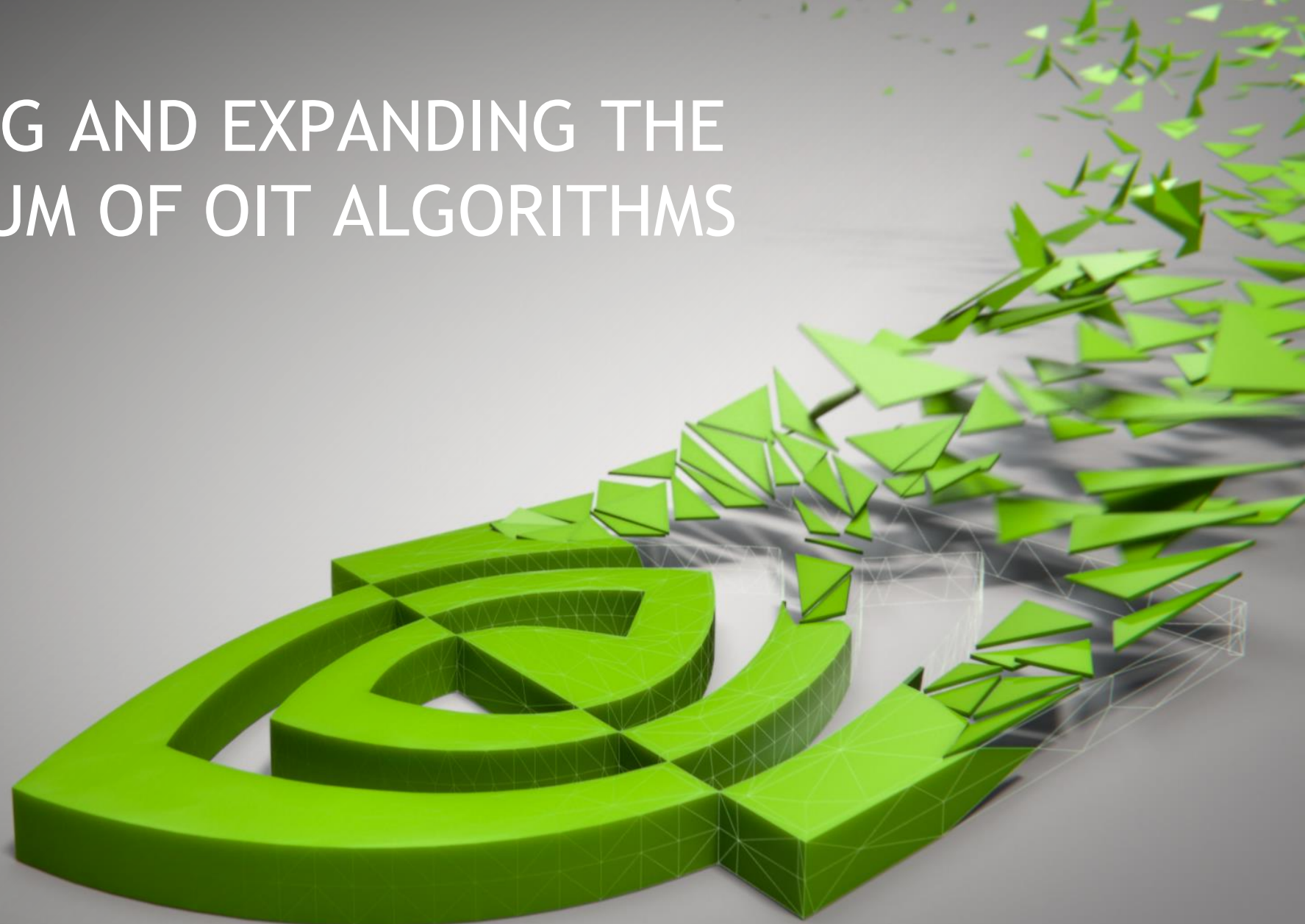


# EXPLORING AND EXPANDING THE CONTINUUM OF OIT ALGORITHMS

*Chris Wyman*



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- ▶ Not a “survey paper,” at least in the traditional sense
  - ▶ You will not identify “the right” OIT algorithm for you

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- ▶ Not a “survey paper,” at least in the traditional sense
  - ▶ You will not identify “the right” OIT algorithm for you
- ▶ Not an “algorithms paper,” at least in the traditional sense
  - ▶ Do present two new algorithms
  - ▶ Do not intend to claim these algorithms are right for you

# WHAT'S THIS PAPER ABOUT?

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- ▶ Story following my thoughts on order-independent transparency
  - ▶ Spurred by discussions w/developers
    - ▶ E.g., Johan Andersson's SIGGRAPH 2015 talk

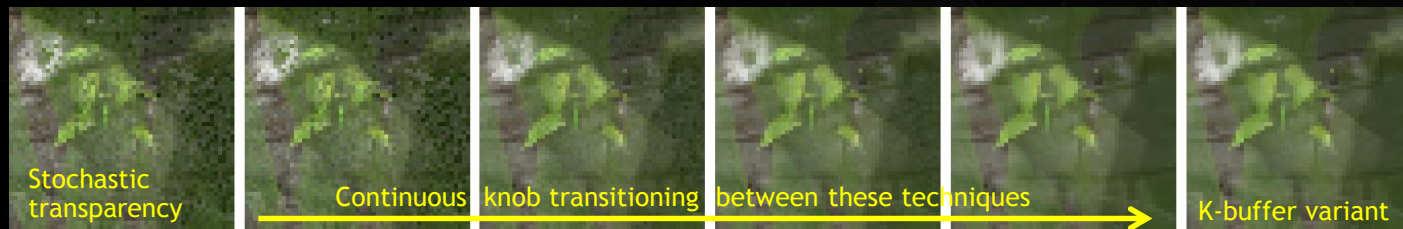


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  - ▶ Started with re-exploration of space
  - ▶ Placed on multi-dimensional continuum
  - ▶ Develop algorithms exploring new spaces
    - ▶ Will talk about one today: Stochastic Layered Alpha Blending
    - ▶ Provides continuous transition between stochastic transparency & k-buffering





**Why is OIT hard?**

# WHY BOTHER AT ALL?

- ▶ [Porter and Duff 84] outlined numerous common compositing operations
  - ▶ The “over” operator, using multiplicative blending, describes most real interactions:

$$c_{result} = \alpha_0 c_0 + (1 - \alpha_0) \alpha_1 c_1$$

- ▶ For streaming compute, you need to sort geometry or keep all  $\alpha_i$  and  $c_i$  around

Merge two fragments then later try to insert one in between?



# WHY BOTHER AT ALL?

- ▶ Sorting geometry in advance can fail
  - ▶ May be no “correct” order for triangles
- ▶ Keep a list of fragments per pixel (i.e., A-Buffers [Carpenter 84])
  - ▶ Virtually unbounded\*\* GPU memory
  - ▶ Still need to sort fragments to apply over operator in correctly
- ▶ Not just a raster problem; affects ray tracing, too
  - ▶ Unless it guarantees ray hits returned perfectly ordered



# Building an OIT continuum

# HOW DO OIT ALGORITHMS WORK?

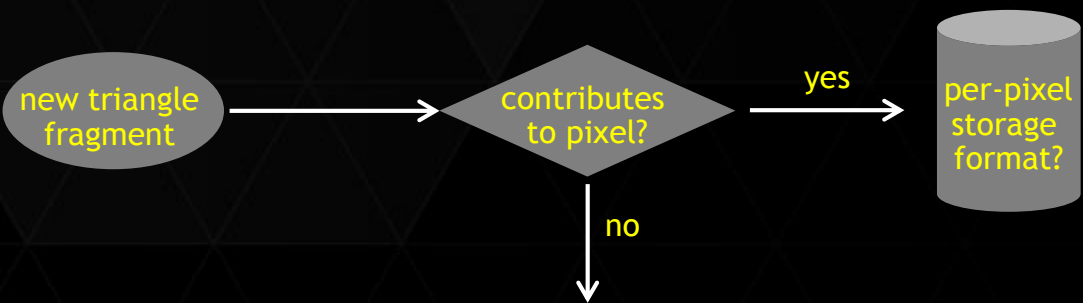


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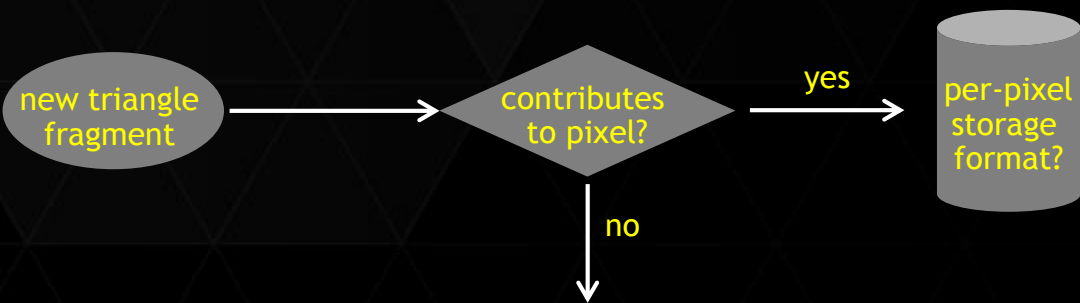


- ▶ Different answers, including:
  - ▶ Only if closest fragment [Depth peeling]
  - ▶ Closest & passes  $\alpha$ -threshold [Alpha testing]
  - ▶ Randomly decide [Stochastic transparency]
  - ▶ Always use new fragments [Most algorithms]

