noise!

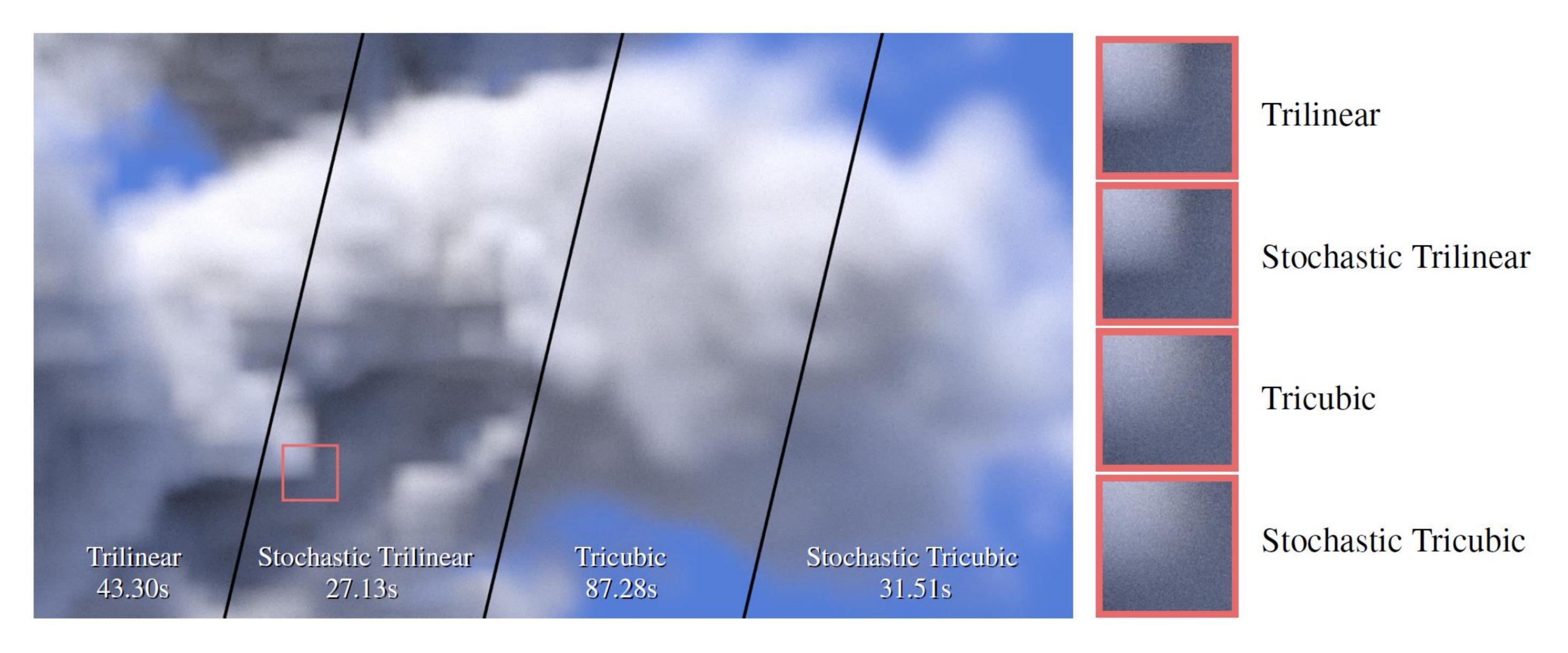
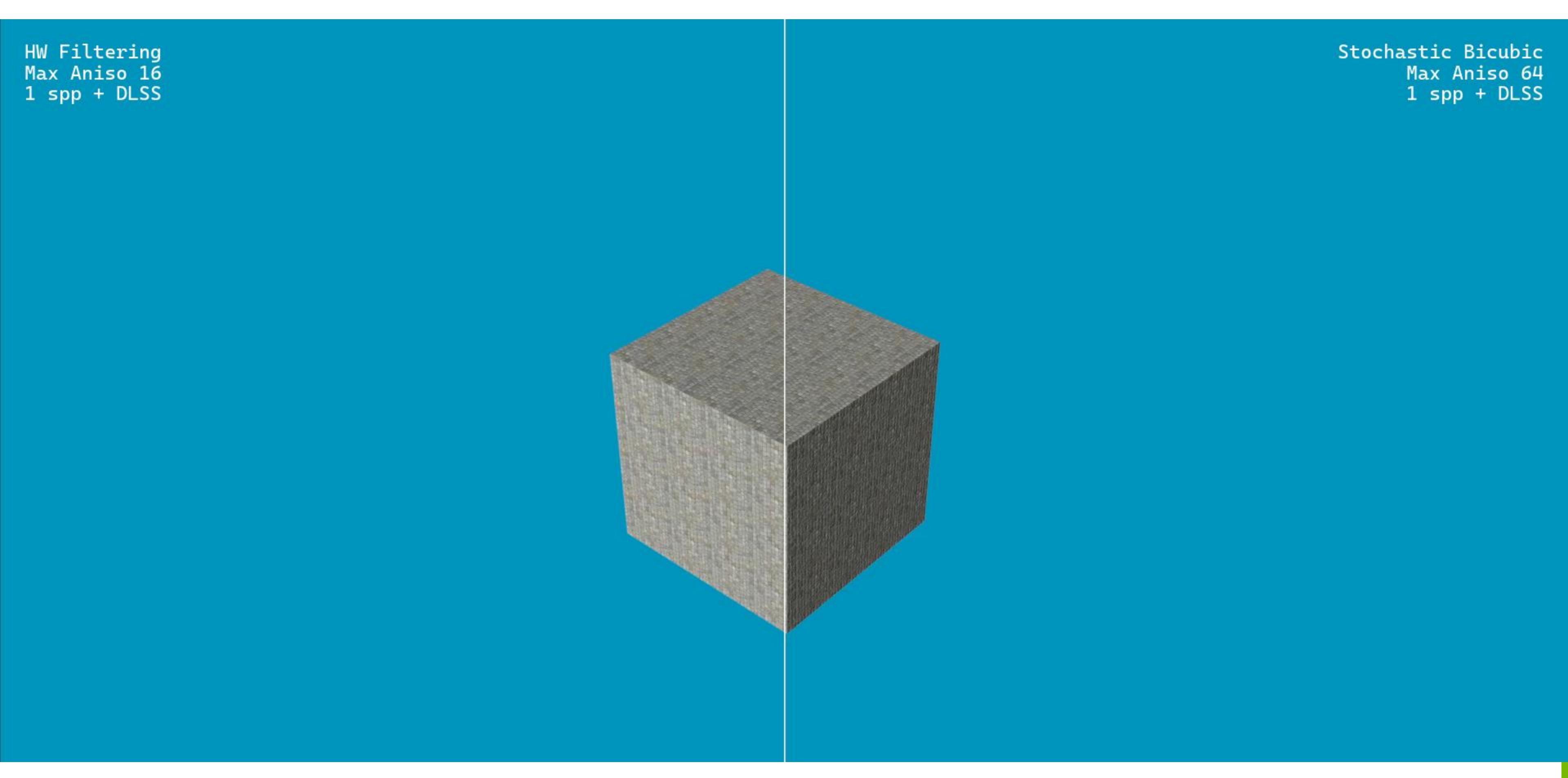