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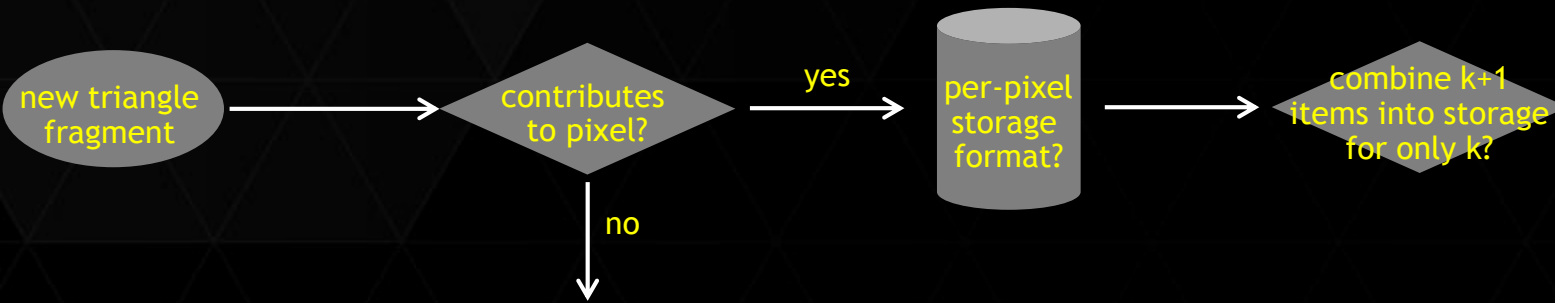


## ▶ Different answers, including:

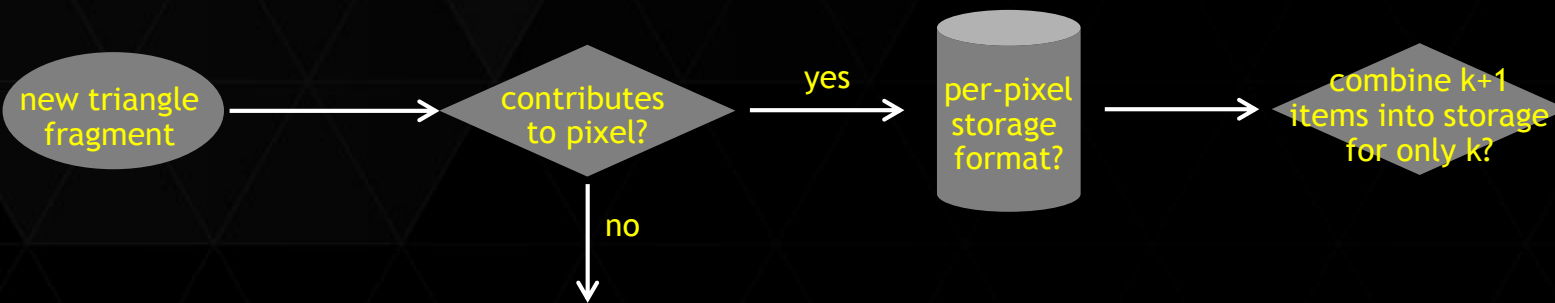
- ▶ Store 1 layer per pass [Depth peeling]
- ▶ Store k layers [K-buffer, alpha blending (k=1), many other algorithms]
- ▶ Store k samples [Stochastic transparency]
- ▶ Store k nodes [Deep shadow maps]
- ▶ Store k coefficients [Fourier opacity maps]



# HOW DO OIT ALGORITHMS WORK?



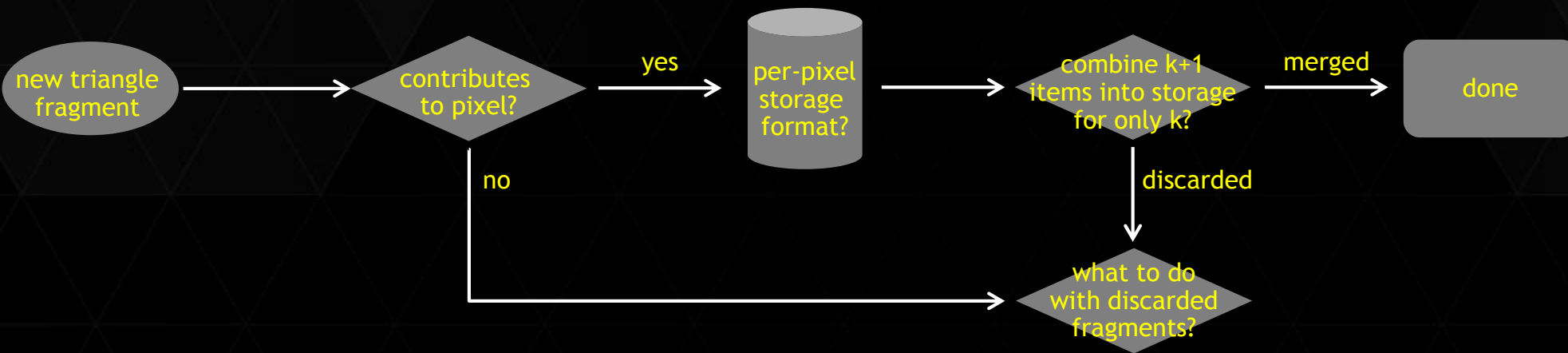
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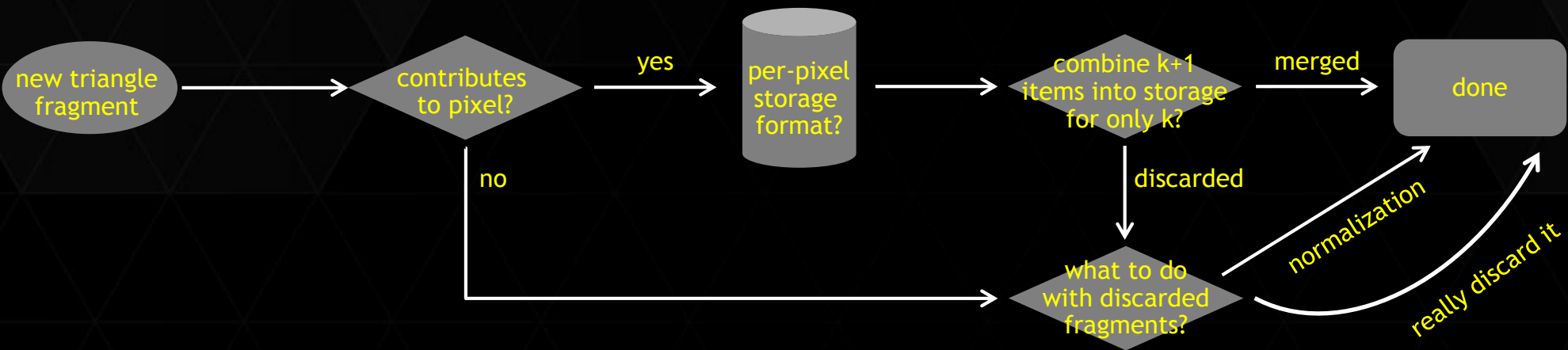
- ▶ Discard furthest [Depth peeling, hybrid transparency]
- ▶ Merge frags w / closest depth [ $Z^3$ ]
- ▶ Merge 2 most distant frags [Multi-layer alpha blend]
- ▶ Merge 2 most near frags [Original k-buffer]
- ▶ Sum coefs in Fourier space [Fourier opacity maps]

# HOW DO OIT ALGORITHMS WORK?



- ▶ Discarding introduces bias or noise

# HOW DO OIT ALGORITHMS WORK?



- Discarding introduces bias or noise
  - That's OK; discard [Depth peeling, screen-door transparency]
  - Sum  $\alpha$ -weighted contribs of discarded frags [Stochastic transparency, hybrid transparency, phenomenological models]

# CONTINUUM SUMMARY

Algorithm	Memory Limit	Insertion Heuristic	Merge Heuristic	Normalize?	Use Alpha or Coverage?
A-buffer [Car84]	none	always	no merging	no	either <sup>†</sup>
Alpha Testing	1 layer	if $\alpha >$ thresh	discard furthest	no	alpha
Alpha Compositing [PD84]	1 layer	always	<i>over</i> operator	no	alpha
Screen-Door Transparency [FGH*85]	k z-samples	always	z-test, discard occluded	no	coverage
Z <sup>3</sup> [JC99]	k layers	always	merge w/closest depths	no	alpha
Deep Shadow Maps [LV00]	k line segments	always	merge w/smallest error	no	alpha
Depth Peeling [Eve01]	1 layer	if closest	discard furthest	no	either <sup>†</sup>
Opacity Shadow Maps [KN01]	k bins	always	$\alpha$ -weighted sum	no	alpha
Density Clustering [MKBVR04]	k bins	always	k-means clustering	no	alpha
k-Buffers [BCL*07]	k layers	always	merge closest to camera	no	alpha
Sort-Independent Alpha Blending [Mes07]	1 layer	always	weighted sum	no	alpha
Deep Opacity Maps [YK08]	k bins	always	$\alpha$ -weighted sum	no	alpha
Multi-Layer Depth Peeling [LHLW09]	k layers	if in k closest	discard furthest	no	either <sup>†</sup>
Occupancy Maps [SA09]	k bins	always	discard if bin occupied	renormalize alpha	alpha
Stochastic Transparency [ESSL10]	k samples	stochastic	z-test, discard occluded	$\alpha$ -weighted average	coverage
Fourier Opacity Maps [JB10]	k Fourier coefs	always	sum in Fourier domain	no	alpha
Adaptive Volumetric Shadow Maps [SVLL10]	k layers	always	merge w/smallest error	no	alpha
Transmittance Function Maps [DGMF11]	k DCT coefs	always	sum in DCT basis	no	alpha
Adaptive Transparency [SML11]	k layers	always	merge w/smallest error	no	alpha
Hybrid Transparency [MCTB13]	k layers	always	discard furthest	$\alpha$ -weighted average	alpha
Weighted Blended OIT [MB13]	empirical func	never	discard all	$\alpha$ -weighted average	alpha
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Notice: Normalization only occurs when algorithms "discard" fragments

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Normalization can be viewed as “storing k+1 layers,” using  $\alpha$ -weighted merge on the furthest layer

# So what?

*(Or: Let's look at an example of how this is useful)*



# CONTINUUM SUMMARY

Interesting note

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    - ▶ *(MSAA pattern simplified for display)*

Values represent current depth sample

1.0	1.0	1.0	1.0
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Values represent current depth sample

0.5	1.0	1.0	0.5
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0.5	1.0	0.5	0.5
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Set 8 samples to red; depth test each

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Values represent current depth sample

0.5	1.0	0.7	0.5
0.7	0.5	0.5	0.7
0.5	0.7	0.5	0.5
1.0	0.5	0.7	1.0

Set 8 samples to blue; depth test each

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Values represent current depth sample

0.5	0.3	0.7	0.3
0.7	0.5	0.5	0.3
0.5	0.3	0.3	0.5
0.3	0.3	0.7	0.3

Set 8 samples to green; depth test each

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  - ▶ Second: draw blue fragment,  $z = 0.7$ ,  $\alpha = 0.5$
  - ▶ Third: draw green fragment,  $z = 0.3$ ,  $\alpha = 0.5$
  - ▶ Fourth: draw yellow fragment,  $z = 0.9$ ,  $\alpha = 1.0$

Values represent current depth sample

0.5	0.3	0.7	0.3
0.7	0.5	0.5	0.3
0.5	0.3	0.3	0.5
0.3	0.3	0.7	0.3

Set 16 samples to yellow; depth test each

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    - ▶ Third: draw green fragment,  $z = 0.3$ ,  $\alpha = 0.5$
    - ▶ Fourth: draw yellow fragment,  $z = 0.9$ ,  $\alpha = 1.0$
- ▶ 2<sup>nd</sup> pass accum. color using this as depth oracle

Values represent current depth sample

0.5	0.3	0.7	0.3
0.7	0.5	0.5	0.3
0.5	0.3	0.3	0.5
0.3	0.3	0.7	0.3



# OBSERVATIONS

- ▶ Can lose surfaces (like yellow one)
  - ▶ But it still converges; surface loss is *stochastic*

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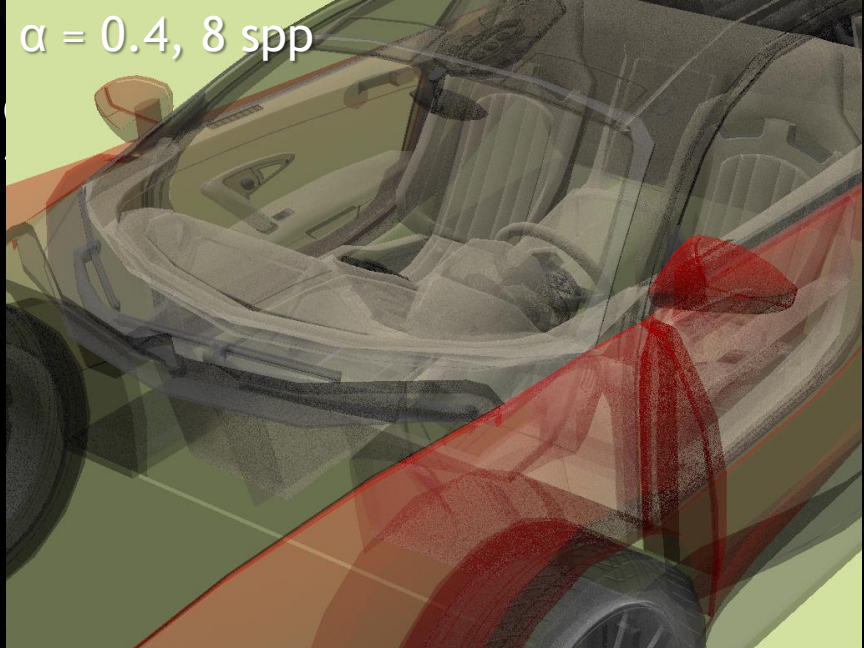
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- ▶ Can lose surfaces (like yellow one)
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- ▶ Loss worse if nearby surfaces almost opaque
  - ▶ Could easily lose blue surface

0.5	0.3	0.7	0.3
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  - ▶ Also noticed in my experiments
    - ▶ Dashboard and seat noisier with high alpha than low!



Note: Even uses stratified sampling!

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- ▶ Seems wasteful to store 8 copies of  $z = 0.3$  \*\*
  - ▶ Why not store one copy of  $z = 0.3$  and a coverage mask?

0.5	0.3	0.7	0.3
0.7	0.5	0.5	0.3
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- ▶ Seems wasteful to store 8 copies of  $z = 0.3$  \*\*
  - ▶ Why not store one copy of  $z = 0.3$  and a coverage mask?
- ▶ *Implicitly* layered – stores (up to) 16 surfaces per pixel (for 16x MSA)
  - ▶ Also wasteful to store just 3 layers in a structure that can hold 16

0.5	0.3	0.7	0.3
0.7	0.5	0.5	0.3
0.5	0.3	0.3	0.5
0.3	0.3	0.7	0.3

# Stochastic Layered Alpha Blending (SLAB)

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- ▶ Identical results to  $k$  spp stoc. transparency, if  $k \geq b$ 
  - ▶ But can independently change values of  $k$  and  $b$ 
    - ▶ Useful since stoc. transp. rarely stores  $k$  surfaces in a  $k$ -sample buffer
    - ▶ Also can explicitly increase  $b$  much further  $\rightarrow$  reduce noise on existing layers

# WHAT IS STOCHASTIC LAYERED ALPHA BLEND?

- ▶ Our same example from before:
  - ▶ First: draw red fragment,  $z = 0.5$ ,  $\alpha = 0.5$