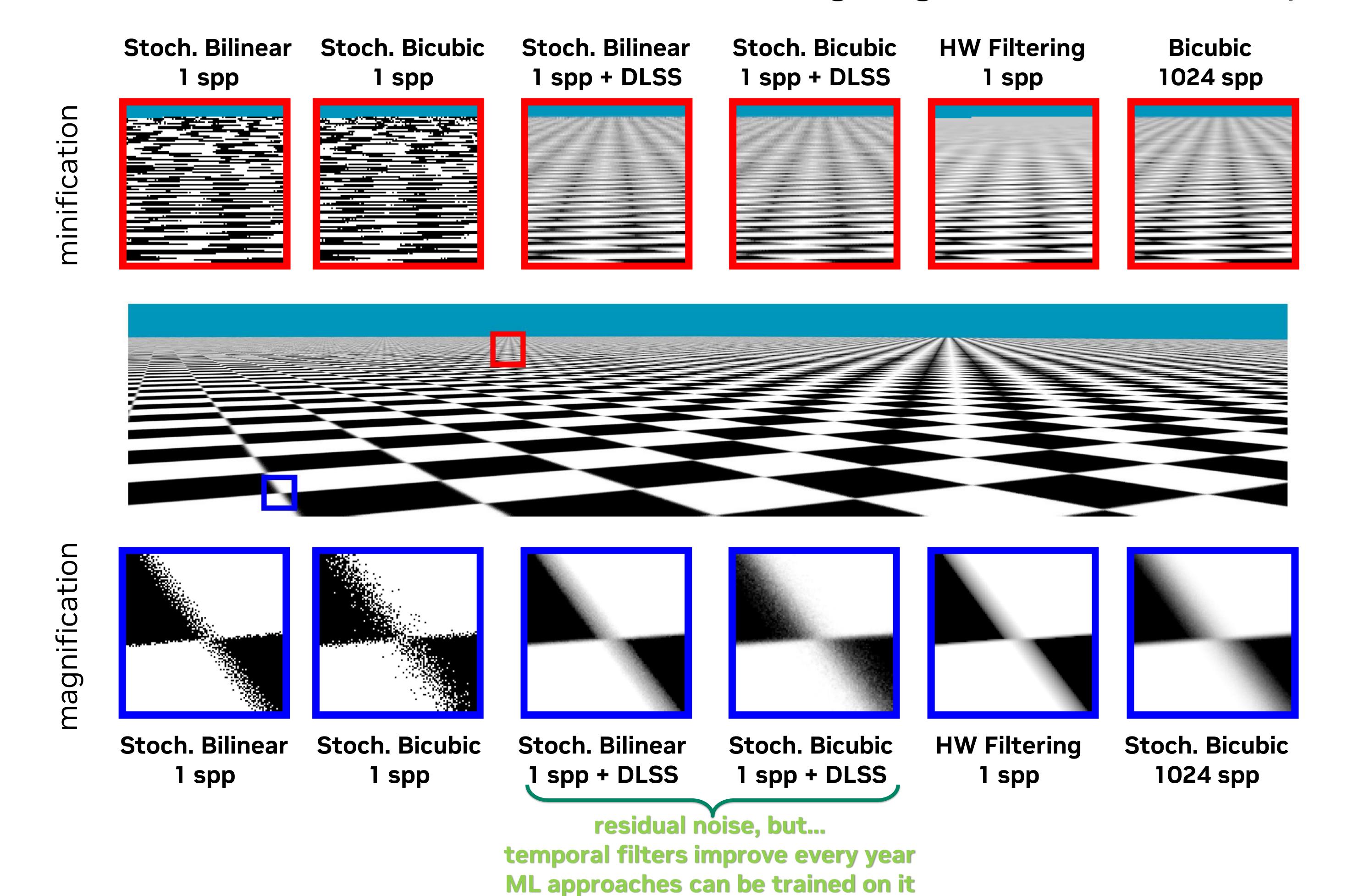
Figure 1: A section of the *Disney Cloud* scene rendered with path tracing. With this close-in viewpoint, trilinear filtering leads to blocky artifacts in the image. Tricubic filtering gives a much better result, though requires 64 voxel lookups into the *NanoVDB* representation. Stochastic filtering performs a single voxel lookup yet provides indistinguishable results, with overall rendering time speedups of $1.60 \times$ and $2.77 \times$ for the trilinear and tricubic filters. Times reported are for *pbrt-v4* running on an NVIDIA 4090 RTX GPU, rendering at 1080p with 256 samples per pixel.



Minification & Magnification DLSS + STBN Temporal Stability Test



Stress Test: Real-Time Stochastic Filtering, high contrast, no mip-maps



OVIDIA.

Recommendations

- Minification: Filtering After Shading is always better
- Minification: Offline rendering can remove mip-maps: rendering Monte Carlo noise dominates
- Minification: Real-time rendering: "hybrid" (performance, temporal stability but some bias remains)

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- Magnification: Filtering After Shading can introduce aliasing
- Magnification: It depends! Decide based on use-case, content type, maximum magnification

Recommendations

- You don't have to go "all in", we recommend a pragmatic approach:
 - There are trade-offs and cases where one is preferred over the other
 - Don't stochastically sample something that relies on interpolation (e.g., SDF fonts)
 - Use STF/non-STF/different filters on different assets only shader code changes!

Conclusions

- Our proposal of "filtering after shading" might seem radical...
- We simply formalize decades of the different film industry and gamedev practices!
 - Filtering after shading is unbiased and better for appearance preservation
 - We need to change the way we teach filtering and blending

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- Stochastic texture filtering present for ~40y in literature in various one-off flavors
 - We explain the prior approaches and generalize them
 - We propose two families of techniques with different trade-offs

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- Stochastic texture filtering present for ~40y in literature in various one-off flavors
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 - We propose two families of techniques with different trade-offs
 - We expand those to more filters, including negative lobe filters
 - Source code of efficient implementations drop-in, zero integration cost!

Summary

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 - Remove workarounds and simplify code (alpha, specular AA, virtual texture padding)
 - Enables efficient filtering of novel compression and storage formats neural, octrees, DCT, ...?