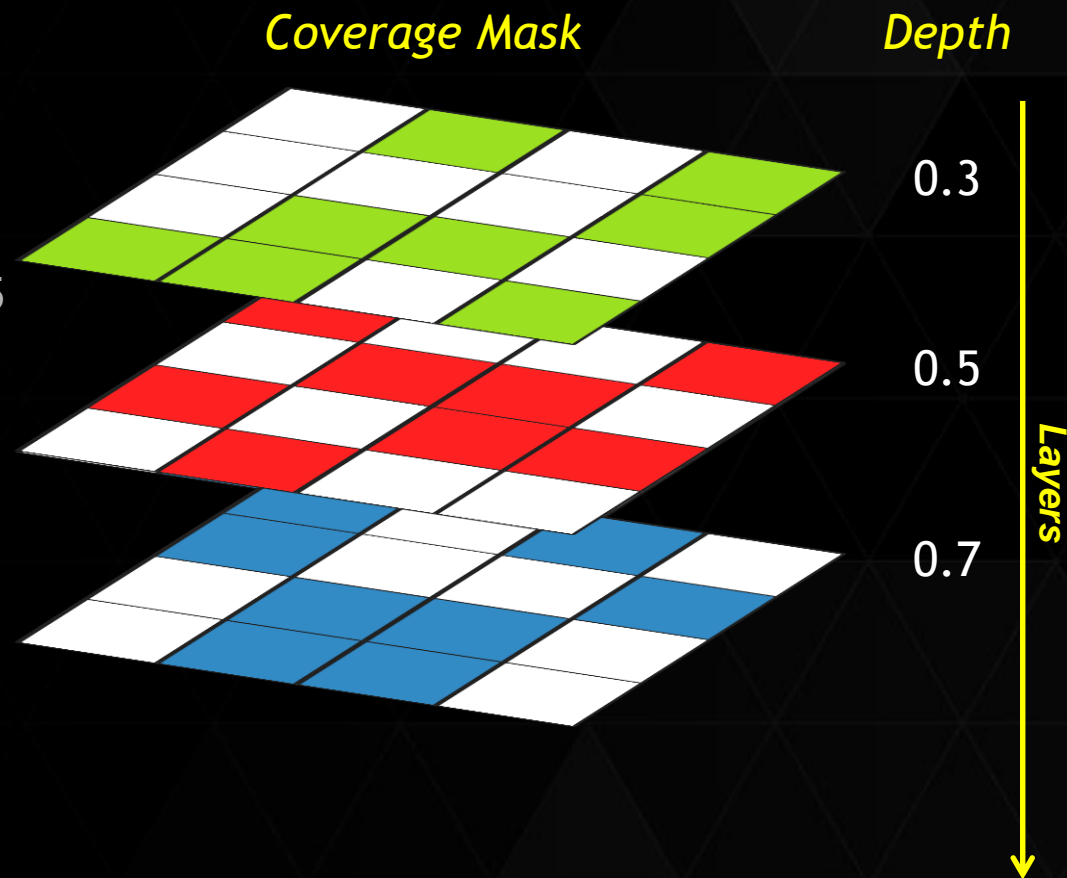
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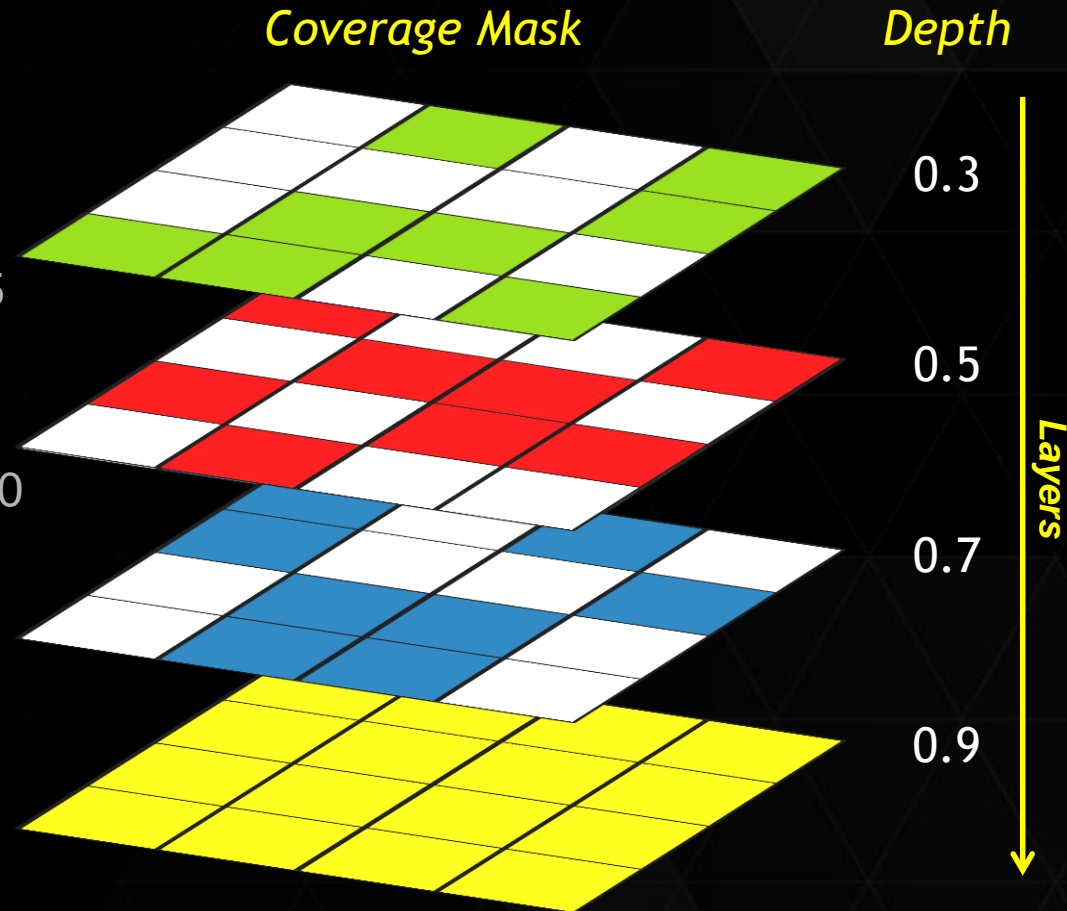
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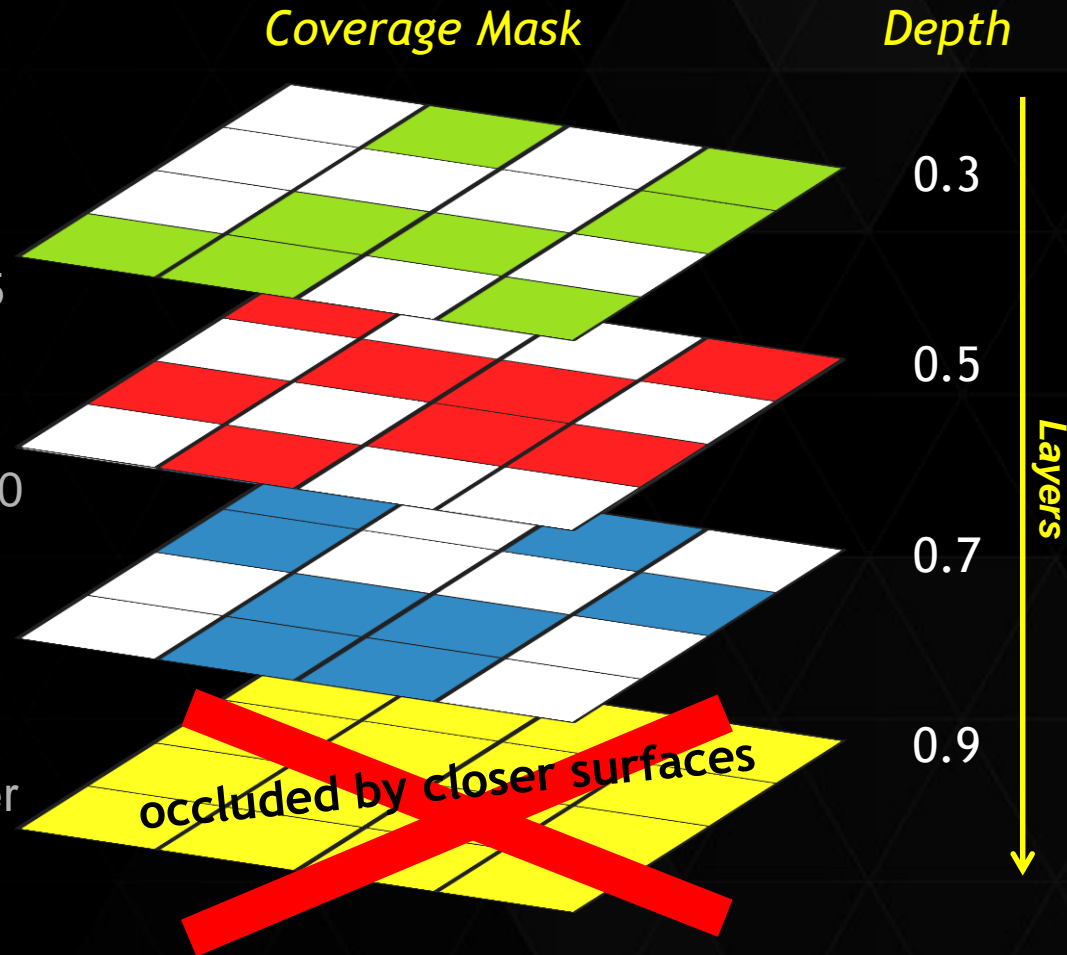
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  - ▶ Second: draw blue fragment,  $z = 0.7$ ,  $\alpha = 0.5$
  - ▶ Third: draw green fragment,  $z = 0.3$ ,  $\alpha = 0.5$
  - ▶ Fourth: draw yellow fragment,  $z = 0.9$ ,  $\alpha = 1.0$



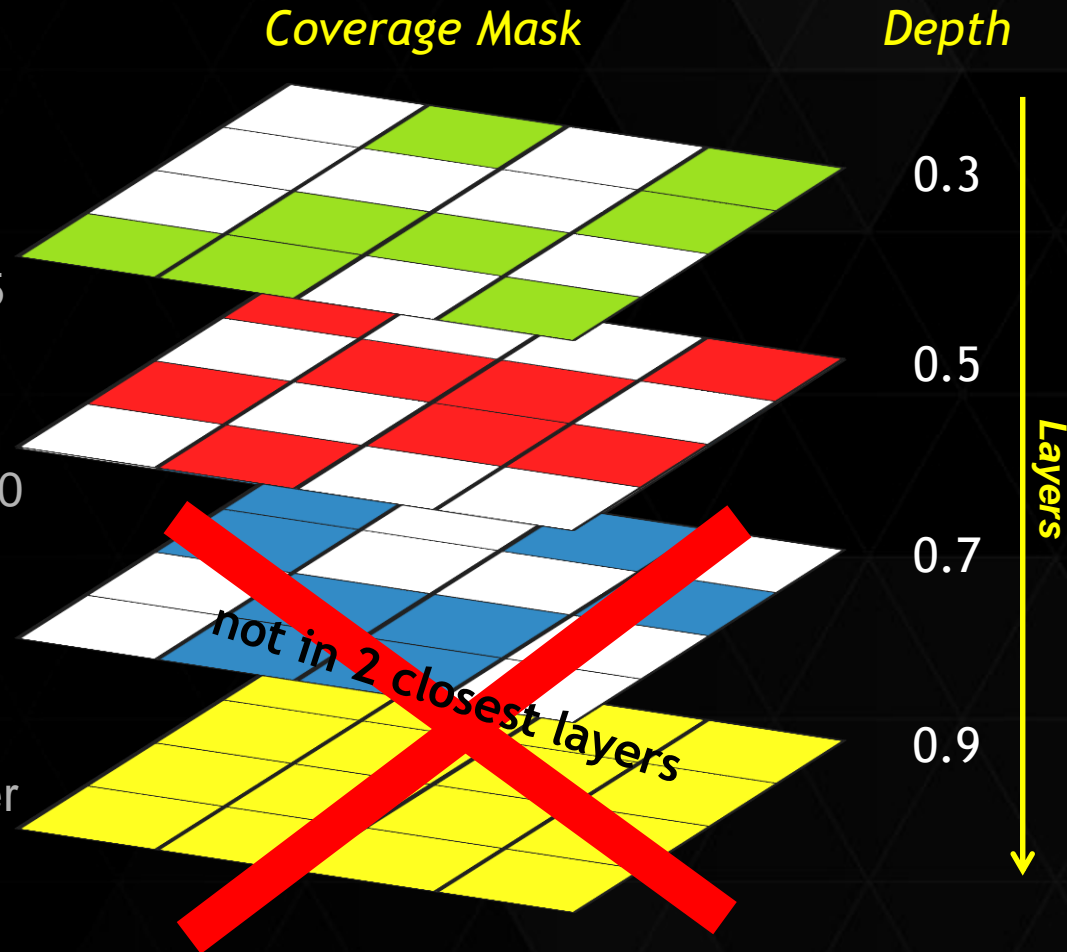
# WHAT IS STOCHASTIC LAYERED ALPHA BLEND?

- ▶ Our same example from before:
  - ▶ First: draw red fragment,  $z = 0.5$ ,  $\alpha = 0.5$
  - ▶ Second: draw blue fragment,  $z = 0.7$ ,  $\alpha = 0.5$
  - ▶ Third: draw green fragment,  $z = 0.3$ ,  $\alpha = 0.5$
  - ▶ Fourth: draw yellow fragment,  $z = 0.9$ ,  $\alpha = 1.0$
- ▶ Layers get inserted only if not occluded
  - ▶ Adds stochasm, if masks randomly chosen
  - ▶ Different random masks might keep this layer



# WHAT IS STOCHASTIC LAYERED ALPHA BLEND?

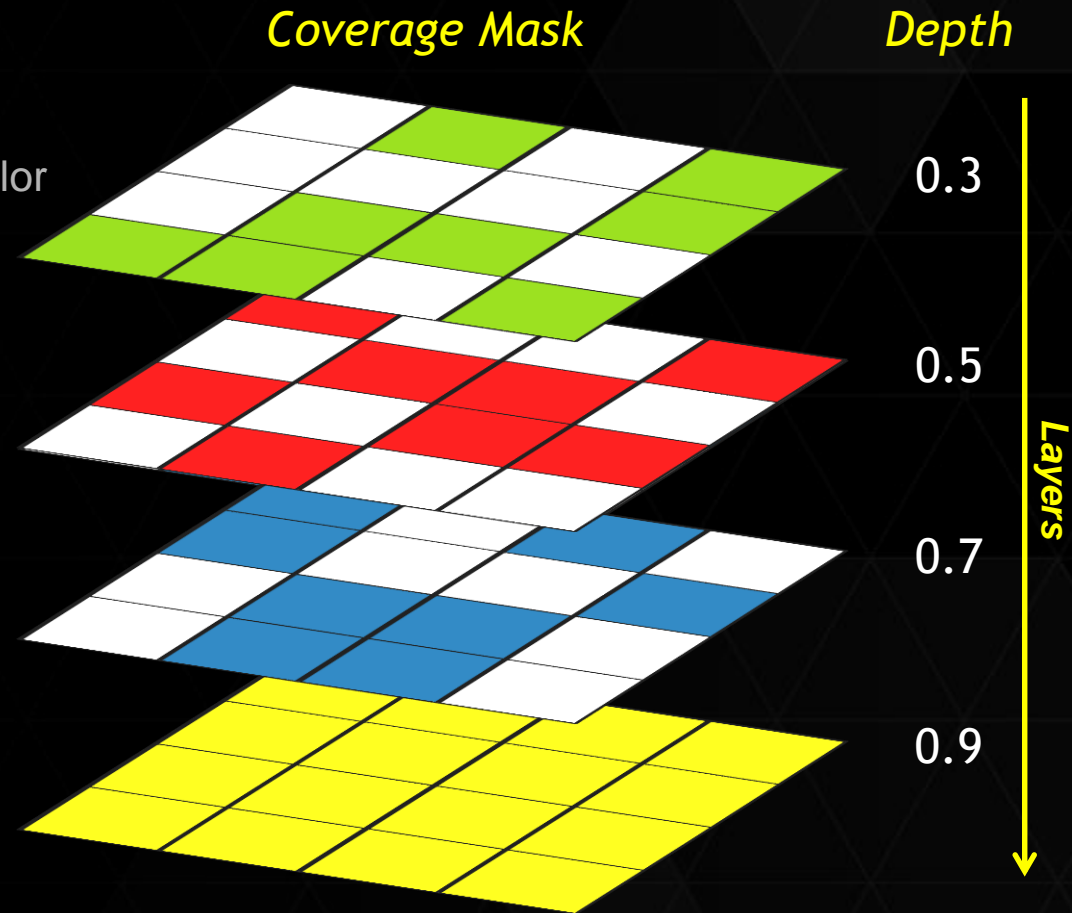
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  - ▶ Fourth: draw yellow fragment,  $z = 0.9$ ,  $\alpha = 1.0$
- ▶ Layers get inserted only if not occluded
  - ▶ Adds stochasm, if masks randomly chosen
  - ▶ Different random masks might keep this layer
- ▶ If  $k = 2$ , layers beyond 2<sup>nd</sup> get discarded





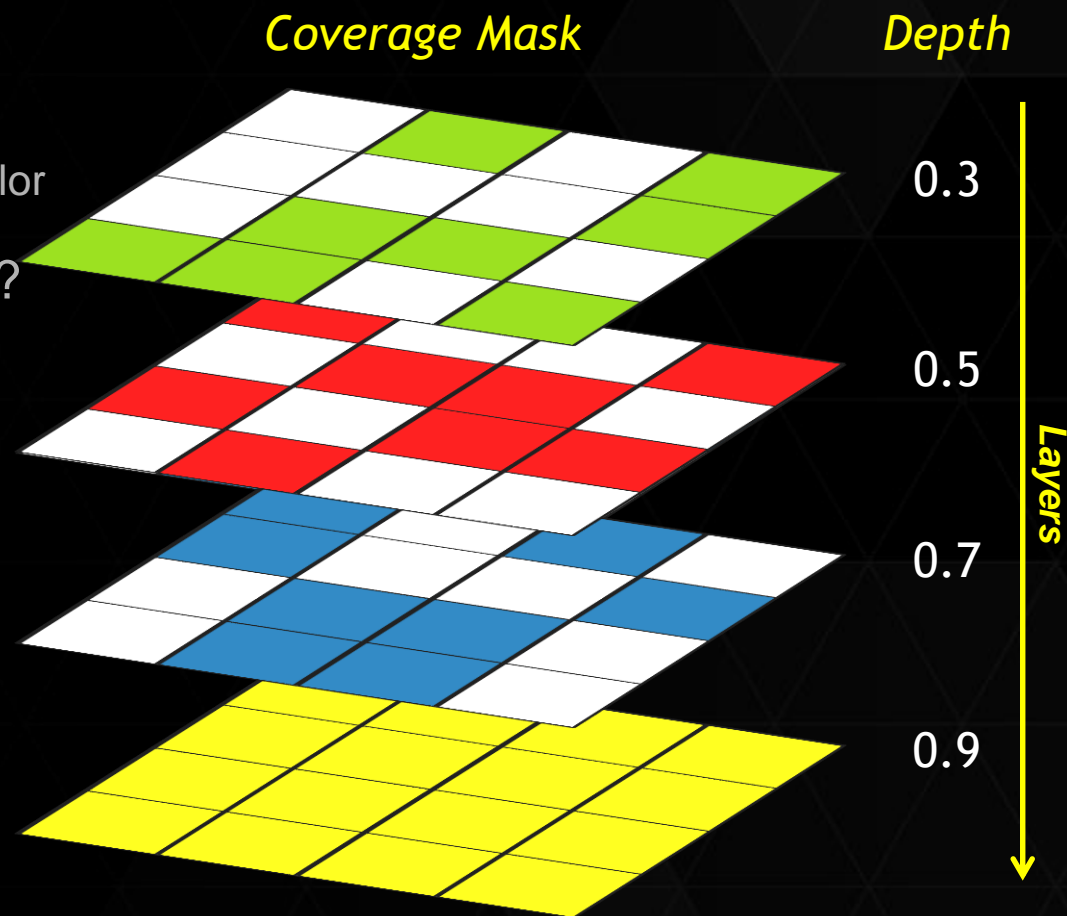
# ADJUSTING PARAMETERS

- ▶ Aim to reduce noise
  - ▶ One way: avoid discarding layers that impact color



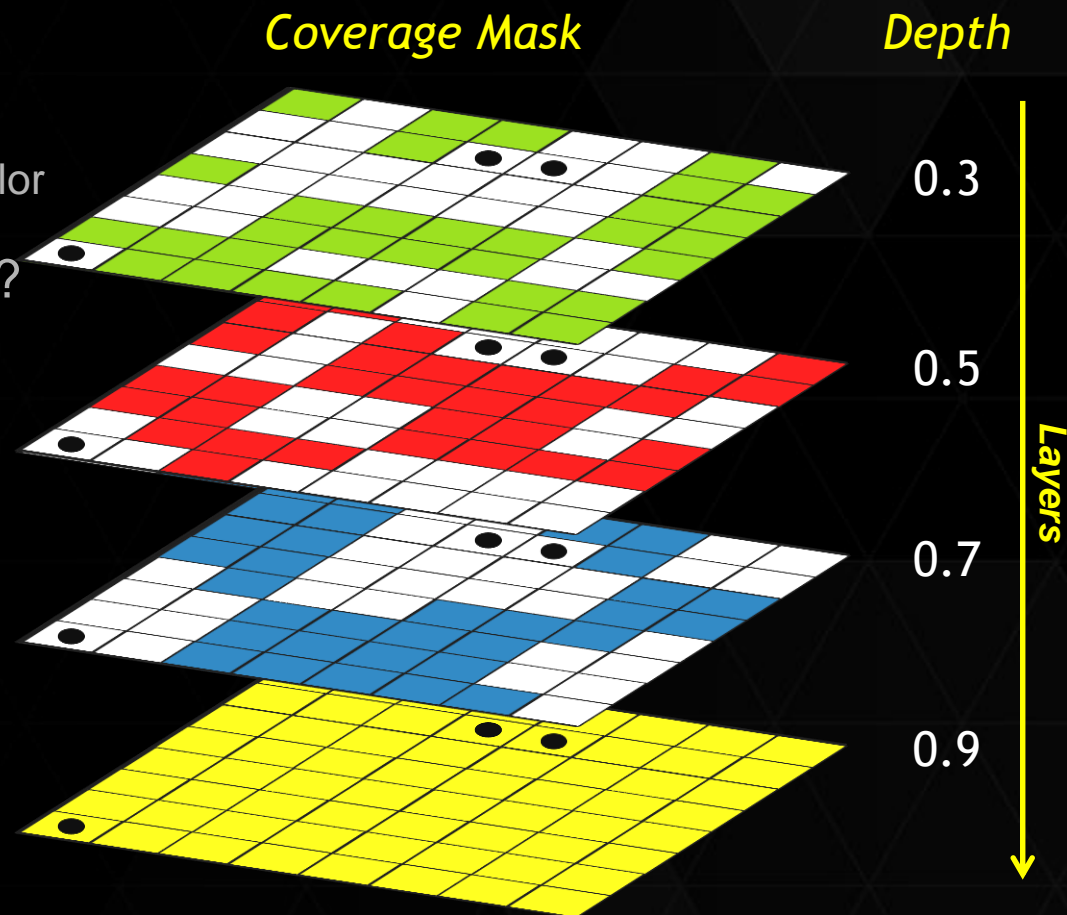
# ADJUSTING PARAMETERS

- ▶ Aim to reduce noise
  - ▶ One way: avoid discarding layers that impact color
- ▶ How to increase chance to store yellow frag?