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 - Efficient better filters (isotropic, smooth, negative weights) let's get rid of bilinear!
 - Beyond textures: optimize and stochastically sample complex shader graphs
- Intrigued? Disagree? Outraged? Let's chat! ©

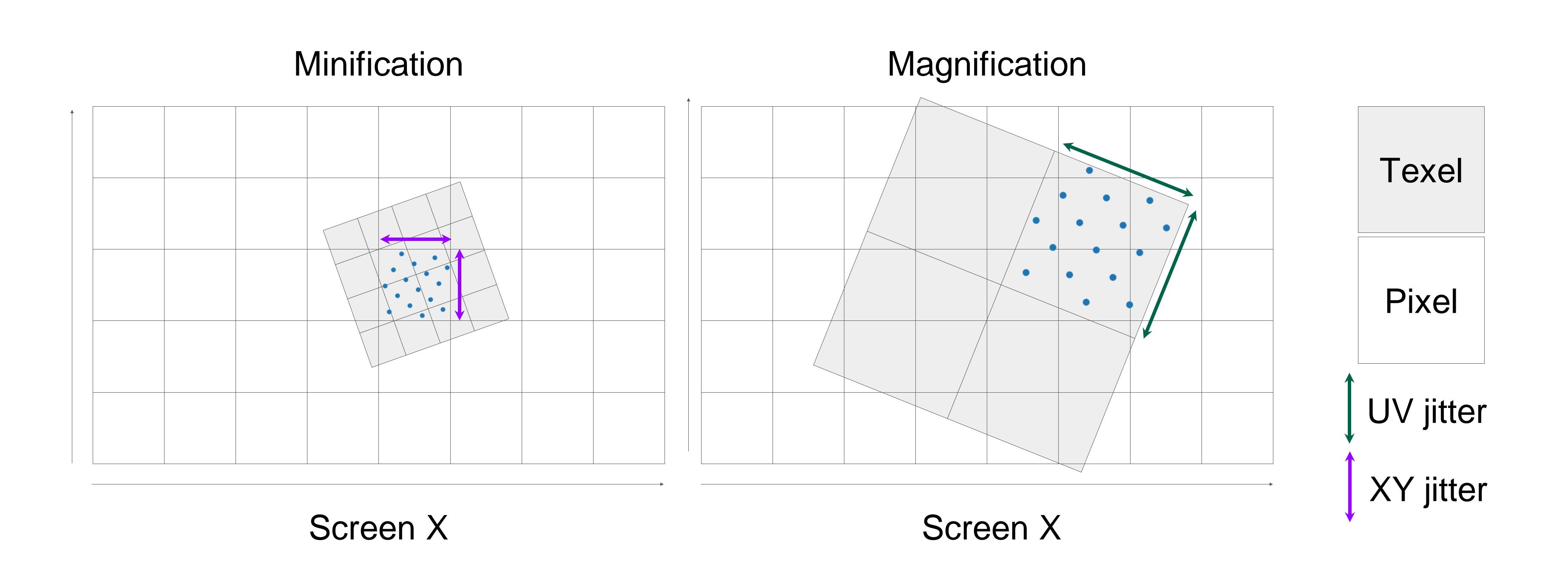




Enable Custom Texture Compression/Storage Algorithms



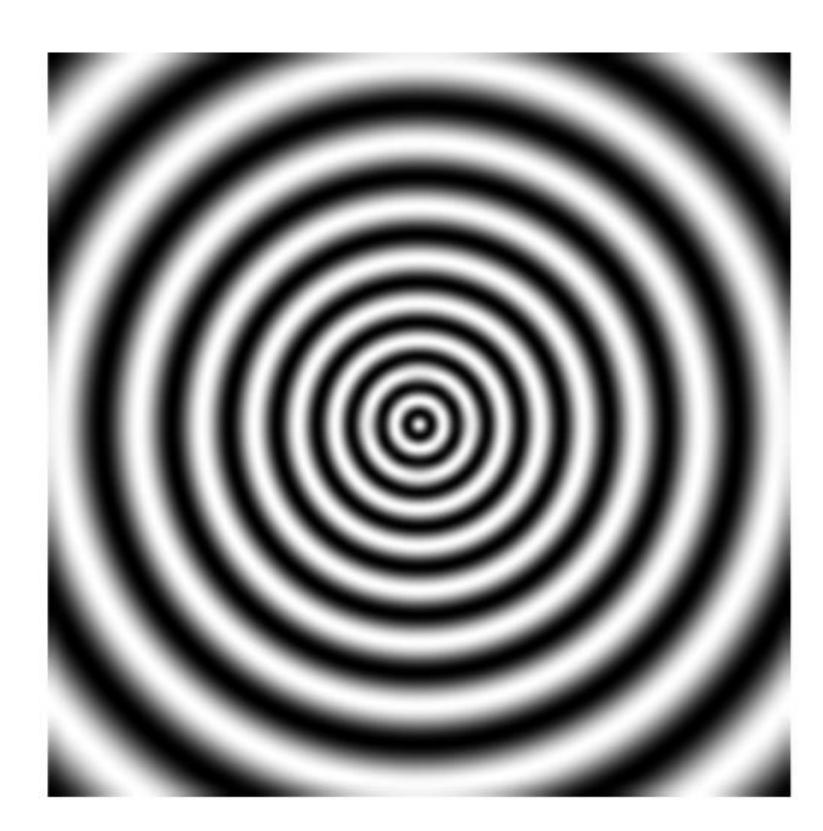