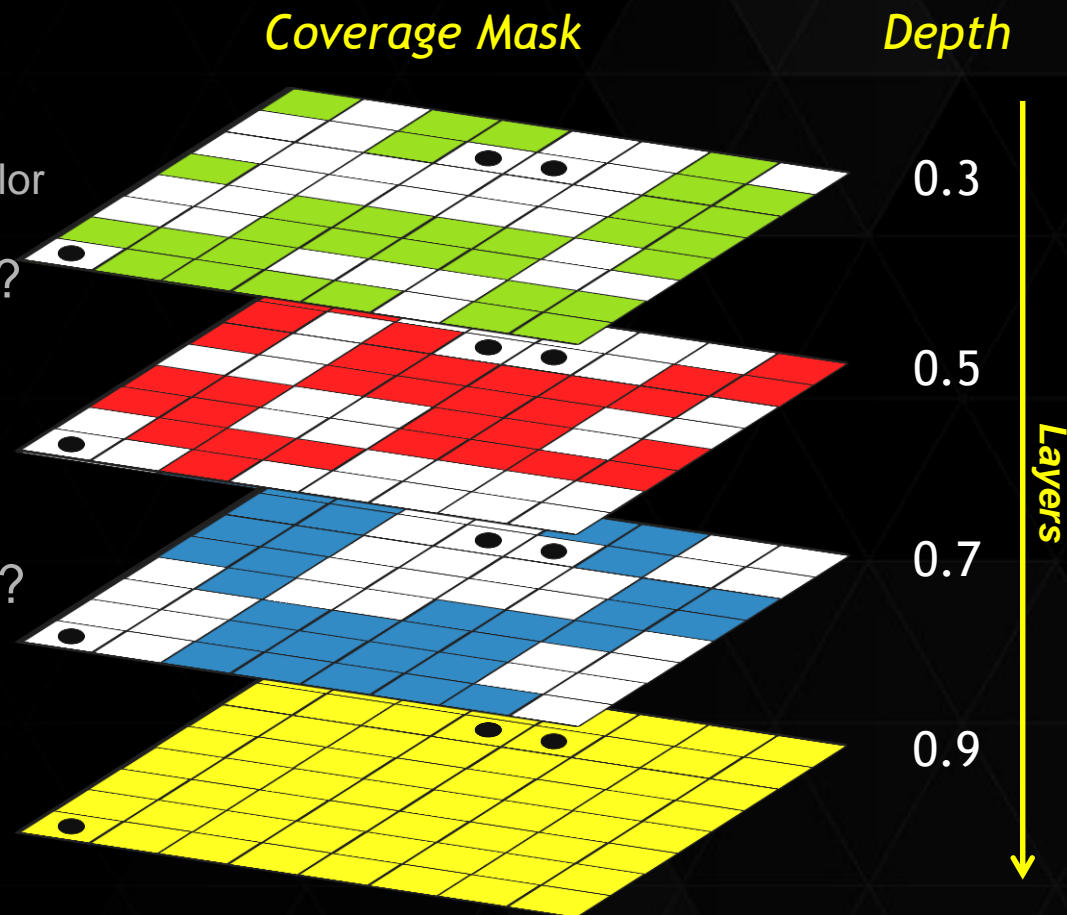
# ADJUSTING PARAMETERS

- ▶ Aim to reduce noise
  - ▶ One way: avoid discarding layers that impact color
- ▶ How to increase chance to store yellow frag?
  - ▶ Increase number of bits in coverage mask



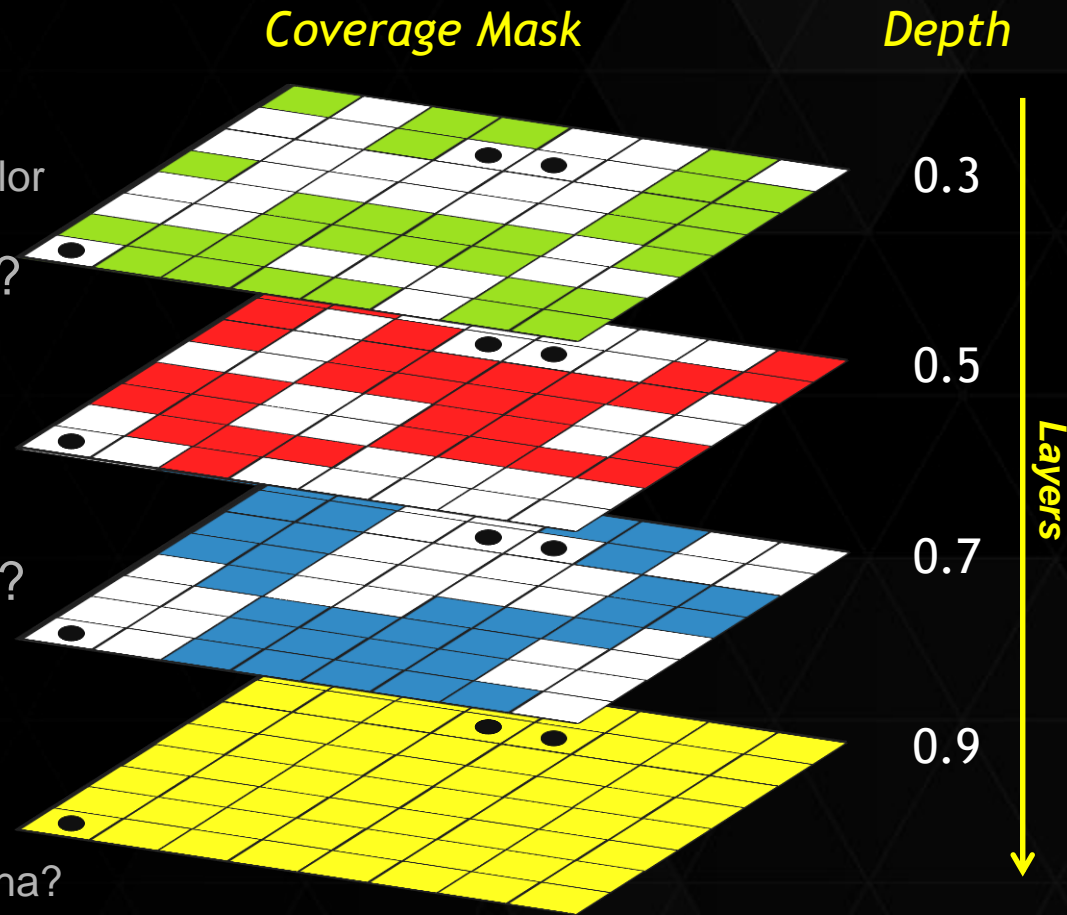
# ADJUSTING PARAMETERS

- ▶ Aim to reduce noise
  - ▶ One way: avoid discarding layers that impact color
- ▶ How to increase chance to store yellow frag?
  - ▶ Increase number of bits in coverage mask
- ▶ Larger coverage masks → lower noise
- ▶ What happens as # coverage bits increases?



# ADJUSTING PARAMETERS

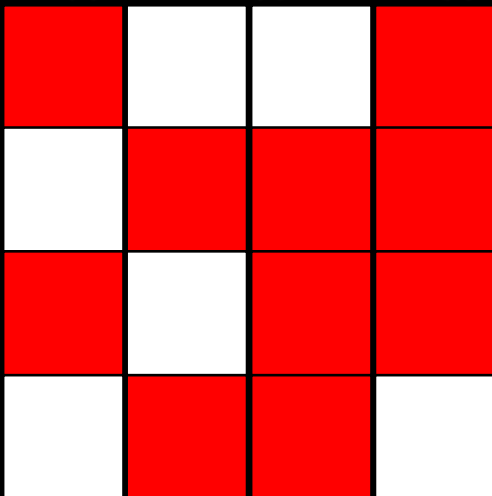
- ▶ Aim to reduce noise
  - ▶ One way: avoid discarding layers that impact color
- ▶ How to increase chance to store yellow frag?
  - ▶ Increase number of bits in coverage mask
- ▶ Larger coverage masks → lower noise
- ▶ What happens as # coverage bits increases?
  - ▶ Starts to behave as alpha
- ▶ Interesting to ask:
  - ▶ Can we stochastically insert fragments using alpha?



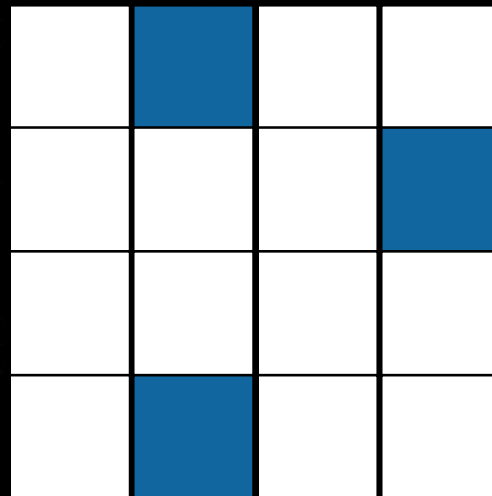
# SLAB USING IMPLICIT COVERAGE

- ▶ Let's compute an insertion probability
  - ▶ Q: What's the chance random bitmask B is visible behind random bitmask A?

Bitmask A



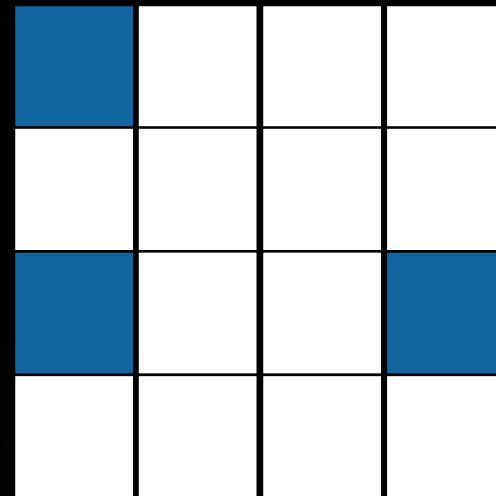
Bitmask B<sub>0</sub>



Visible



Bitmask B<sub>1</sub>

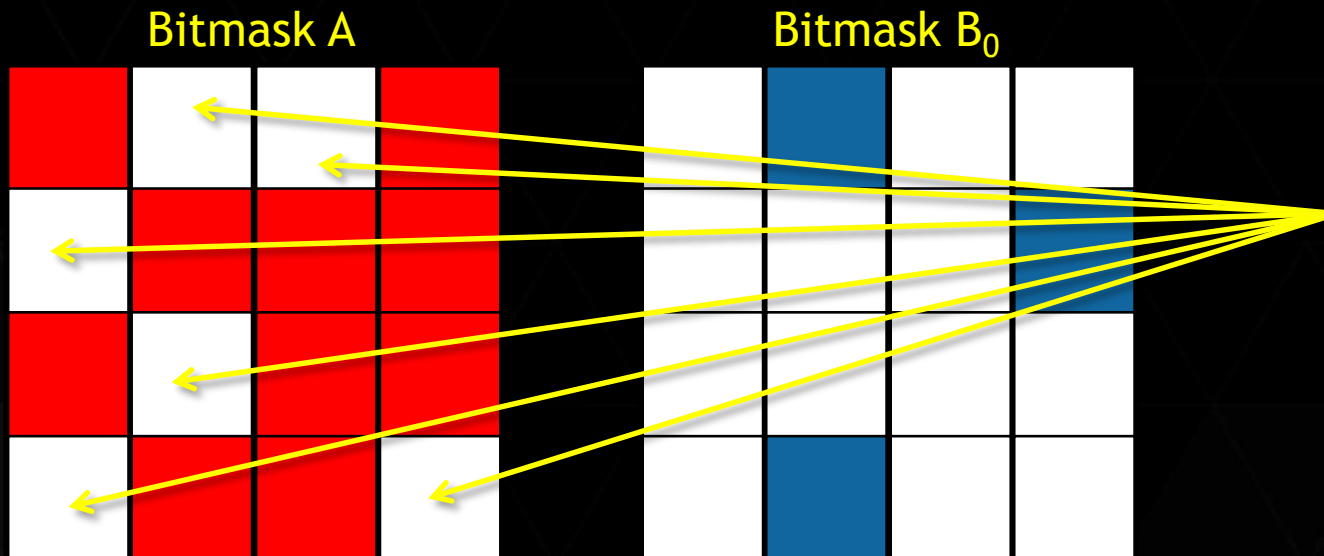


Hidden



# SLAB USING IMPLICIT COVERAGE

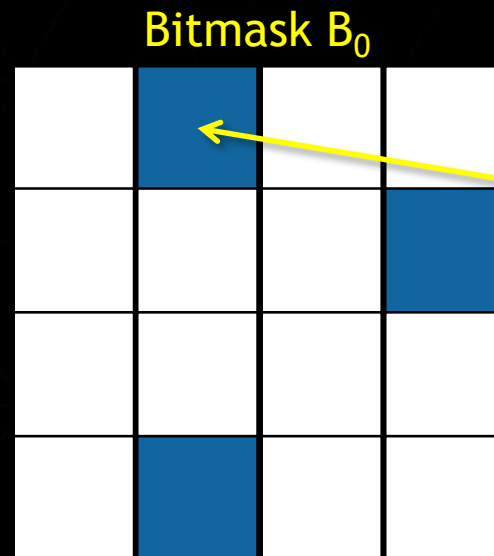
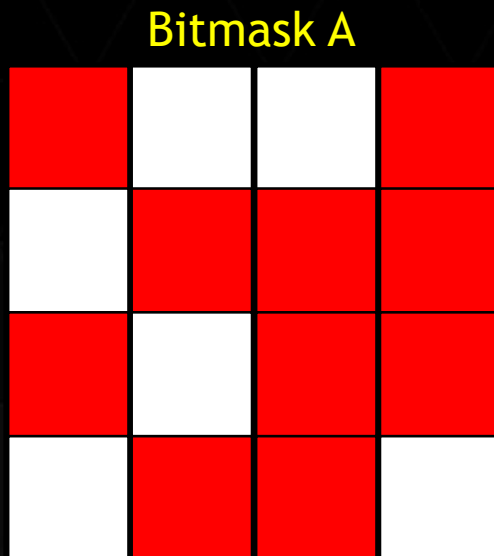
- ▶ Let's compute an insertion probability
  - ▶ Q: What's the chance random bitmask B is visible behind random bitmask A?



Hidden if *none* of these get covered by bits in bitmask B

# SLAB USING IMPLICIT COVERAGE

- ▶ Let's compute an insertion probability
  - ▶ Q: What's the chance random bitmask B is visible behind random bitmask A?

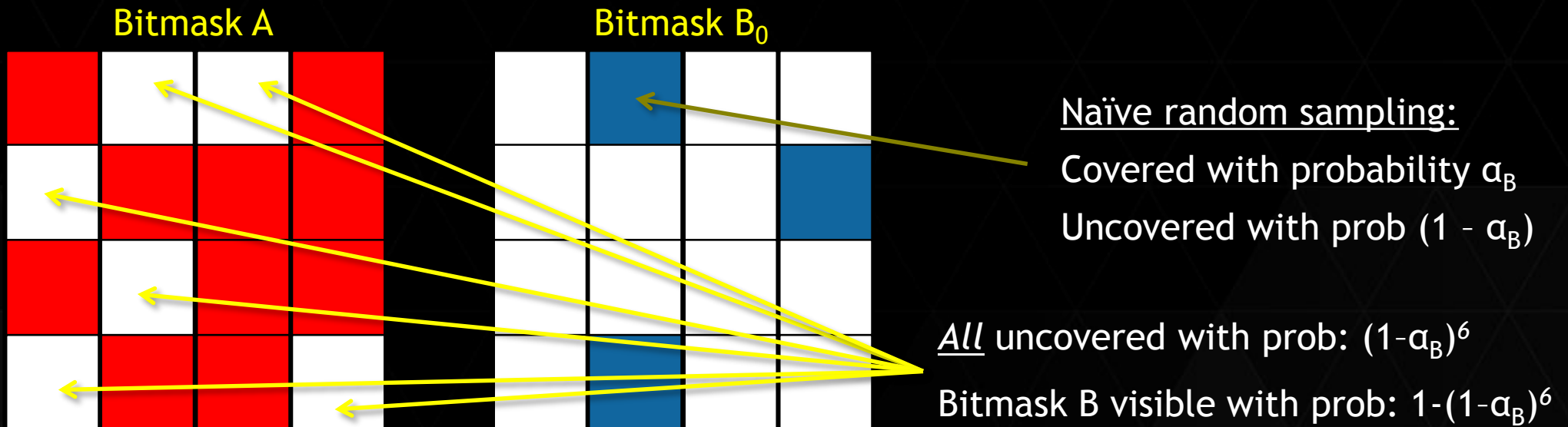


Naïve random sampling:  
Covered with probability  $\alpha_B$   
Uncovered with prob  $(1 - \alpha_B)$



# SLAB USING IMPLICIT COVERAGE

- ▶ Let's compute an insertion probability
  - ▶ Q: What's the chance random bitmask B is visible behind random bitmask A?



# SLAB USING IMPLICIT COVERAGE

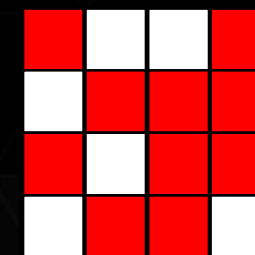
- ▶ Let's compute an insertion probability
  - ▶ Q: What's the chance random bitmask B is visible behind random bitmask A?

$$P_b(\beta_A, \beta_B) = 1 - \left(1 - \frac{\beta_B}{b}\right)^{(b - \beta_A)}$$

Or

$$P_b(\beta_A, \alpha_B) = 1 - (1 - \alpha_B)^{(b - \beta_A)}$$

Bitmask A



$\beta_A \equiv \#$  bits covered  
 $\beta_A = \lfloor \alpha_A b \rfloor$  or  $\lceil \alpha_A b \rceil$   
for  $b$  bits in bitmask

# SLAB USING IMPLICIT COVERAGE

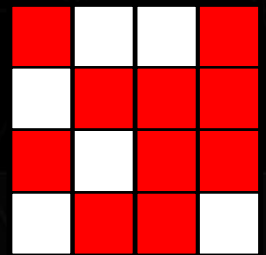
- ▶ Let's compute an insertion probability
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$$P_b(\beta_A, \beta_B) = 1 - \left(1 - \frac{\beta_B}{b}\right)^{(b - \beta_A)}$$

Or

$$P_b(\beta_A, \alpha_B) = 1 - \underbrace{\left(1 - \alpha_B\right)}_{\text{prob of leaving 1 bit uncovered}} \underbrace{\left(b - \beta_A\right)}_{\text{number of bits that must be uncovered}}$$

Bitmask A



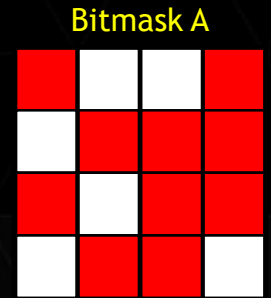
$\beta_A \equiv \#$  bits covered

$\beta_A = \lfloor \alpha_A b \rfloor$  or  $\lceil \alpha_A b \rceil$   
for  $b$  bits in bitmask

# SLAB USING IMPLICIT COVERAGE

- ▶ Let's compute an insertion probability
  - ▶ Q: How about for random masks using stratified samples?

$$P_b(\beta_A, \beta_B) = \begin{cases} 1 - \frac{\beta_A!(b-\beta_B)!}{b!(\beta_A-\beta_B)!} & \text{if } \beta_B \leq \beta_A \\ 1 & \text{if } \beta_B > \beta_A \end{cases}$$



$\beta_A \equiv \#$  bits covered

- ▶ Based on combinatorics
  - ▶ Choosing dependent probabilities so all mask bits in B are covered by A