Minification vs Magnification jitter



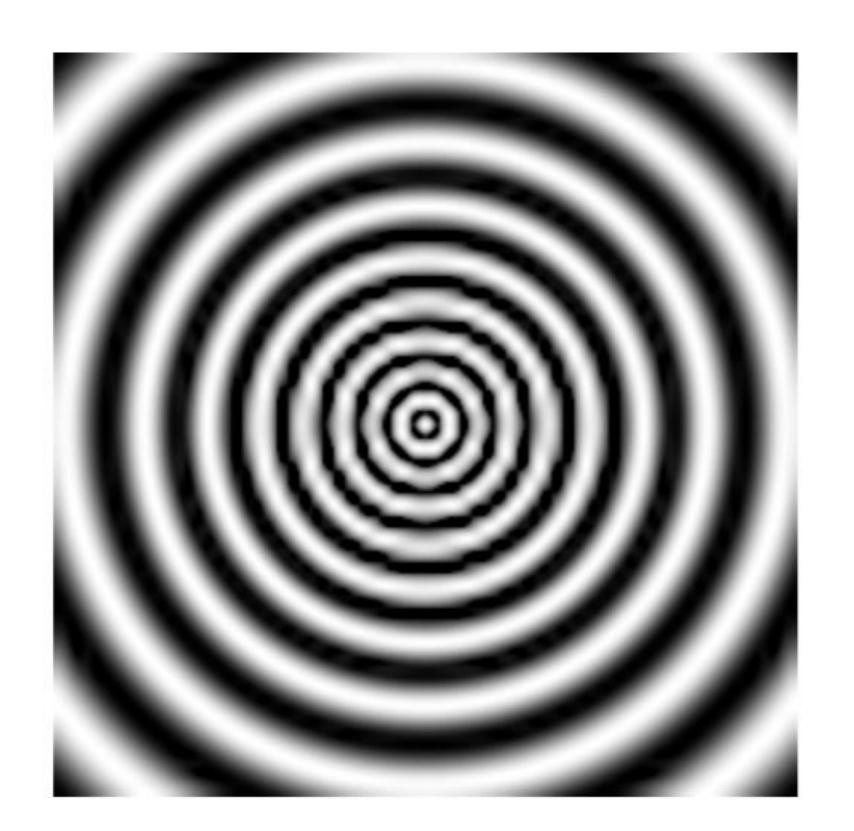


Bonus: unexpected consequence

- Something that bothered me for many years...
- We always recommend decoding to linear before generating mip-maps (minification)...
- But why upsampling/sharpening looks way better applied in sRGB/gamma space?
- Gamma conversion in either direction introduces aliasing!
- Doing/undoing gamma correction: Alias -> upsample -> Alias