# WAIT! NOT USING INFINITE # BITS?

- ▶ Both equations require a number of bits  $b$  in the coverage mask

$$P_b(\beta_A, \beta_B) = \begin{cases} 1 - \frac{\beta_A!(b-\beta_B)!}{b!(\beta_A-\beta_B)!} & \text{if } \beta_B \leq \beta_A \\ 1 & \text{if } \beta_B > \beta_A \end{cases}$$

*using stratified random samples*

$$P_b(\beta_A, \beta_B) = 1 - \left(1 - \frac{\beta_B}{b}\right)^{(b-\beta_A)}$$

*using naïve random samples*

# WAIT! NOT USING INFINITE # BITS?

- ▶ Both equations require a number of bits  $b$  in the coverage mask
  - ▶ Can ask what happens to  $P_b$  as  $b \rightarrow \infty$
  - ▶ Turns out as  $b \rightarrow \infty$ ,  $P_b \rightarrow 1$
  - ▶ Instead of *stochastic* insertion of fragments, they're *always* inserted

$$P_b(\beta_A, \beta_B) = \begin{cases} 1 - \frac{\beta_A!(b-\beta_B)!}{b!(\beta_A-\beta_B)!} & \text{if } \beta_B \leq \beta_A \\ 1 & \text{if } \beta_B > \beta_A \end{cases} \quad \text{using stratified random samples}$$

$$P_b(\beta_A, \beta_B) = 1 - \left(1 - \frac{\beta_B}{b}\right)^{(b-\beta_A)} \quad \text{using naïve random samples}$$

# WAIT! NOT USING INFINITE # BITS?

- ▶ Both equations require a number of bits  $b$  in the coverage mask
  - ▶ Can ask what happens to  $P_b$  as  $b \rightarrow \infty$
  - ▶ Turns out as  $b \rightarrow \infty$ ,  $P_b \rightarrow 1$
  - ▶ Instead of *stochastic* insertion of fragments, they're *always* inserted
- ▶ Going back to our continuum
  - ▶ When  $b = k$ , SLAB is equivalent to stochastic transparency
  - ▶ When  $b \rightarrow \infty$ , SLAB is equivalent to hybrid transparency (a variant of k-buffer)

Stochastic Transparency [ESSL10]	k samples	stochastic	z-test, discard occluded	$\alpha$ -weighted average	coverage
Hybrid Transparency [MCTB13]	k layers	always	discard furthest	$\alpha$ -weighted average	alpha
(NEW) Stochastic Layered Alpha Blending	k layers	stochastic	discard furthest	$\alpha$ -weighted average	either <sup>†</sup>

# WAIT! NOT USING INFINITE # BITS?

- ▶ To get something between k-buffers and stoc. transp.
  - ▶ Need to use  $k \leq b < \infty$



# WAIT! NOT USING INFINITE # BITS?

- ▶ To get something between k-buffers and stoc. transp.
  - ▶ Need to use  $k \leq b < \infty$
  - ▶ Can do this with an *explicit* coverage mask with b random bits
    - ▶ Using deterministic insertion based on random coverage masks

# WAIT! NOT USING INFINITE # BITS?

- ▶ To get something between k-buffers and stoc. transp.
  - ▶ Need to use  $k \leq b < \infty$
  - ▶ Can do this with an *explicit* coverage mask with  $b$  random bits
    - ▶ Using deterministic insertion based on random coverage masks
  - ▶ Can do this with an *implicit* coverage (i.e., alpha) using  $b$  *virtual* bits
    - ▶ Using stochastic insertion using probability functions
    - ▶  $b$  only controls distance along the k-buffer  $\leftrightarrow$  stoc transp continuum

**Let's demonstrate**

# FOLIAGE MAP

(From Epic's Unreal SDK)

All surfaces  $\alpha = 0.5$



# FOLIAGE MAP

(From Epic's Unreal SDK)

All surfaces  $\alpha = 0.5$



Stoc transp, 8 spp

SLAB,  $k = b = 8$

SLAB,  $k = 8, b = 32$

SLAB,  $k = 8, b = 128$

SLAB,  $k = 8, b = 32$   
using alpha

Hybrid Transparency



# FOLIAGE MAP

(From Epic's Unreal SDK)

All surfaces  $\alpha = 0.5$




Stoc transp, 8 spp

SLAB,  $k = b = 8$

SLAB,  $k = 8, b = 32$

SLAB,  $k = 8, b = 128$

SLAB,  $k = 8, b = 32$   
using alpha

Hybrid Transparency  NVIDIA

# FOLIAGE MAP

(From Epic's Unreal SDK)

All surfaces  $\alpha = 0.5$




Stoc transp, 8 spp

SLAB,  $k = b = 8$

SLAB,  $k = 8, b = 32$

SLAB,  $k = 8, b = 128$

SLAB,  $k = 8, b = 32$   
using alpha

Hybrid Transparency  NVIDIA

# STOCHASTIC TRANSPARENCY TO K-BUFFERS



Stochastic Layered Alpha Blending,  $k=b=4$



Stochastic Transparency, 4 spp



# STOCHASTIC TRANSPARENCY TO K-BUFFERS



Stochastic Layered Alpha Blending,  $k=4$ ,  $b=32$



Stochastic Transparency, 4 spp

# STOCHASTIC TRANSPARENCY TO K-BUFFERS



Stochastic Layered Alpha Blending,  $k=4$ ,  $b=8$   
(using alpha rather than coverage)



Stochastic Transparency, 4 spp

# STOCHASTIC TRANSPARENCY TO K-BUFFERS



Stochastic Layered Alpha Blending,  $k=4$ ,  $b=32$   
(using alpha rather than coverage)



Hybrid Transparency, 4 layers

# Summary

# SUMMARY

- ▶ Introduced an OIT continuum
  - ▶ More detailed discussion in the paper
  - ▶ My key takeaways
    - ▶ All OIT algorithms limit memory by using  $k$  “layers” ( $k=0,1,4,8,32$  common)
    - ▶ Biggest difference is merge heuristic
    - ▶ Some algorithm do renormalization; just a fancy merge heuristic
    - ▶ Insertion via stochastic processes is underexplored
    - ▶ Algorithms using coverage masks are underexplored

# SUMMARY

- ▶ Proposed two new algorithms
  - ▶ Stochastic layered alpha blending (SLAB)
  - ▶ Multi-layer coverage blending (MLCB)
    - ▶ Not discussed today, see paper for details
    - ▶ Explored combining OIT + MSAA sampling

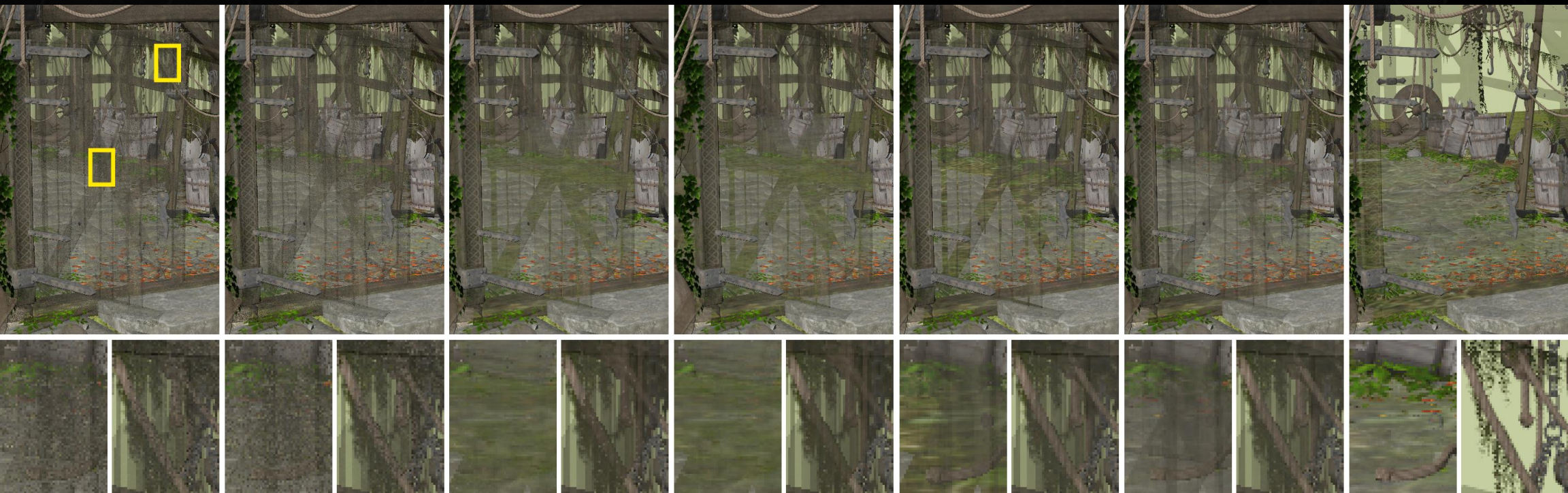
# SUMMARY

- ▶ Proposed two new algorithms
  - ▶ Stochastic layered alpha blending (SLAB)
  - ▶ Key takeaways:
    - ▶ K-buffers need not be deterministic
    - ▶ Stochastic transparency and k-buffering are similar; transition via bit count
    - ▶ “Stochastic” need not mean random bitmask generation
    - ▶ Algorithms connecting others useful; here, allow trading noise for bias
    - ▶ SLAB with alpha values can stratify samples in z (between layers)
      - (Not really discussed in this talk)

# QUESTIONS?

E-mail: [cwyman@nvidia.com](mailto:cwyman@nvidia.com), Twitter: [@\\_cwyman\\_](https://twitter.com/_cwyman_)

Blacksmith building, from Unity's "The Blacksmith" demo



Stochastic  
transparency  
4 spp

SLAB  
 $k = 4, b = 4$

SLAB  
 $k = 4, b = 16$   
using alpha

Hybrid  
transparency  
4 layers

Multi-layer  
alpha blending  
4 layers

Ground truth  
(A-buffer)

8x MSAA,  
alpha-to-coverage