Upsampling in sRGB

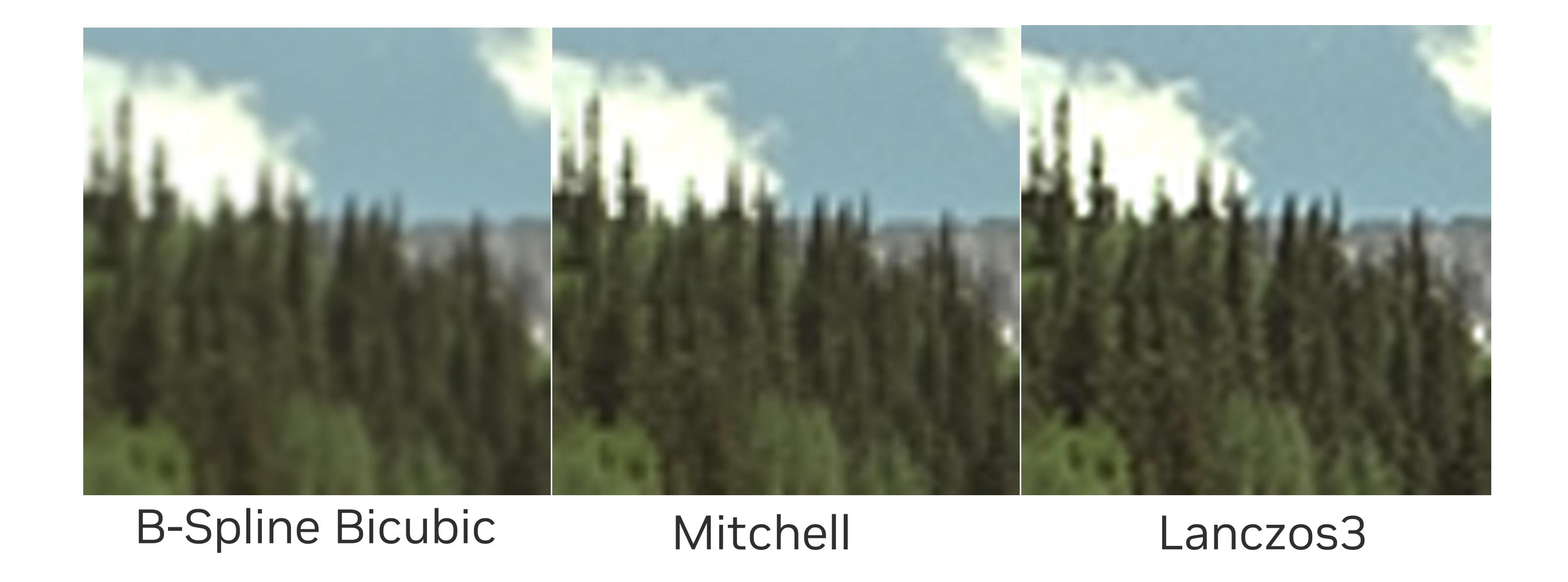


Upsampling in linear

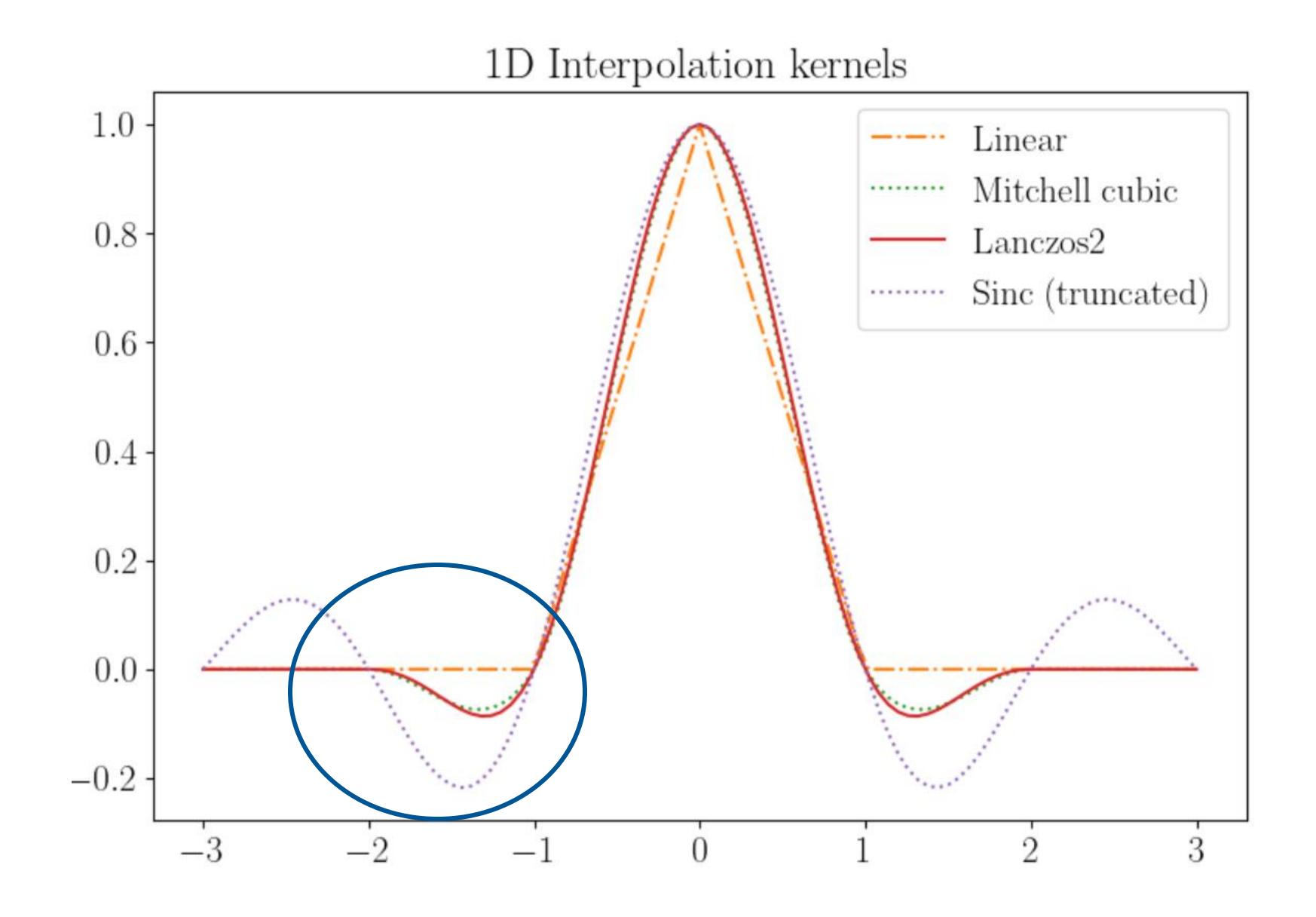




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- Approximations of a "perfect" interpolation filter
- Sharp, anti-aliased



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- Approximations of a "perfect" interpolation filter
- Sharp, anti-aliased
- Examples: Sinc, Lanczos, Mitchell...

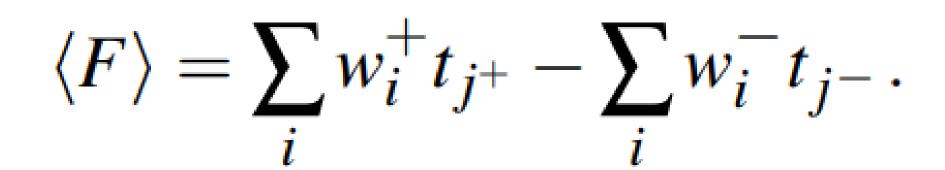


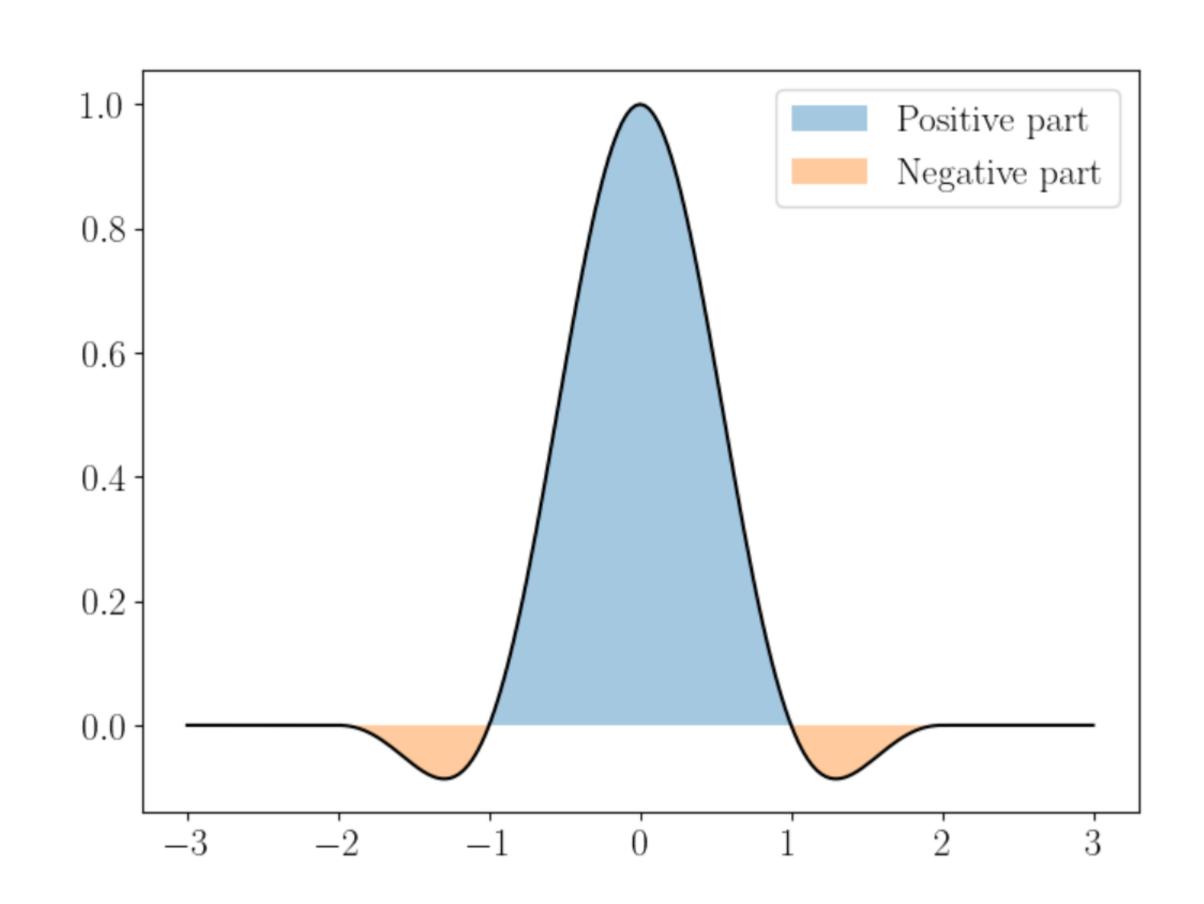
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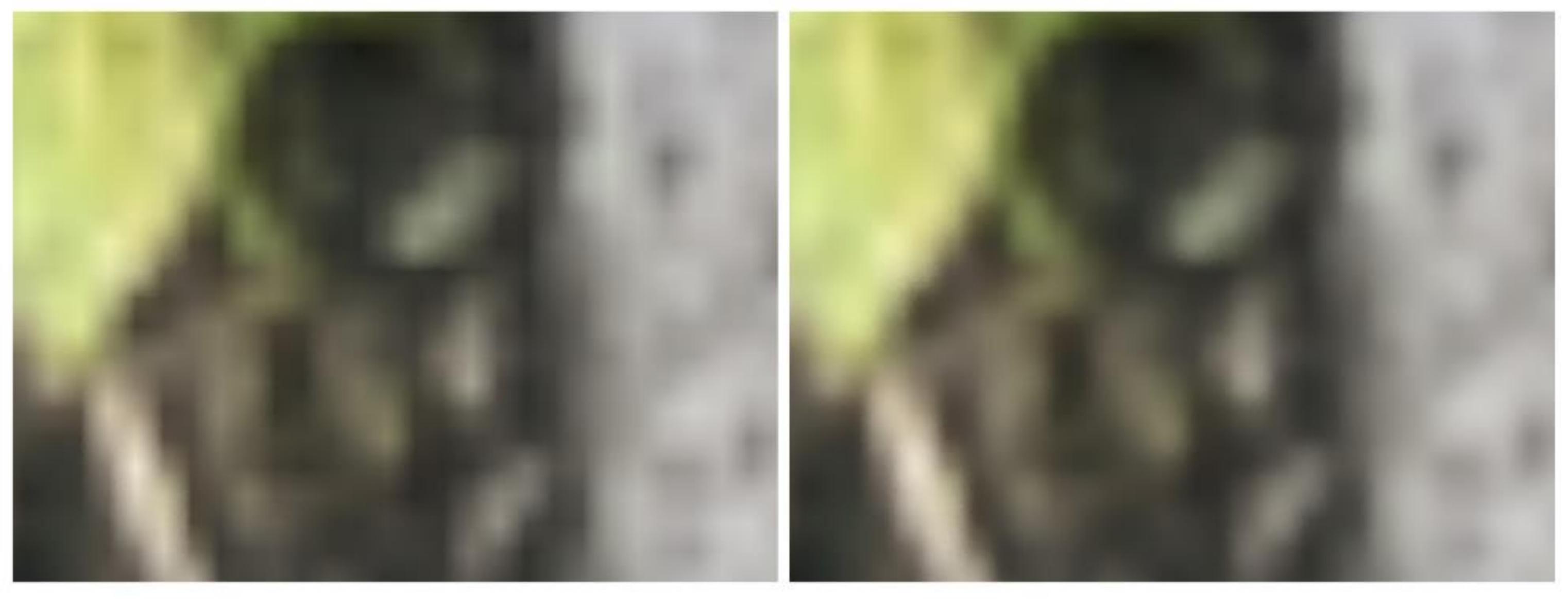
Solution – positivization

- Importance sample the positive and negative parts separately
- Always evaluate two samples
- Weight sum always positive
- 2X the cost
- Low variance





Positivization – Results



Bilinear Mitchell

